

# Today's Announcements

1. Test given back next Wednesday
2. HW assigned next Wednesday.
3. Next Monday—1<sup>st</sup> discussion about Individual Projects.

## Today's take-home lessons

(i.e. what you should be able to answer at end of lecture)

1. Seeing things with Light and Electron Microscopes
2. Accuracy and Resolution—how fine can you see.
3. Fluorescence. What is it (amplitude, time-scale)?

# Today

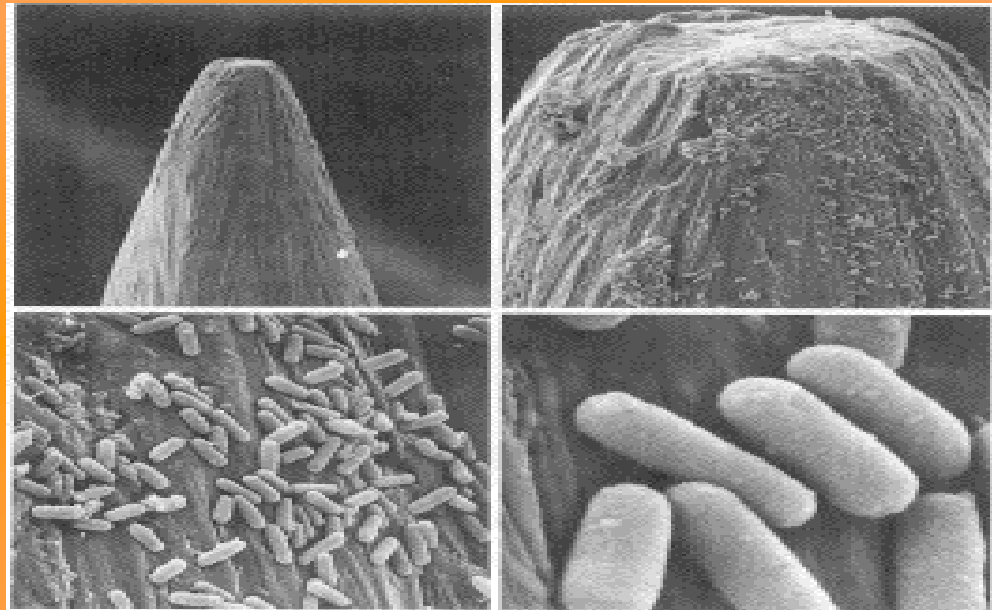
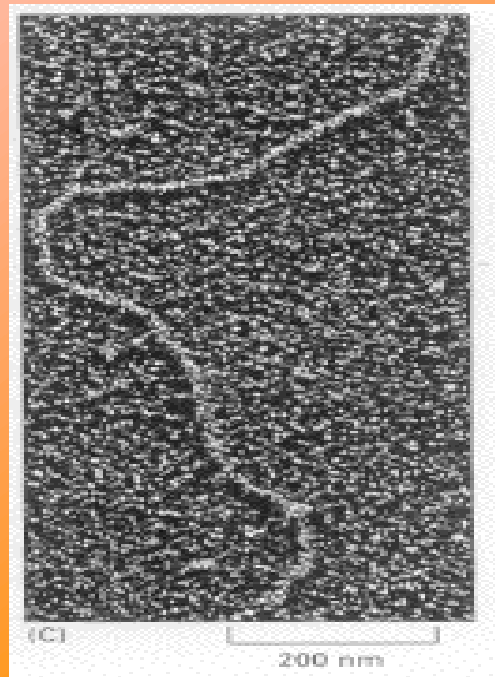
## Techniques for measuring distances

(where physicists have made a big impact on bio.)

X-ray *diffraction* (atomic resolution)

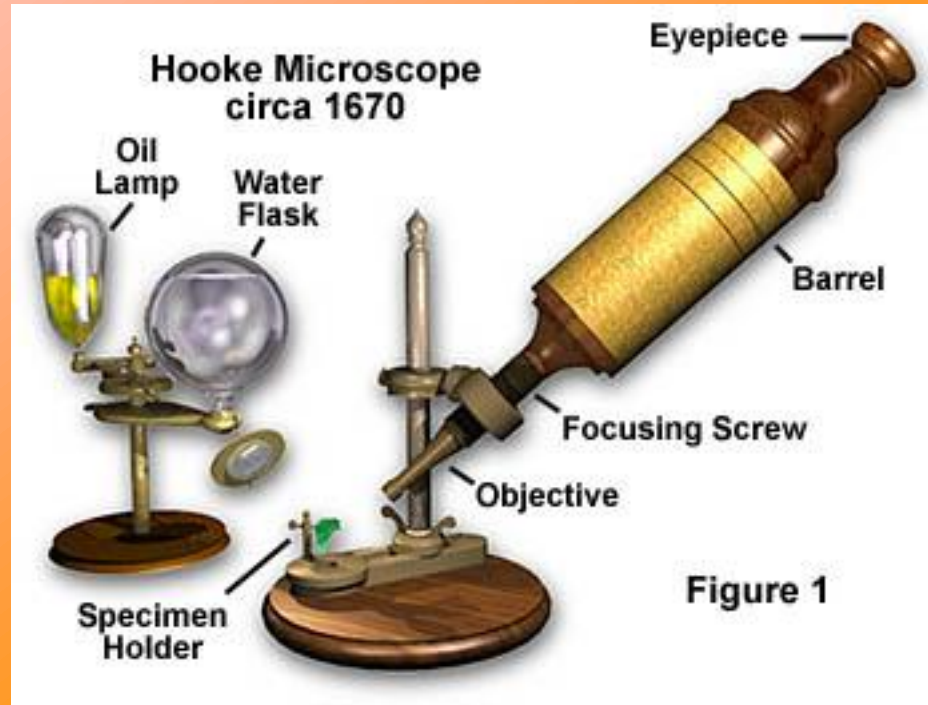
Electron (*Imaging*) Microscopy (nm-scale)

