## Announcements

- Morning Office Hours: Mon/Wed, 9-10am in MEB 220H
- Quiz 2 sign-ups are now open
- The scope of the exam will cover up to the end of today's lecture (Lecture 7)
- Same format as Quiz 1
$\square$ Upcoming deadlines:
- Thursday (9/14)
- ME HW5
- Tuesday (9/19)
- PL HW6
- Due next week
- Writing Assignment 1



## Recap

- Equilibrium of a particle in 2D and 3D
- Equilibrium of a system of particles
- Free body diagram
- Equation of equilibrium



## Chapter 4: Force System Resultants

## Goals and Objectives

- Discuss the concept of the moment of a force and show how to calculate it in two and three dimensions
- How to find the moment about a specified axis
- Define the moment of a couple
- Finding equivalence force and moment systems
- Reduction of distributed loading


## Applications



Carpenters often use a hammer in this way to pull a stubborn nail. Through what sort of action does the force $F_{H}$ at the handle pull the nail? How can you mathematically model the effect of force $F_{H}$ at point $O$ ?


Moment 1. a very brief period of time. An Exact point in time. 2. importance. 3. A turning Effect produced by a force acting at a distance on An object.

## Moment of a Force



Which force(s) have NO turning effect?

## Moment of a Force



1) Which force(s) yields a "tighty" effect?
2) Which force(s) yields a "loosey" effect?

## Moment of a force - scalar formulation

The moment of a force about a point provides a measure of the tendency for rotation (sometimes called a torque).

(a) Sense of rotation


## Example - Scalar Formulation

Determine the moment of this force about the point $A$ as a function of $\mathbf{F}$.


## Moment of a force - vector formulation

The moment of a force $\mathbf{F}$ about point $\mathbf{O}$, or actually about the moment axis passing through $O$ and perpendicular to the plane containing $\mathbf{O}$ and $\mathbf{F}$, can be expressed using the cross (vector) product, namely:


## Example - Vector Formulation



Given: The angle $\boldsymbol{\theta}=30^{\circ}$ and $x=10 \mathrm{~m}$.
Find: The moment by $\mathbf{P}$ about point O .

## Example - Vector Formulation <br> \section*{$z$}



Find: Moment of the force about point $B$.

## Moment about a Specific Axis

Remember, the component of a vector, $\mathbf{A}$, along the direction of another, $\mathbf{B}$, can be determined using the dot product:


