

Name: \_\_\_\_\_

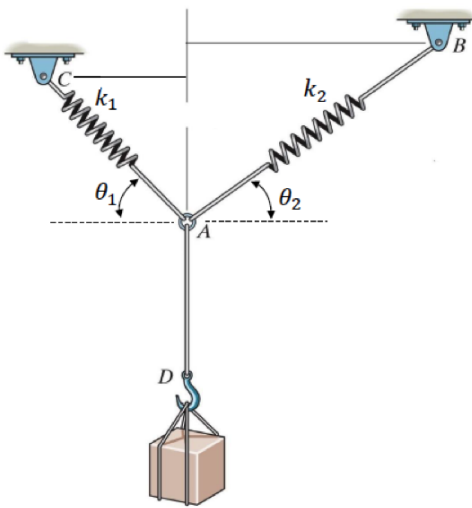
Group members: \_\_\_\_\_

### TAM 210/211 - Worksheet 3

Objectives:

- Use free body diagrams and equilibrium equations to determine forces in cables and springs.

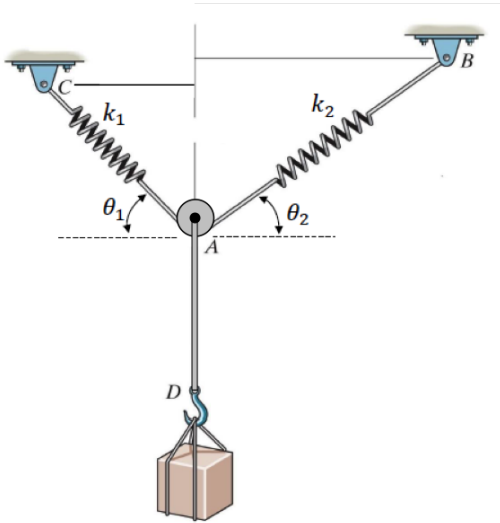
1) A box of weight  $W$  is supported by two springs, as illustrated below.



a) Next to spring-mass figure above, draw a free body diagram for ring  $A$ . Denote the force in spring  $AC$  as  $F_{AC}$  and the force in spring  $AB$  as  $F_{AB}$ .

b) Use the equilibrium equations  $\sum \mathbf{F} = \mathbf{0}$  to determine  $F_{AC}$  and  $F_{AB}$ . Your answers should be functions of  $W$ ,  $\theta_1$  and  $\theta_2$ .

2) In this next setup, the two identical springs are fixed at uneven positions (different heights) again, but the springs are no longer connected to each other via a ring. Instead, connect the springs using a piece of string, to model the cable that goes through the pulley at  $A$ .

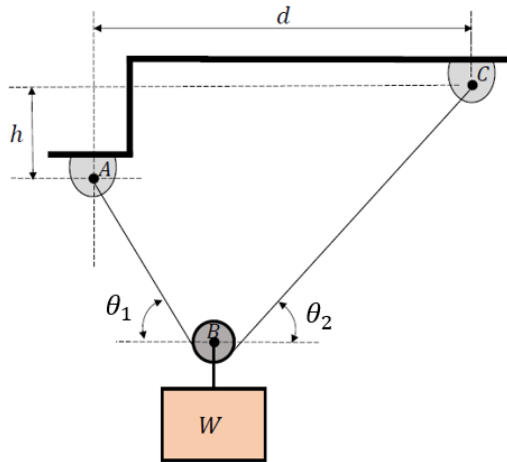


a) Before doing any calculations, predict if angle  $\theta_1$  would be greater than, less than, or equal to  $\theta_2$ . Explain your reasoning.

b) The tension in the cable over a pulley is constant everywhere for a static system. Show that if spring constants  $k_1$  and  $k_2$  are equal,  $\theta_1$  and  $\theta_2$  must also be equal.

c) Express the magnitude of the forces in the springs as a function of  $W$ ,  $\theta_1$ , and  $\theta_2$ .

3) Another setup is illustrated below with string  $ABC$  of length  $L$ .



a) What happens to angles  $\theta_1$  and  $\theta_2$  when the weight  $W$  is changed by changing the object? Why?

b) How do angles  $\theta_1$  and  $\theta_2$  relate to each other? Express the angles **in terms of the given symbolic variables and dimensions** (neglect the size of the frictionless pulley  $B$ ). How does your theoretical expression validate your conclusions in part (a)?

c) Express the forces along  $AB$  and  $BC$  as Cartesian vectors in terms of the given symbolic variables and dimensions.

d) If the string  $ABC$  were shorter, how would angles  $\theta_1$  and  $\theta_2$  and the forces along  $AB$  and  $BC$  change?

e) What implications does part (d) have on the design of systems with different string lengths in terms of the required strengths of the strings?