Visible (*Imaging*) Microscopy (nm -  $\mu\text{m}$ )



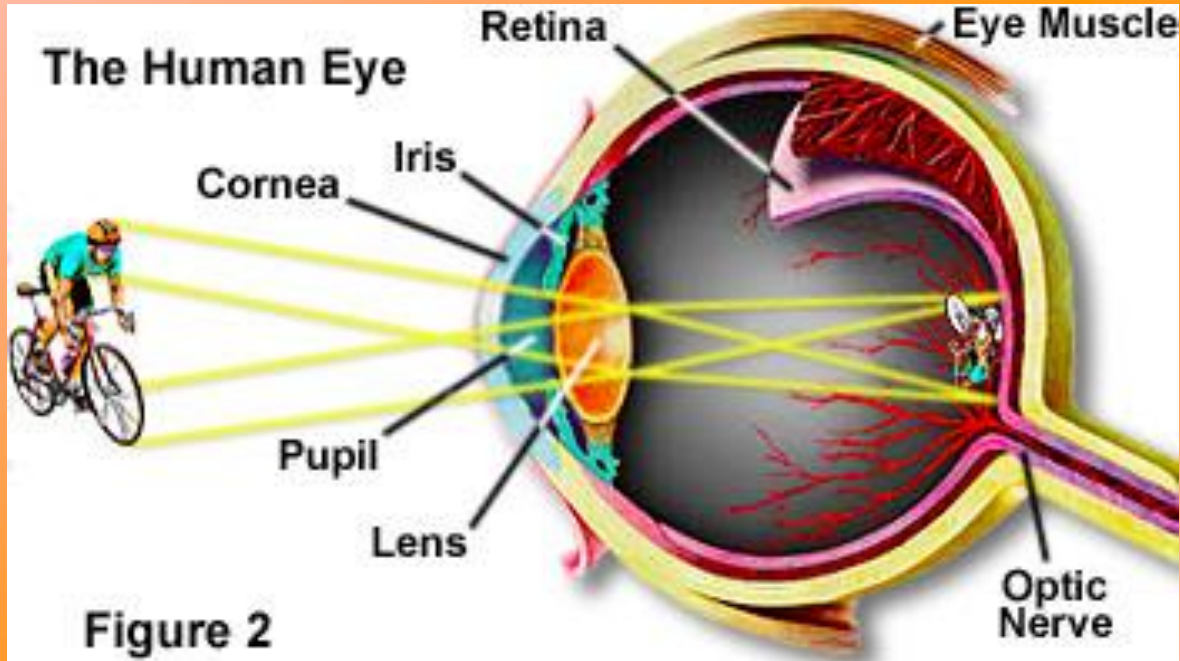
Bacteria on head of a pin  
at different magnifications

# Beginning of microscopes



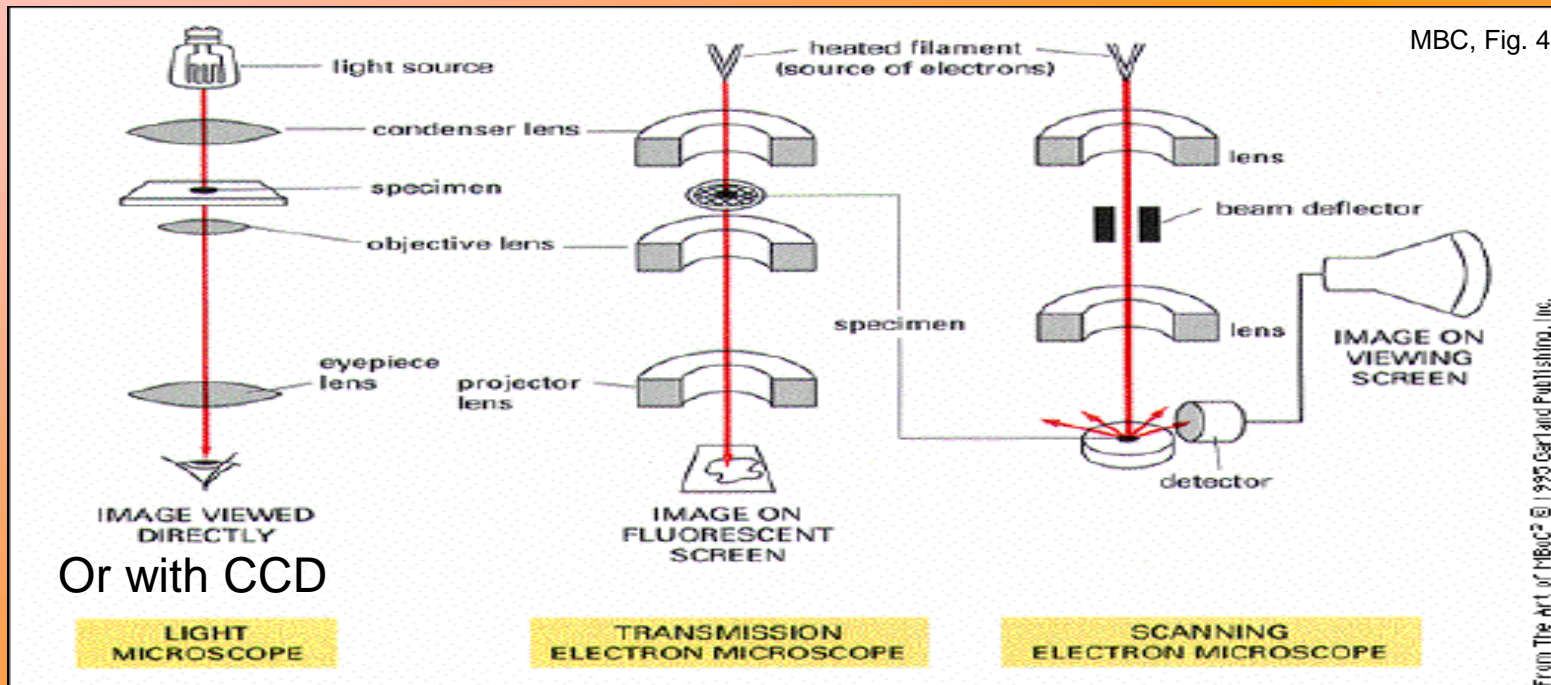
Microscope must produce a magnified image of the specimen, separate the details in the image, and render the details visible to the human eye or camera.

# Your eye is a Microscope!



# Microscopes

Cells discovered with invention of microscope.



Or with CCD

**LIGHT MICROSCOPE**

**TRANSMISSION ELECTRON MICROSCOPE**

**SCANNING ELECTRON MICROSCOPE**

1000x, 0.2um

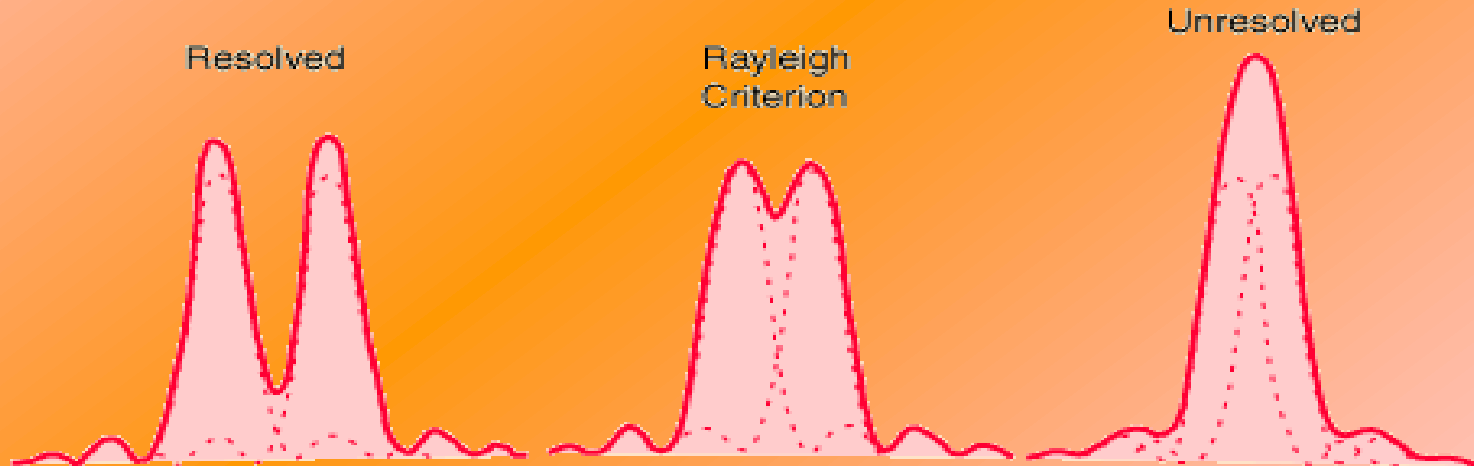
10<sup>6</sup>x, 2 nm

20,000, 10 nm (3-d)



# Resolution: The Rayleigh criteria

How well can you resolve two point objects?



