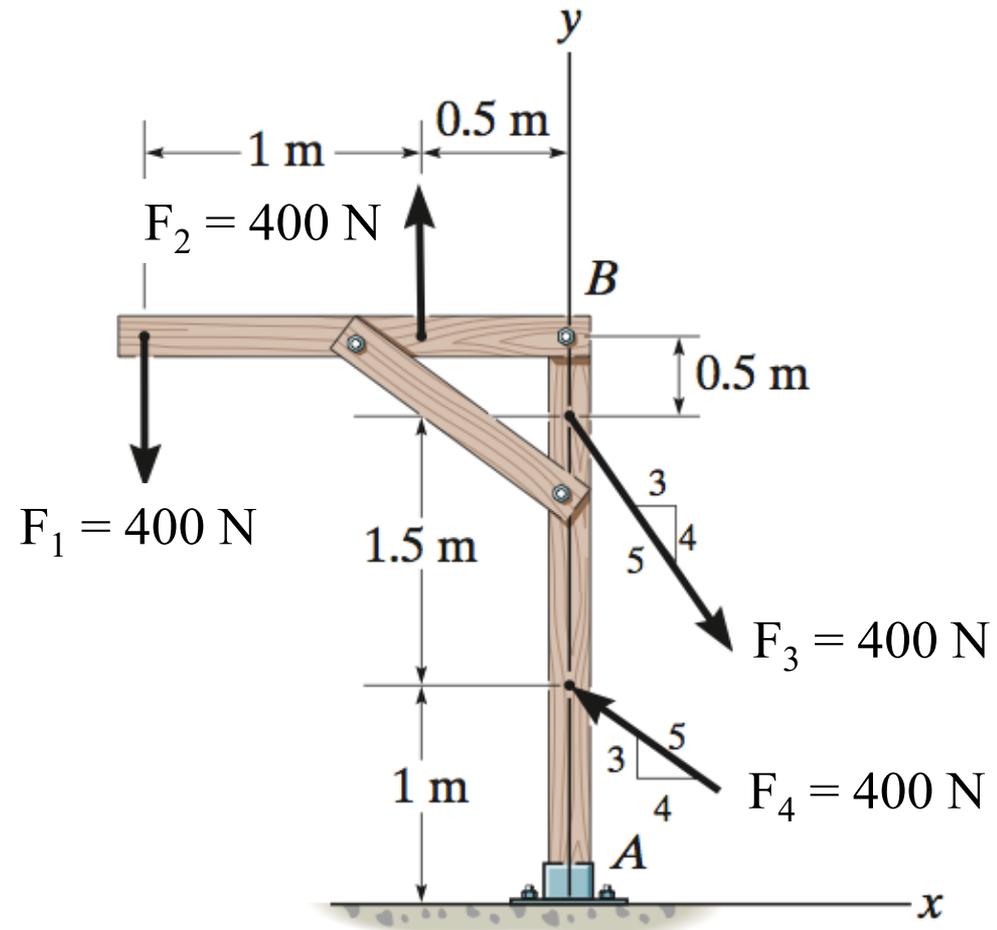


# Objective

- Equivalent Systems
  - Force
  - Moment
  - Distributed load

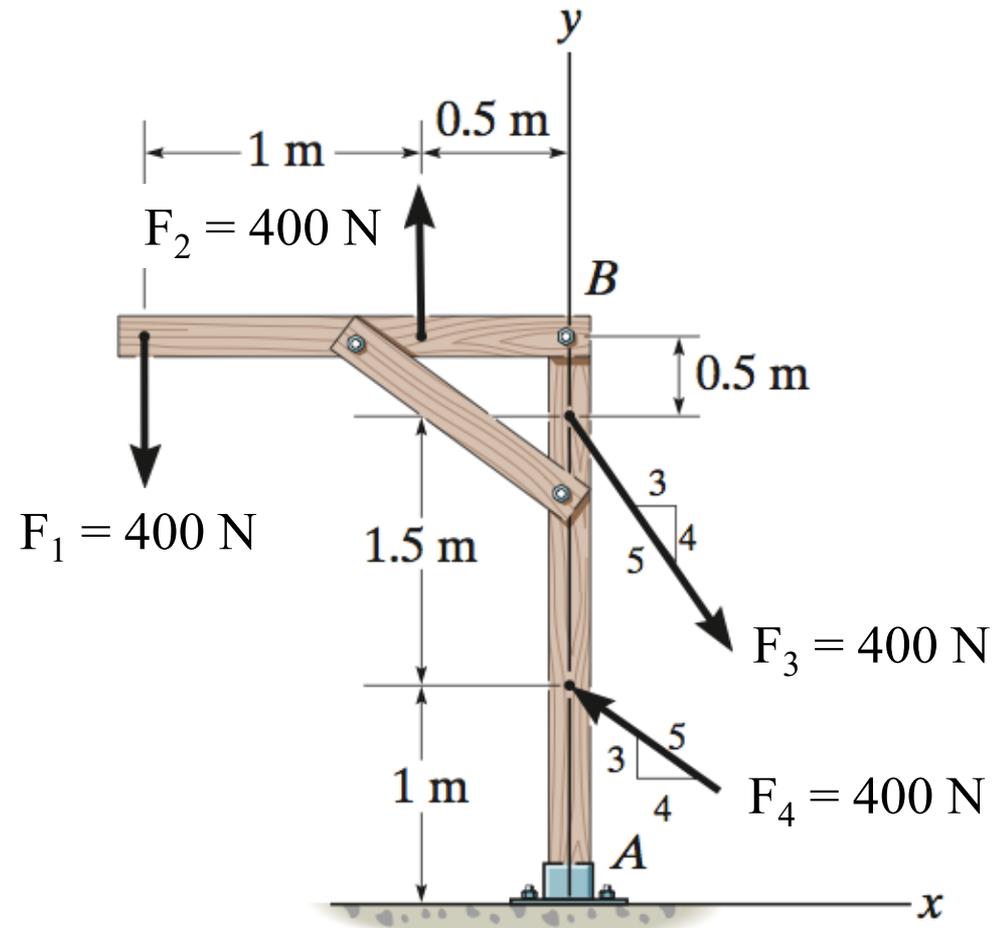
# Example – 2D Equivalent System

What is the resultant force and moment on point  $A$  and  $B$  from  $F_1$  and  $F_2$ ?



