

9/8/2017

Announcements

- Quiz 1 Next Week!!! (How's your MATLAB skills?)
 - Practice quiz available on PL

□ Upcoming deadlines:

- Friday (9/8 – TODAY!)
 - Quiz 1 Sign-up
- Tuesday (9/12)
 - PL HW4
- Thursday (9/14)
 - ME HW5

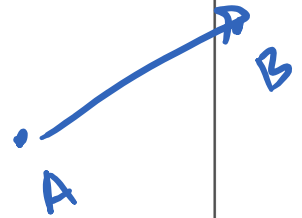


Ant-eater

Recap

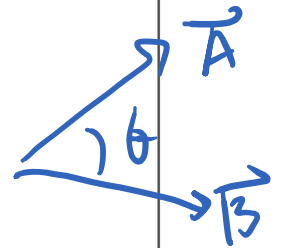
- Position vectors

$$\vec{r}_{AB} = \vec{r}_B - \vec{r}_A$$



- Dot (scalar) product

$$\vec{A} \cdot \vec{B} = c = |\vec{A}| |\vec{B}| \cos \theta = \sum_{i=x,y,z} A_i B_i$$



- Cross (vector) product

$$\vec{A} \times \vec{B} = \vec{C}$$

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Chapter 3: Equilibrium of a particle

Goals and Objectives

- Practice following general procedure for analysis.
- Introduce the concept of a free-body diagram for an object modeled as a particle.
- Solve particle equilibrium problems using the equations of equilibrium.

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Applications

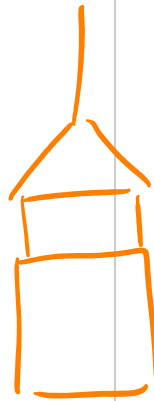
For a spool of given weight, how would you find the forces in cables AB and AC?

If designing a spreader bar (BC) like this one, you need to know the forces to make sure the rigging (A) doesn't fail.



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L5 - Force along a line Cross product



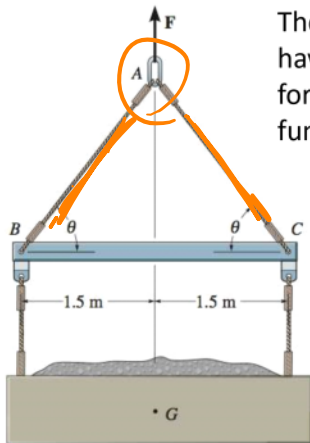
model

General procedure for analysis

1. Read the problem carefully; write it down carefully.
2. MODEL THE PROBLEM: Draw given diagrams neatly and construct additional figures as necessary.
3. Apply principles needed.
4. Solve problem symbolically. Make sure equations are dimensionally homogeneous
5. Substitute numbers. Provide proper units *throughout*. Check significant figures. Box the final answer(s).
6. See if answer is reasonable.

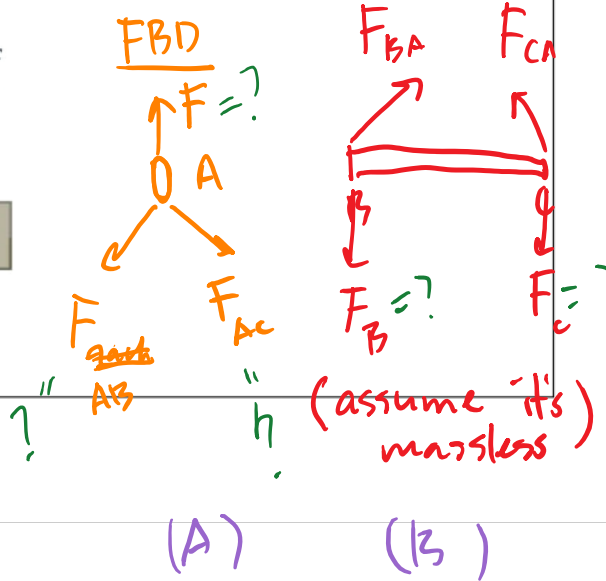
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Free body diagram



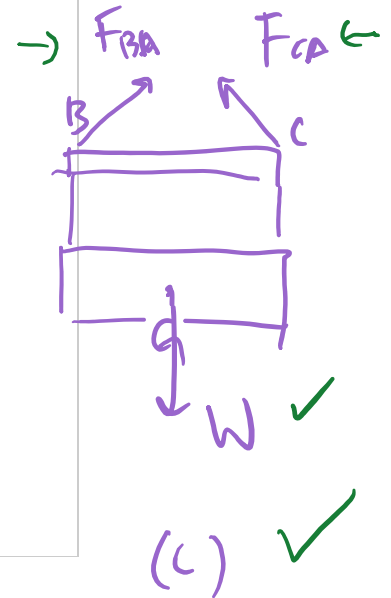
The lift sling is used to hoist a container having a mass of 500 kg. Determine the force in each of the cables AB and AC as a function of θ .

