#### Announcements

- Quiz 1 Next Week!
- If this is your first week check out the course website for all the logistics you need to know:

https://courses.engr.illinois.edu/tam210

Upcoming deadlines:

- Friday (9/7 TODAY!)
  - Writtein Assignment #1
- Tuesday (9/11)
  - PL HW
- Friday (9/14)
  - Writtein Assignment #2

7th September is...



#### Chapter 3: Equilibrium of a particle

## **Goals and Objectives**

- Practice following general procedure for analysis.
- Introduce the concept of a <u>free-body diagram</u> for an object modeled as a particle.
- Solve particle equilibrium problems using the <u>equations</u> <u>of equilibrium</u>.

# Applications

For a spool of given weight, how would you find the forces in cables AB and AC?

If designing a spreader bar (BC) like this one, you need to know the forces to make sure the rigging (A) doesn't fail.



#### General procedure for analysis

1. Read the problem carefully; write it down carefully.

2. MODEL THE PROBLEM: Draw given diagrams neatly and construct additional figures as necessary.

3. Apply principles needed.

4. Solve problem symbolically. Make sure equations are dimensionally homogeneous

5. Substitute numbers. Provide proper units *throughout*. Check significant figures. Box the final answer(s).

6. See if answer is reasonable.

#### Free body diagram



The lift sling is used to hoist a container having a mass of 500 kg. Determine the force in each of the cables *AB* and *AC* as a function of  $\theta$ .

## Idealizations

Pulleys are (usually) regarded as frictionless; then the tension in a rope or cord around the pulley is the same on either side.



**Frictionless pulley** 

### Idealizations

Springs are (usually) regarded as linearly elastic; then the tension is proportional to the *change* in length *s*.



Linearly elastic spring

#### Idealizations



**Contact force in smooth surface:** 

10 L5 - Force along a line Cross product

#### Free Body Diagram Example



#### Free Body Diagram Example



# Equilibrium of a particle

According to Newton's first law of motion, a particle will be in **equilibrium** (that is, it will remain at rest or continue to move with constant velocity) if and only if

In three dimensions, equilibrium requires:

**Coplanar forces**: if all forces are acting in a single plane, such as the "xy" plane, then the equilibrium condition becomes

#### Example

If the spring *DB* has an unstretched length of 2 m, determine the stiffness of the spring to hold the 40- 2 m kg crate in the position shown.



#### Example



Determine the distances x and y for equilibrium if  $F_1 = 800$  N and  $F_2 = 1000$  N.