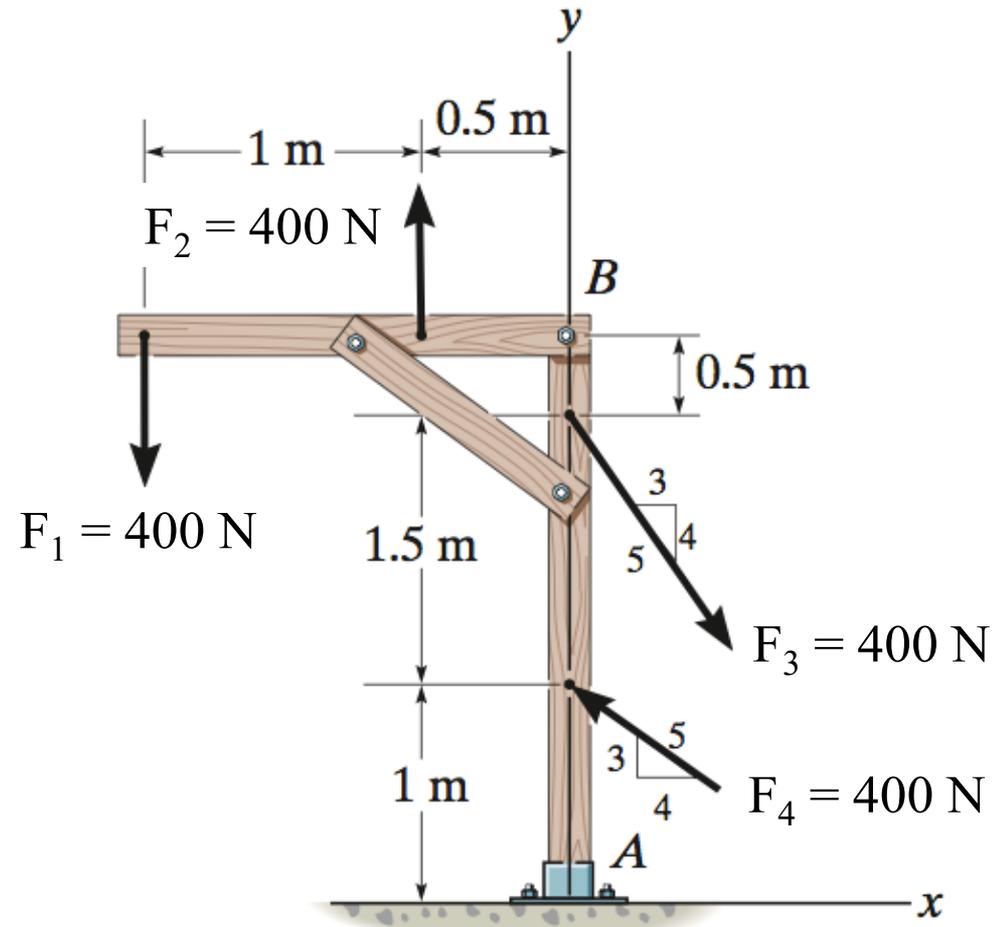
# Example – 2D Equivalent System

What is the resultant force and moment on point  $A$  and  $B$  from  $F_3$  and  $F_4$ ?