A single light-emitting spot will be smeared out, no matter how small the spot is, because of the wavelength of light to  $\sim \lambda/2$ .

Point-Spread Function (PSF)



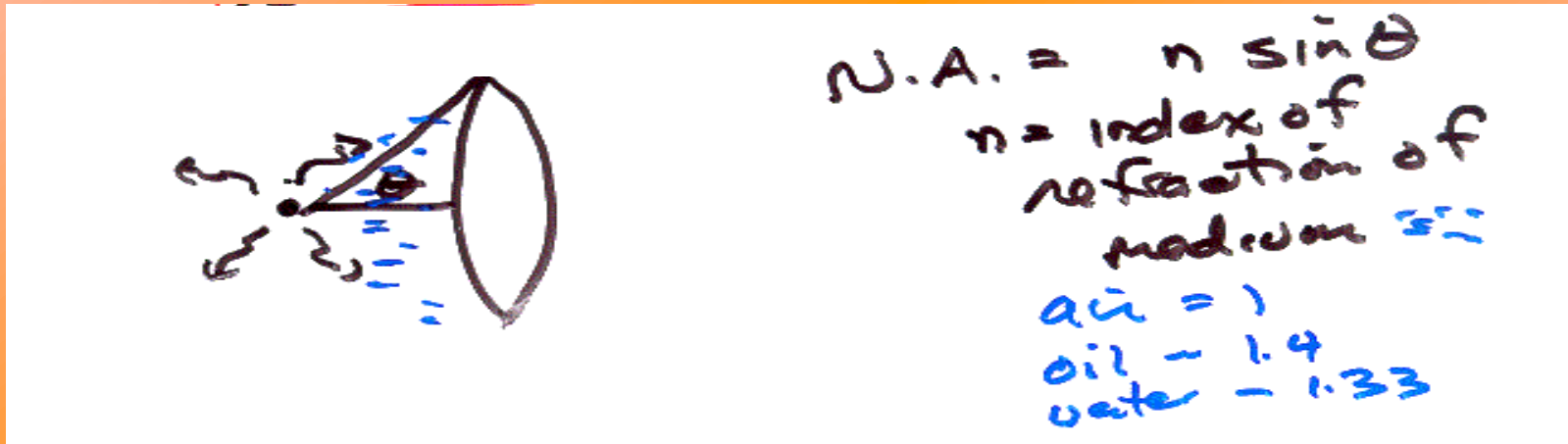
# What determines (ultimate, i.e. best) resolution of technique... microscope, eye, etc.?

[2 parts]

1. Primarily  $\lambda$  (wavelength).

Why? Uncertainty principle (Will show).

2. Collection Angle/focal length/ Numerical Aperture



Resolution  $\approx$  #  $\lambda$  N.A.

# = a factor =  $\frac{1}{2}$  (details not important)

**Resolution  $\approx \lambda/[2N.A.]$**

# Why is resolution $\lambda/2$ N.A. (N.A. = $n \sin \theta$ )

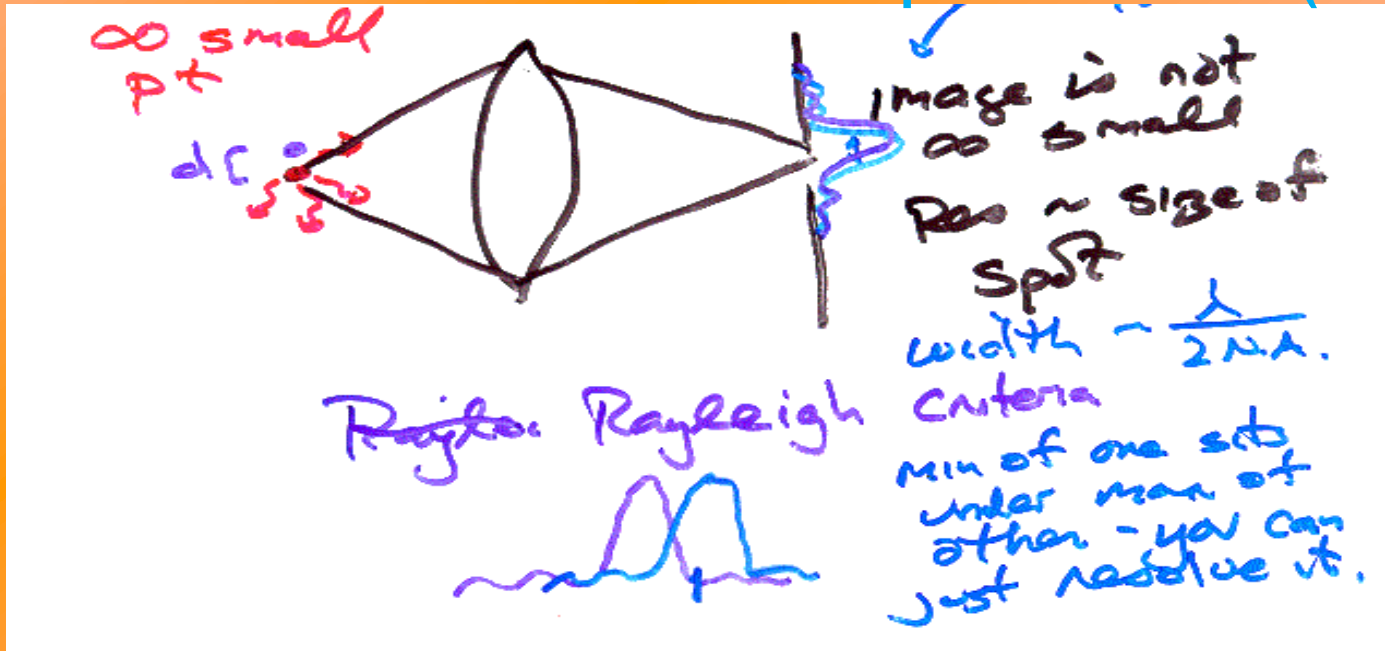
## Resolution:

- 1) how small of a spot of excitation light can you make (scanning microscope)



- 2) how big of a spot an infinitely small object makes

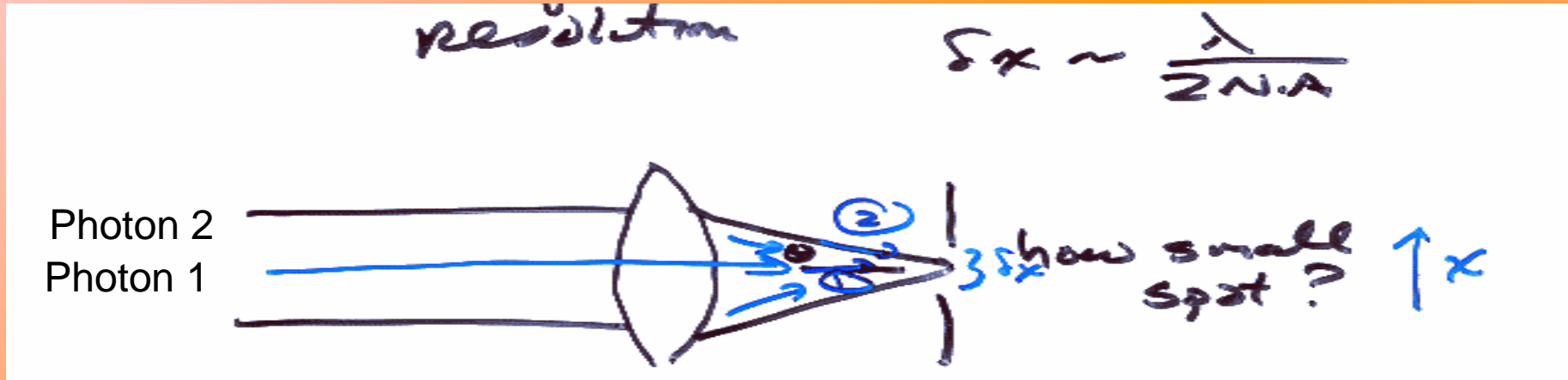
### Point Spread Function (PSF)





# Calculating optimal diffraction-limited resolution.

What is uncertainty principle applied here?



Photon 1:  $p = p \hat{y}$

Photon 2:  $p_x = p \sin \theta$  :  $p_y = p \cos \theta$

$$\begin{aligned} \Delta p_x &= p \sin \theta - (-p \sin \theta) \\ &= 2p \sin \theta \end{aligned}$$

# Calculating resolution (con' t)

$$\Delta p \Delta x = h/2\pi$$

$$2p \sin \theta \Delta x = h/2\pi$$

$$p = h/\lambda$$

$$\left( \frac{2 h \sin \theta}{\lambda} \right) (\Delta x) \sim \frac{h}{2\pi} = \frac{h}{2\pi}$$

