## Announcements

- CBTF Quiz 7 this week!
- Last day of office hours and Piazza help: Wed, Dec. 13
- No discussion sections next week
$\square$ Upcoming deadlines:
- Saturday (12/9)
- ME HW27
- Tuesday (12/12)
- PL HW26


Determine the force in member GH of the truss which serves to support the deck of a bridge. State if the member is in tension or compression.
A) $0 \mathrm{lb}<\mathbf{F}_{\mathrm{GH}}<5000 \mathrm{lb}(\mathrm{C})$
B) $5000 \mathrm{lb}<\mathbf{F}_{\mathrm{GH}}<10000 \mathrm{lb}$ (C)
C) $0 \mathrm{lb}<\mathrm{F}_{\mathrm{GH}}<5000 \mathrm{lb}(\mathrm{T})$
D) $5000 \mathrm{lb}<\mathbf{F}_{\mathrm{GH}}<10000 \mathrm{lb}(\mathrm{T})$
E) None of the above

8000 lb


## Definition of Work

## Work of a force

A force does work when it undergoes a displacement in the direction of the line of action.


The work $d U$ produced by the force $\boldsymbol{F}$ when it undergoes a differential displacement $d \boldsymbol{r}$ is given by

$$
d U=\mathbf{F} \cdot d \mathbf{r}
$$

Work of a couple $\quad d U=M \mathbf{k} \cdot d \theta \mathbf{k}=M d \theta$


## Virtual Displacements

A virtual displacement is a conceptually possible displacement or rotation of all or part of a system of particles. The movement is assumed to be possible, but actually does not exist. These "movements" are first order differential quantities:

## Virtual Work

The principle of virtual work states that if a body is in equilibrium, then the algebraic sum of the virtual work done by all the forces and couple moments acting on the body is zero for any virtual displacement of the body. Thus,


## Procedure for Analysis

- Thin rod of weight $W$
- Smooth wall and floor
- Determine P

1. Draw FBD of the entire system and provide coordinate system
2. Sketch the "deflected position" of the system
3. Define position coordinates measured from a fixed point and select the parallel line of action component and remove forces that do no do work
4. Differentiate position coordinates to obtain virtual displacement
5. Write the virtual work equation and express the virtual work of each force / couple moment
6. Factor out the comment virtual displacement term and solve



Determine the required force P needed to maintain equilibrium of the scissors linkage when the angle is 60 degrees. The spring is unstretched when the angle is 30 degrees.

The scissors jack supports a load $\mathbf{P}$. Determine the axial force in the screw necessary for equilibrium when the jack is in the position shown. Each of the four links has a length $L$ and is pin-connected at its center. Points $B$ and $D$ can move horizontally.