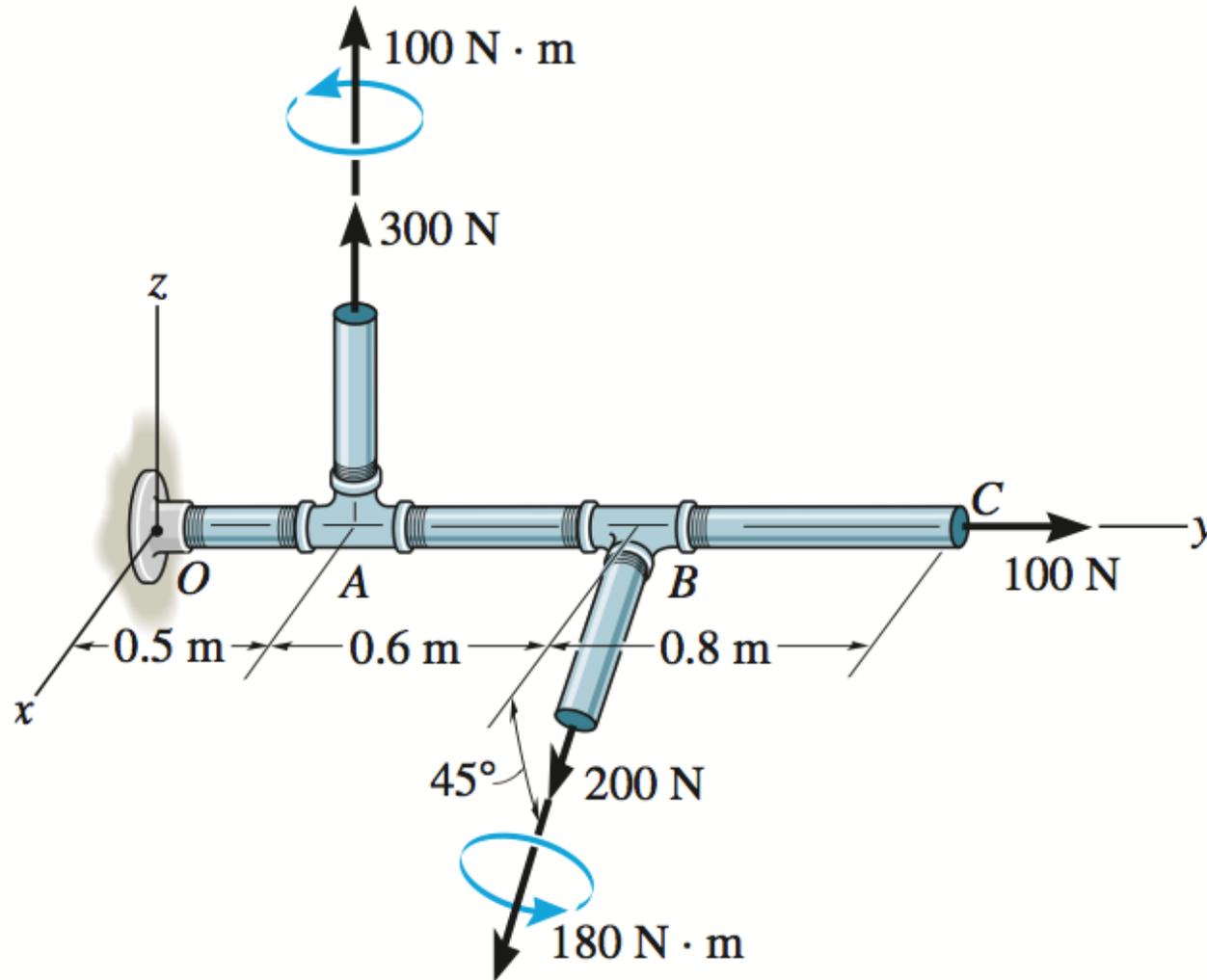
# Example – 2D Equivalent System

Replace the loading on the frame by a single resultant force. Specify where its line of action intersects