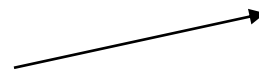
resolution:  $\Delta x$

$$\frac{\lambda}{4\pi \sin \theta}$$

within a factor

$$\frac{\lambda}{\sin \theta}$$

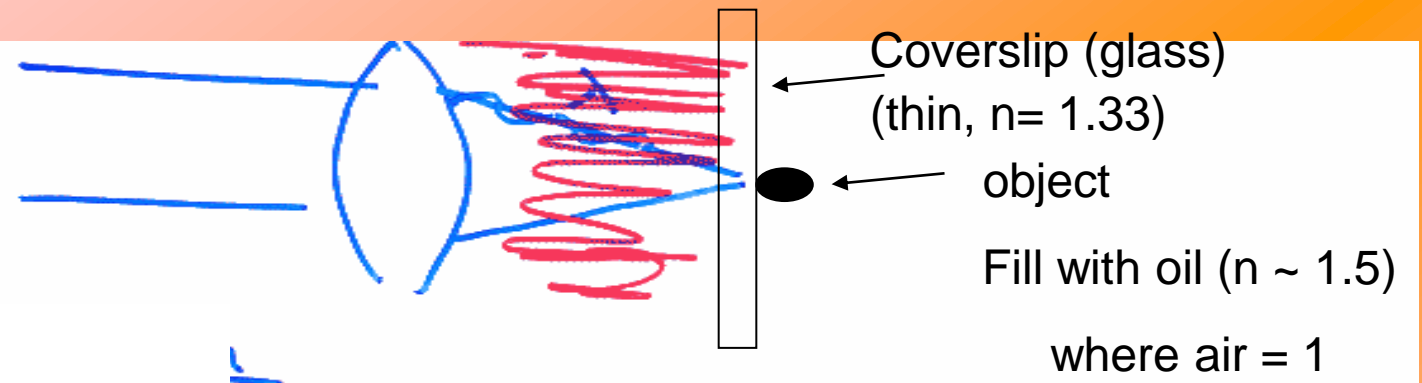
Wavelength at screen



... need n.

Where does n come in?

# Calculating resolution (con't) : "n", index of refraction



$v = \lambda f$  for any wave

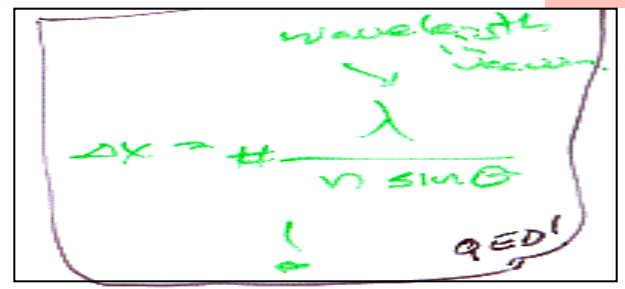
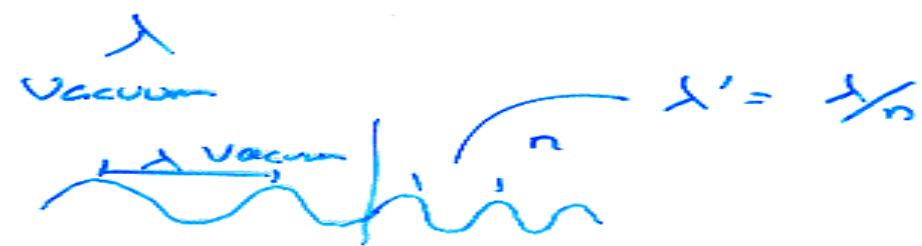
$n = \text{index of refraction} = \frac{c}{v}$

$c \rightarrow$  speed of light in vac.  
 $v \rightarrow$  speed of light in medium of index  $n$

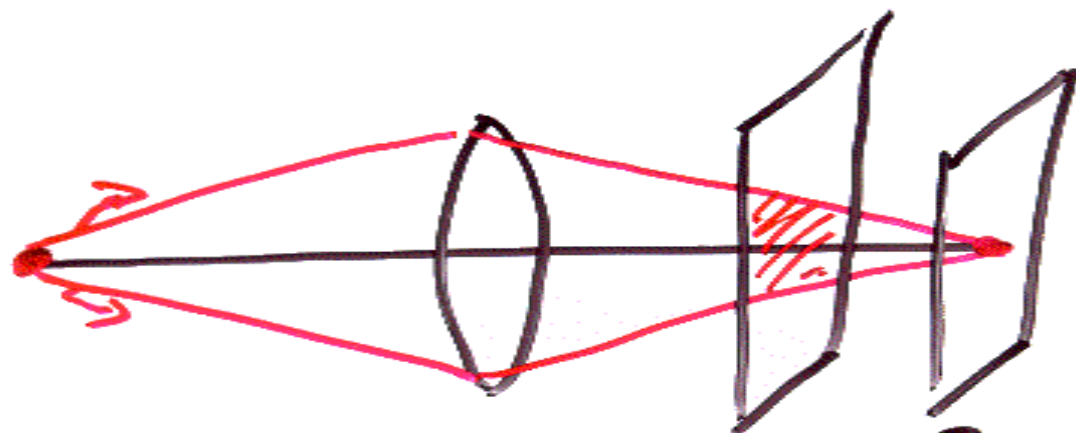
slowed light down  
if speed  $\rightarrow$  speed

either  $\lambda$  gets smaller or  $f$  gets smaller  
which one?  $\rightarrow$  ans.  $\lambda \rightarrow \frac{\lambda}{n}$

(Homework)



Sidelight: what does it mean for something to be in focus?