9 L5 - Force along a line Cross product



Given: $m \Rightarrow W = mg$

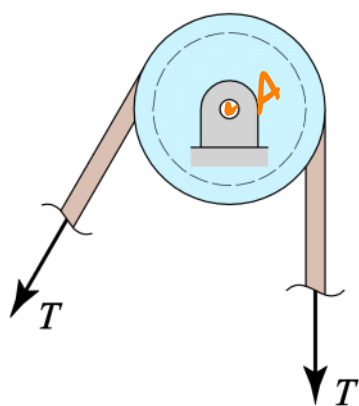
Find: F_{AB}, F_{AC}



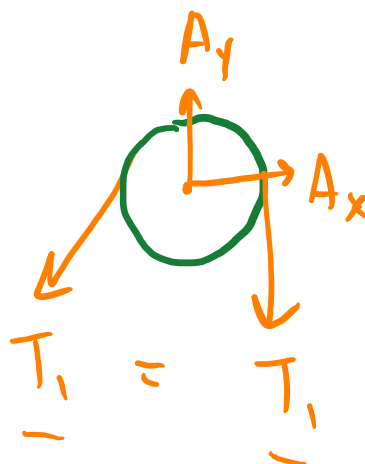
Idealizations

— massless

Pulleys are (usually) regarded as frictionless; then the tension in a rope or cord around the pulley is the same on either side.



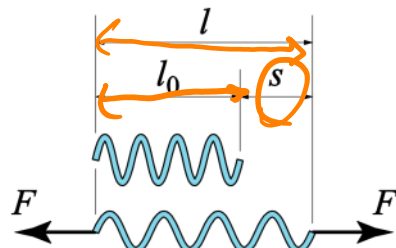
Frictionless pulley



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Idealizations

Springs are (usually) regarded as linearly elastic; then the tension is proportional to the *change* in length s .



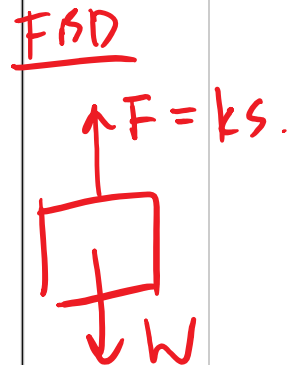
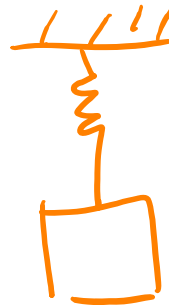
$$F = k s = k(l - l_0)$$

Linearly elastic spring

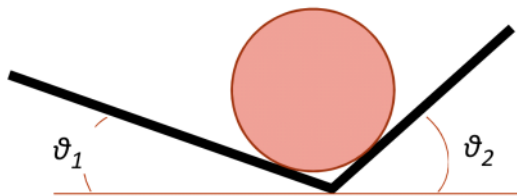
constant or

$$\left[\frac{N}{m} \right] \left[\frac{lb}{ft} \right]$$

$$[N] = [?] [m]$$

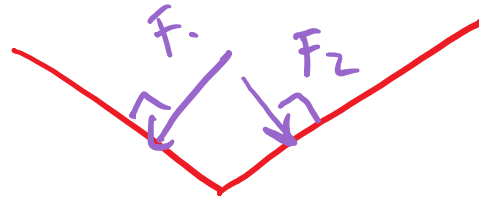
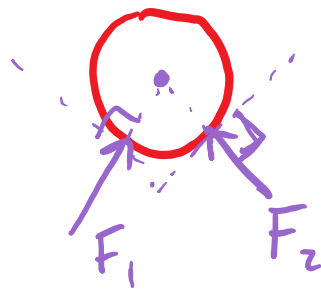


Idealizations



Contact force in smooth surface:

(no friction)



12 LS - Force along a line Cross product

Equilibrium of a particle

According to Newton's first law of motion, a particle will be in **equilibrium** (that is, it will remain at rest or continue to move with constant velocity) if and only if

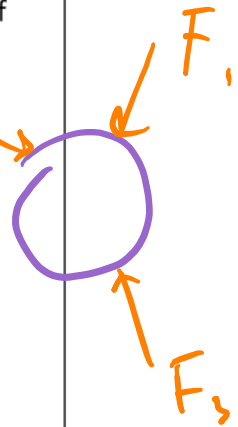
$$m\vec{a} = 0 \quad \sum \vec{F} = 0 = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots + \vec{F}_n = 0$$

In three dimensions, equilibrium requires:

$$\sum F_x = 0 \quad \sum F_y = 0 \quad \sum F_z = 0.$$

Coplanar forces: if all forces are acting in a single plane, such as the "xy" plane, then the equilibrium condition becomes

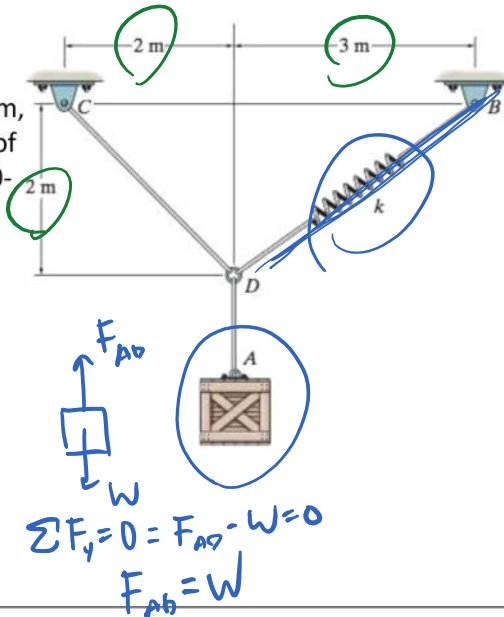
$$\sum F_x = 0 \quad \sum F_y = 0$$



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Example

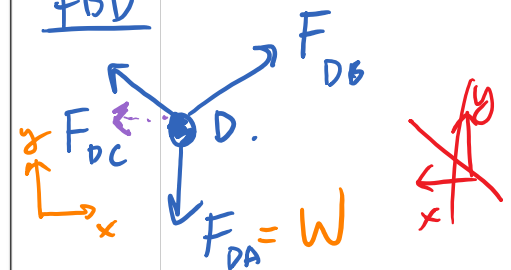
If the spring DB has an unstretched length of 2 m, determine the stiffness of the spring to hold the 40-kg crate in the position shown.



Given: $l_0, m, \hat{u}_{DC}, \hat{u}_{DB}$

Find: k

FBD



EoE

$$\sum F_y = 0 = F_{DB}y + F_{DC}y - W$$

$$= F_{DB} \left(\frac{2}{\sqrt{3^2+2^2}} \right) + F_{DC} \left(\frac{2}{\sqrt{2^2+2^2}} \right) - W$$

$$= k s \left(\frac{2}{\sqrt{13}} \right) + F_{DC} \left(\frac{2}{2\sqrt{2}} \right) - W$$

$$0 = k s \left(\frac{2+3}{\sqrt{13}} \right) - W$$

$$k = \frac{W}{s \left(\frac{5}{\sqrt{13}} \right)}$$

$$W = mg = (40 \text{ kg}) \left(9.81 \frac{\text{m}}{\text{s}^2} \right)$$

$$s = \sqrt{13} \text{ m} - 2 \text{ m}$$

$$s = (l - l_0)$$

$$\sum F_x = 0 = F_{DB}x + F_{DC}x$$

$$= F_{DB} \left(\frac{3}{\sqrt{3^2+2^2}} \right) - F_{DC} \left(\frac{2}{\sqrt{2^2+2^2}} \right)$$

$$0 = k s \left(\frac{3}{\sqrt{3^2+2^2}} \right) - F_{DC} \left(\frac{2}{\sqrt{2^2+2^2}} \right)$$

$$\Rightarrow F_{DC} = \frac{k s \left(\frac{3}{\sqrt{3^2+2^2}} \right)}{\left(\frac{2}{2\sqrt{2}} \right)}$$