a vertical line along member  $AB$ , measured from  $A$ .



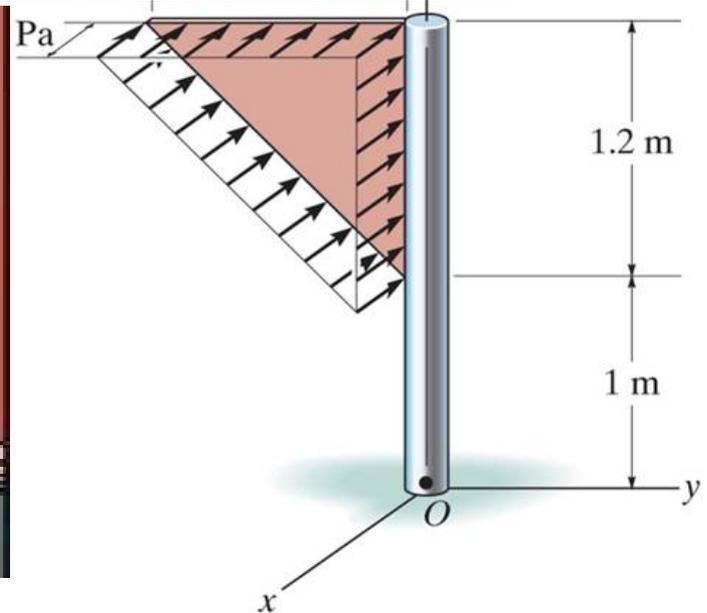
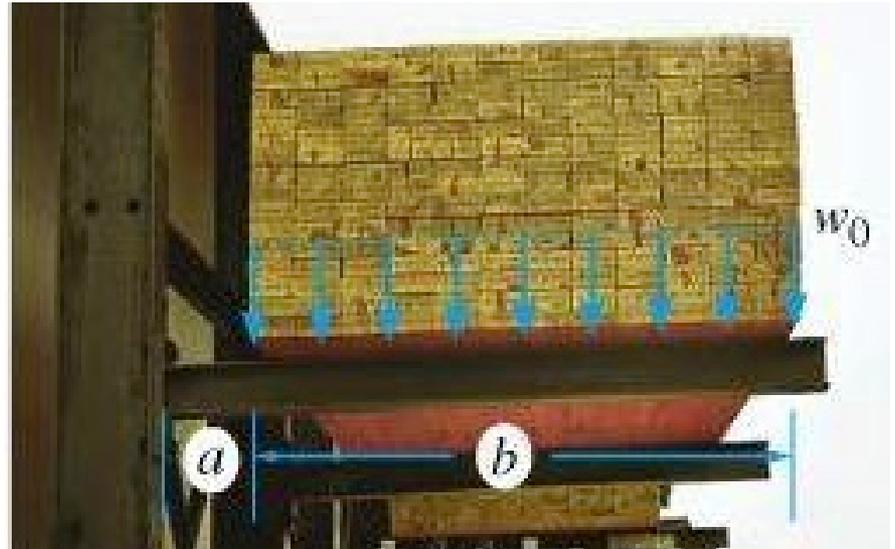
# Example – 3D Equivalent System