Smear  
out of  
focus

pt.



out of  
focus

focus

pt on screen has light  
from many obj. pt.  
parts of object  
Each pt on  
object  
gets  
imaged  
to one just  
in image  
plane

Bottom line:

$$\text{Resolution} \approx \lambda/[2\text{NA}]$$

$$\text{NA} \approx 1 \quad \lambda \approx 500 \text{ nm (green)}$$

(for visible light)

$$\text{Resolution} \approx 250 \text{ nm}$$

# Wavelength & Resolution

$\lambda_{\text{visible}} \approx 400\text{-}700 \text{ nm}$

$\lambda/2 \text{ N.A.}: \text{air} = \lambda/2: \text{oil} = \lambda/(2)(1.4)$

$\lambda = 500 \text{ nm}$ : Best resolution 200-250 nm

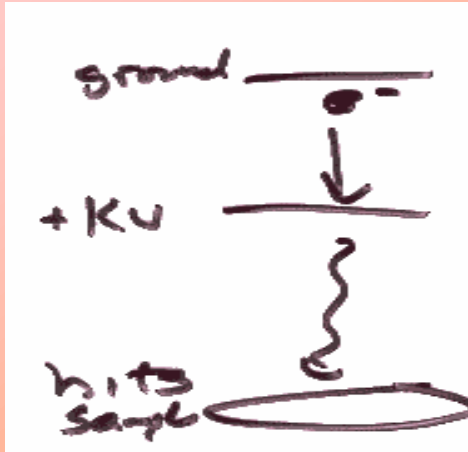


Visible Light "White Light"	
Wavelength in nanometer (nm)	
400 - 450	violet
450 - 500	blue
500 - 570	green
570 - 590	yellow
590 - 610	orange
610 - 750	red

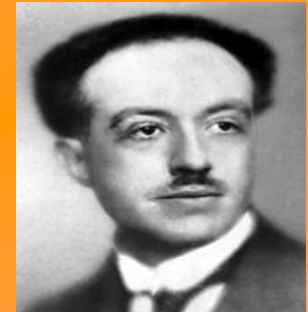
Modern day optical microscopes are highly optimized— perfect diffraction limited.  
(Electron microscopes are 1000' s of times worse.)



# $\lambda$ of electrons



(Who was famous guy who got Nobel prize in 1929 for the “wave nature of electrons”?)



DeBroglie

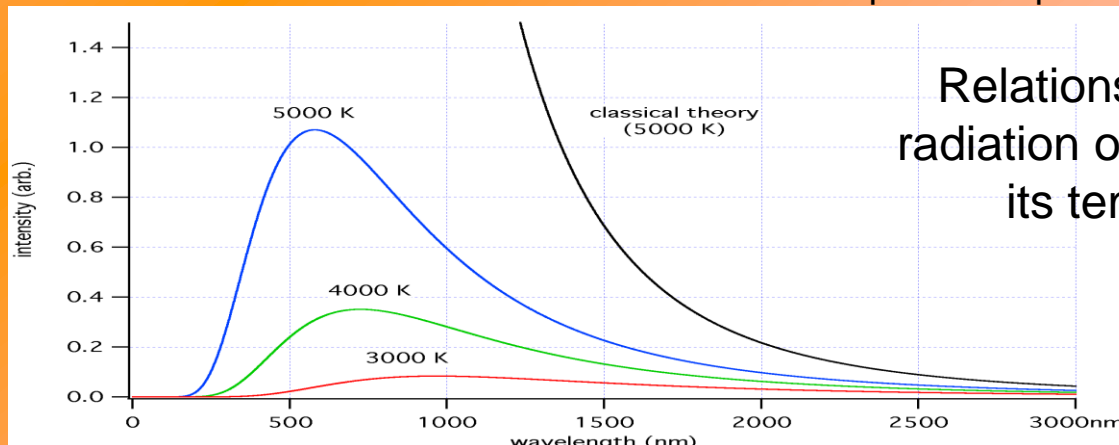
What relationship between wavelength,  $\lambda$ , and energy,  $E$ , and momentum,  $p$ , does this correspond to?

$$E = h\nu = hc/\lambda; \quad p = h/\lambda$$

Where does Planck’s constant come from?

The Planck constant came from law of black body radiation: that the electromagnetic radiation emitted by a black body could be modeled as a set of harmonic oscillators with **quantized** energy of the form:  $E = h\nu$

<http://en.wikipedia.org/wiki/Black-body>



Relationship between radiation of an object and its temperature

# Resolution of Electron Microscope

Given electron 100 KeV,  
(typical upper-value for electron microscope)  
what is  $\lambda$ ?

$$(h = 6.63 \times 10^{-34} \text{ J-sec} = 4.1 \times 10^{-15} \text{ eV-sec})$$

$$E_{100\text{kV}} = 0.004 \text{ nm (really short!)}$$

In reality, because not perfect electron lenses, resolution is  $\sim 1$  nm.

**E.M. are far from ideal.**

# Noise

Why can't you see starlight in the day?

(The stars are just as bright during the day as at night.)

You have a “bright” background (sun)...  
which has a lot of noise.

If you have  $N$  photons, then you have  $\sqrt{N}$  noise.

(This is important to remember!)

Example: Sun puts out a  $10^6$  photons/sec. Noise =  $10^3$  photons/sec

Therefore: if star puts out  $10^3$  photons/sec,  
can just barely “see it” with Signal/Noise = 1

(Really want to “see it” with S/N of at least a few >2-5))

# Example of Noise con't

Let's say star puts out 100 photon/sec.  
(It turns out you (your eye) can see about 1 photon!!)


