

## Announcements

- Last day of class: Monday, Dec. 9
- No discussion sections next week
- Last day of office hours and Piazza help: Wednesday, Dec. 12
- CBTF (last) Quiz 6 starts Thursday, Dec. ~~14~~ **13** (thanks Matt)

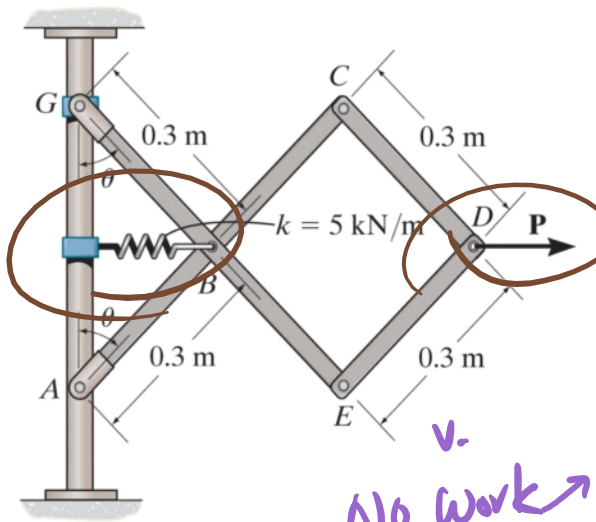
### □ Upcoming deadlines:

- Friday (12/7)
  - Written assignment 9
- Tuesday (12/11)
  - Last PL HW



**HAPPY NINJA DAY!**

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Determine the required force P needed to maintain equilibrium of the scissors linkage when the angle is 60 degrees. The spring is unstretched when the angle is 30 degrees.

**FBD**

No work  $\rightarrow$   $G$

$F$   $\leftarrow$

$A_y$   $\rightarrow$   $A_x$   $\uparrow$

$d r_B$   $\rightarrow$

$d r_D$   $\rightarrow$

$P$   $\rightarrow$

displacement from unstretched length

$F_{spring} = k s = k(l - l_0)$

$$dU = 0 = dU_F + dU_P$$

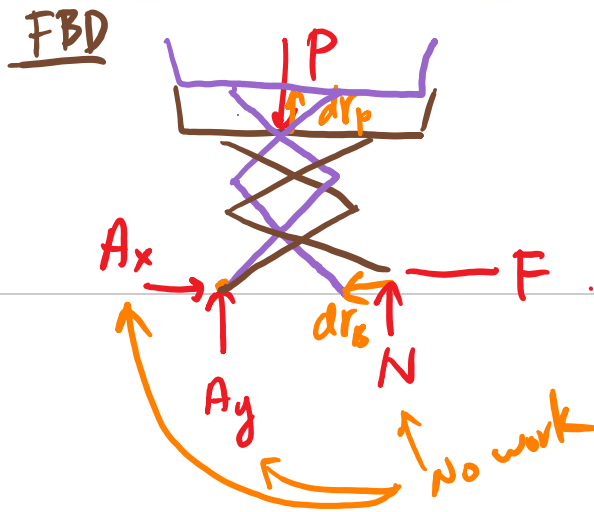
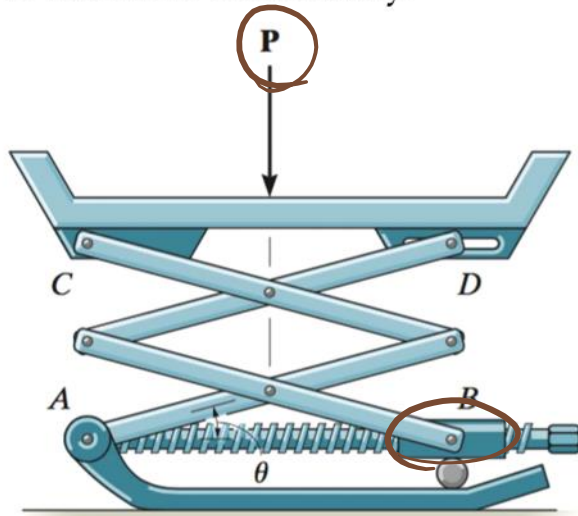
$$dU_F = -F dr_B = -ks(0.3 \cos\theta d\theta)$$

$$dU_P = +P dr_D = +P(0.9 \cos\theta d\theta)$$

$$-0.3ks \cos\theta d\theta + 0.9P \cos\theta d\theta = 0$$

$$\rightarrow P = \frac{ks}{3}$$

The scissors jack supports a load  $P$ . Determine the axial force in the screw necessary for equilibrium when the jack is in the position shown. Each of the four links has a length  $L$  and is pin-connected at its center. Points  $B$  and  $D$  can move horizontally.