Find the equivalent resultant force and couple moment at point  $O$  as the the two wrenches and the force acting on the pipe assembly below.



# Distributed Loading

What is the equivalent sys...



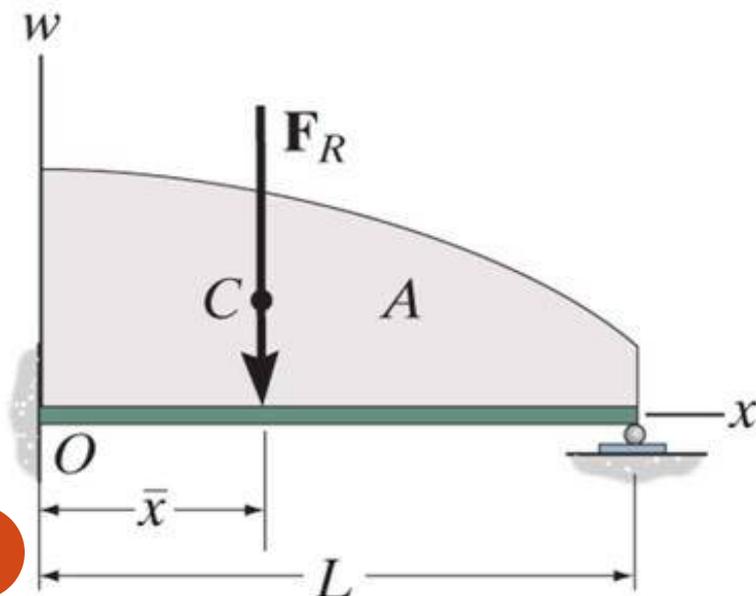
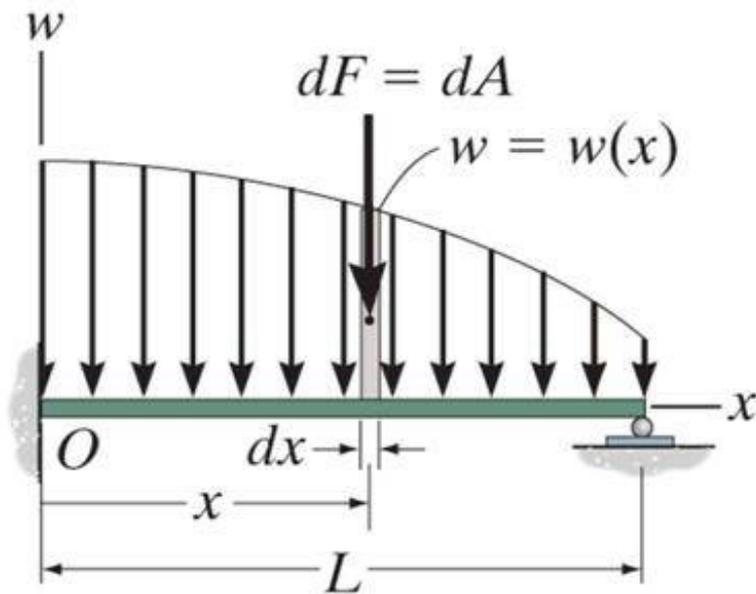
# Distributed Loading

A common case of distributed loading in a uniform load along one axis of a flat rectangular body.

In such cases,  $w$  is a function of  $x$  and has units of

Consider an element of length  $dx$ . The force magnitude  $dF$  acting on it is given as

The net force on the beam is given by



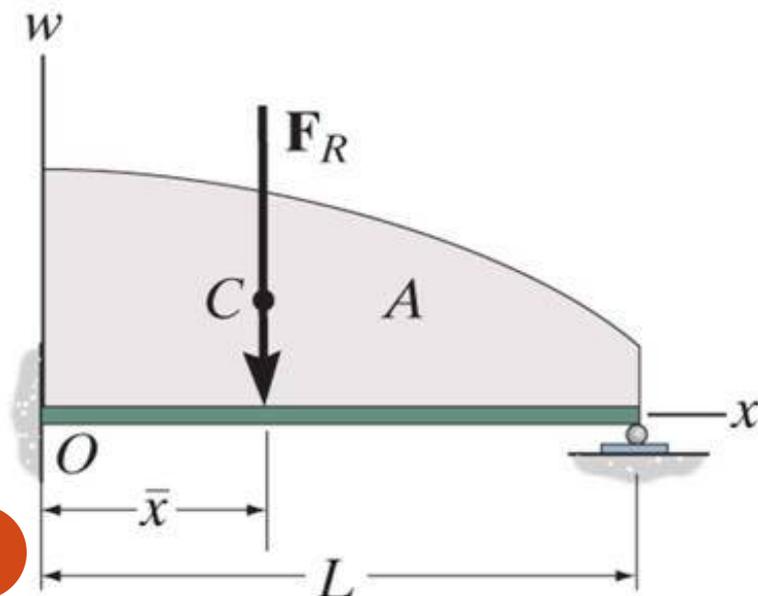
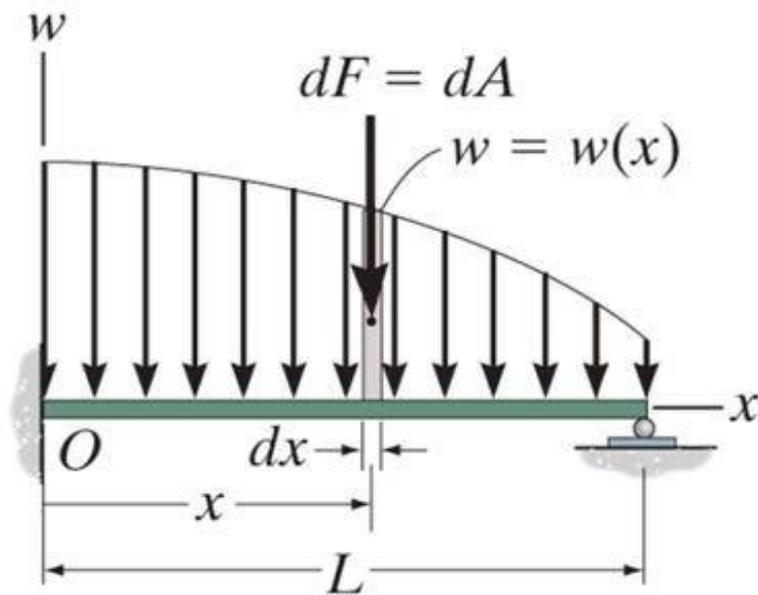
# Location of the Resultant Force