$$dU = 0 = dU_p + dU_F$$

$$dr_B = \text{horizontal}$$

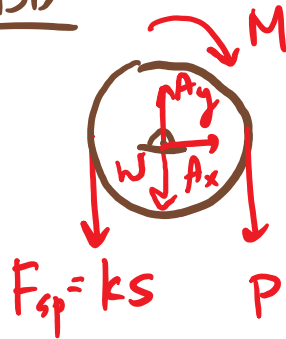
$$dr_p = \text{vertical}$$

$$dU = -P dr_p + F dr_B = -P(2L \cos \theta d\theta) + F(L \sin \theta d\theta) = 0$$

$$F = \frac{2P \cos \theta}{\sin \theta}$$

The disk has a weight of 10 lb and is subjected to a vertical force  $P = 8$  lb and a couple moment  $M = 8$  lb ft. Determine the disk's rotation  $\theta$  if the end of the spring wraps around the periphery of the disk as the disk turns. The spring is originally unstretched.

FBD



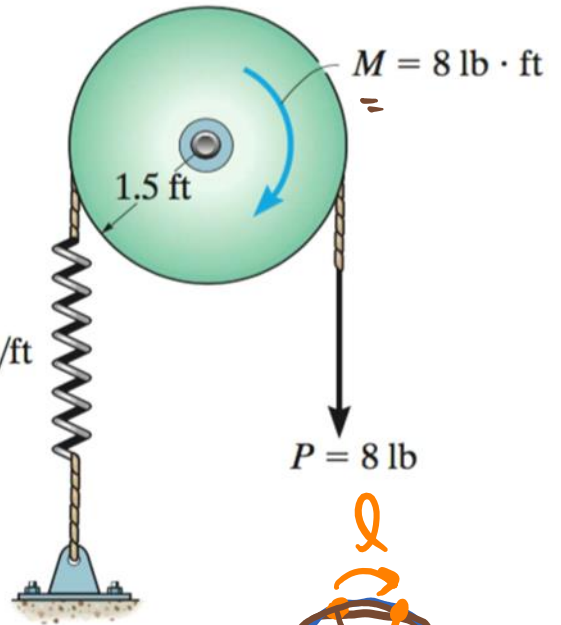
$A_x$  &  $A_y$  won't do work.

$$dU_F = -F dr_c$$

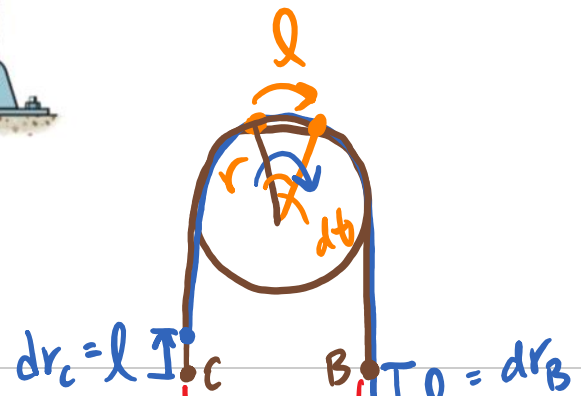
$$dU_M = +M d\theta$$

$$dU_P = +P dr_B$$

$$k = 12 \text{ lb/ft}$$



$$\begin{aligned} dU = 0 &= dU_F + dU_M + dU_P \\ &= -F dr_c + M d\theta + P dr_B \\ &= -F(1.5 d\theta) + M d\theta + P(1.5 d\theta) \end{aligned}$$



$$F = \frac{M + 1.5P}{1.5} = ks$$

$$s = \frac{M + 1.5P}{1.5k} = l = r\theta$$

$$\theta = \frac{M + 1.5P}{1.5kr}$$

$$\text{arc length: } l = r\theta$$

$$dr_B = 1.5 d\theta$$

$$dr_c = 1.5 d\theta$$