The force  $dF$  will produce a moment about  $O$  of

The total moment about point  $O$  is

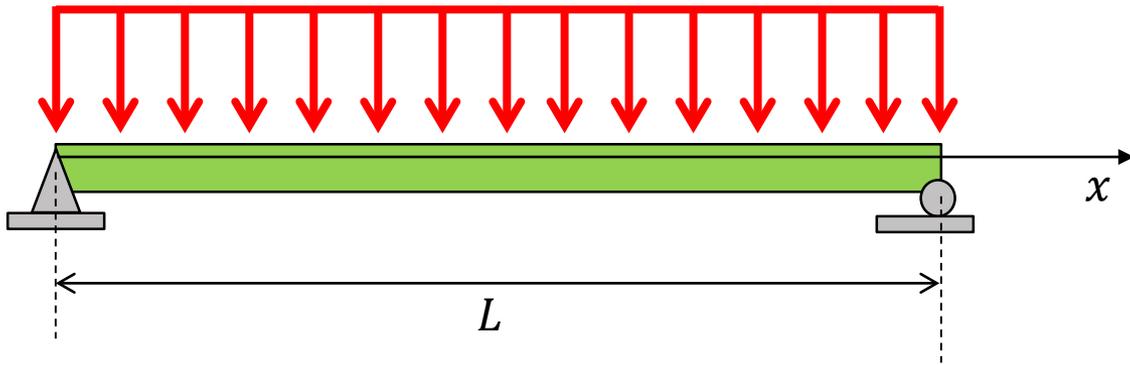
Assuming that  $F_R$  acts at  $\bar{x}$ , it will produce the moment about point  $O$  as

Hence,

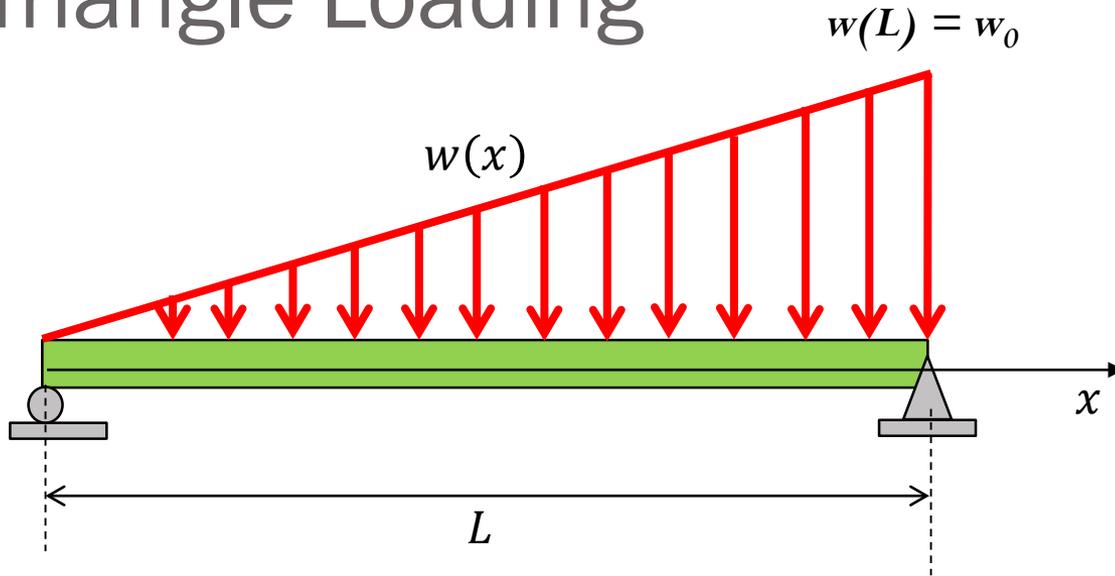


# Rectangle Loading

$$w(x) = w_0$$

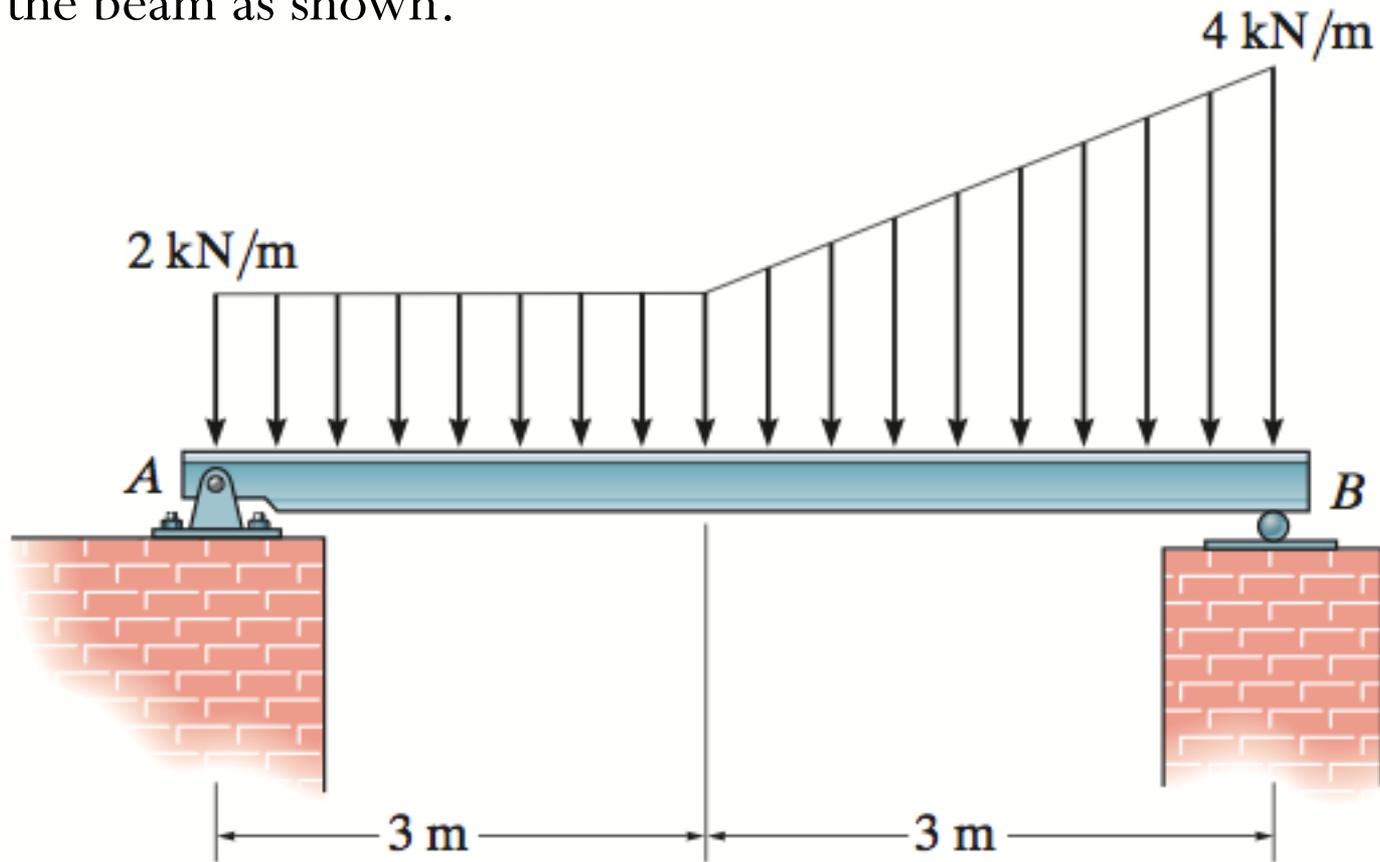


# Triangle Loading



# Example

Find the equivalent force and its location from point  $A$  for the loading on the beam as shown.



# Example

Find the equivalent force and its location from point A for the loading on the beam as shown.