S/N day?

At night?

Fluorescence vs standard light Microscopy

# Biophysics 101

## Essentials of fluorescence



Basic Fluorescence  
Single molecule detection methods  
(confocal, two-photon, TIRF)  
Imaging (FIONA, etc...)

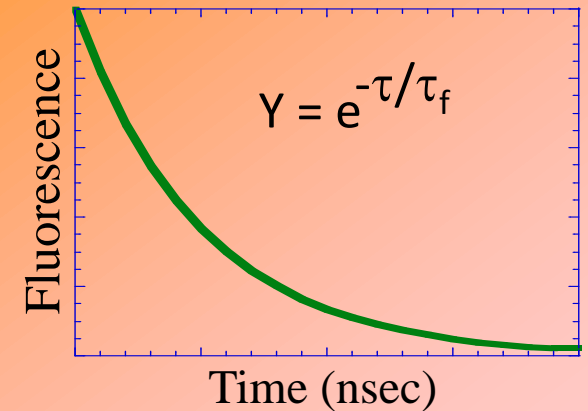
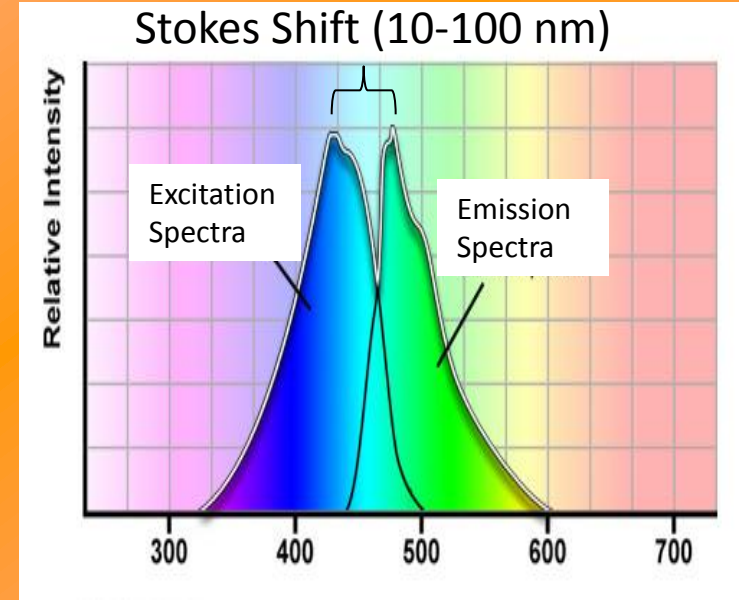
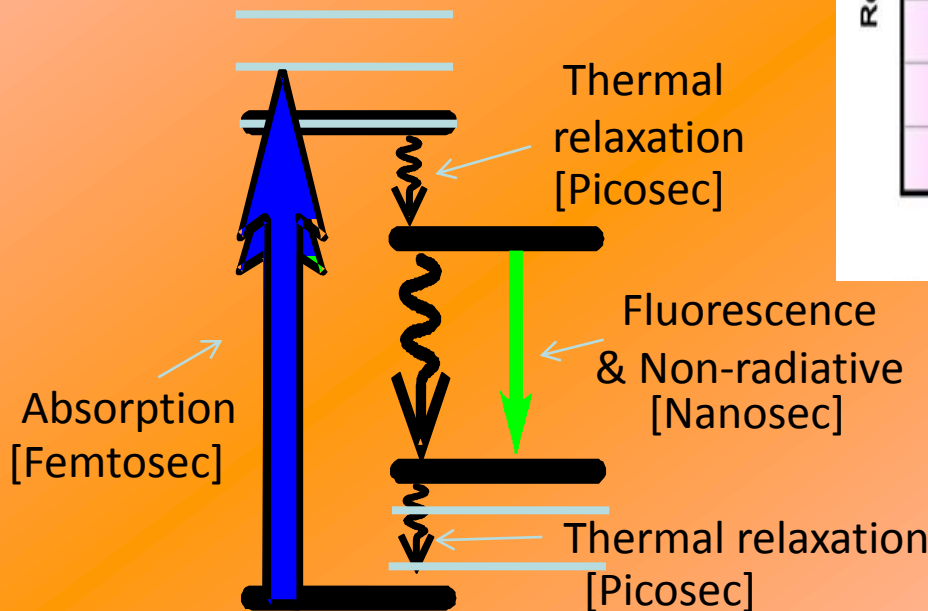
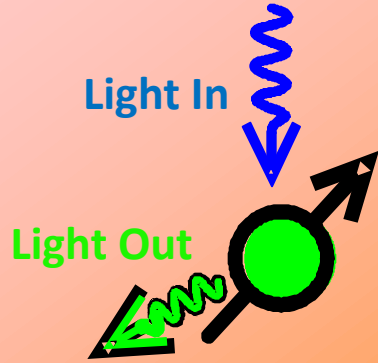
**(Later)**



FRET  
(Polarization, FCS)

# Basics of fluorescence

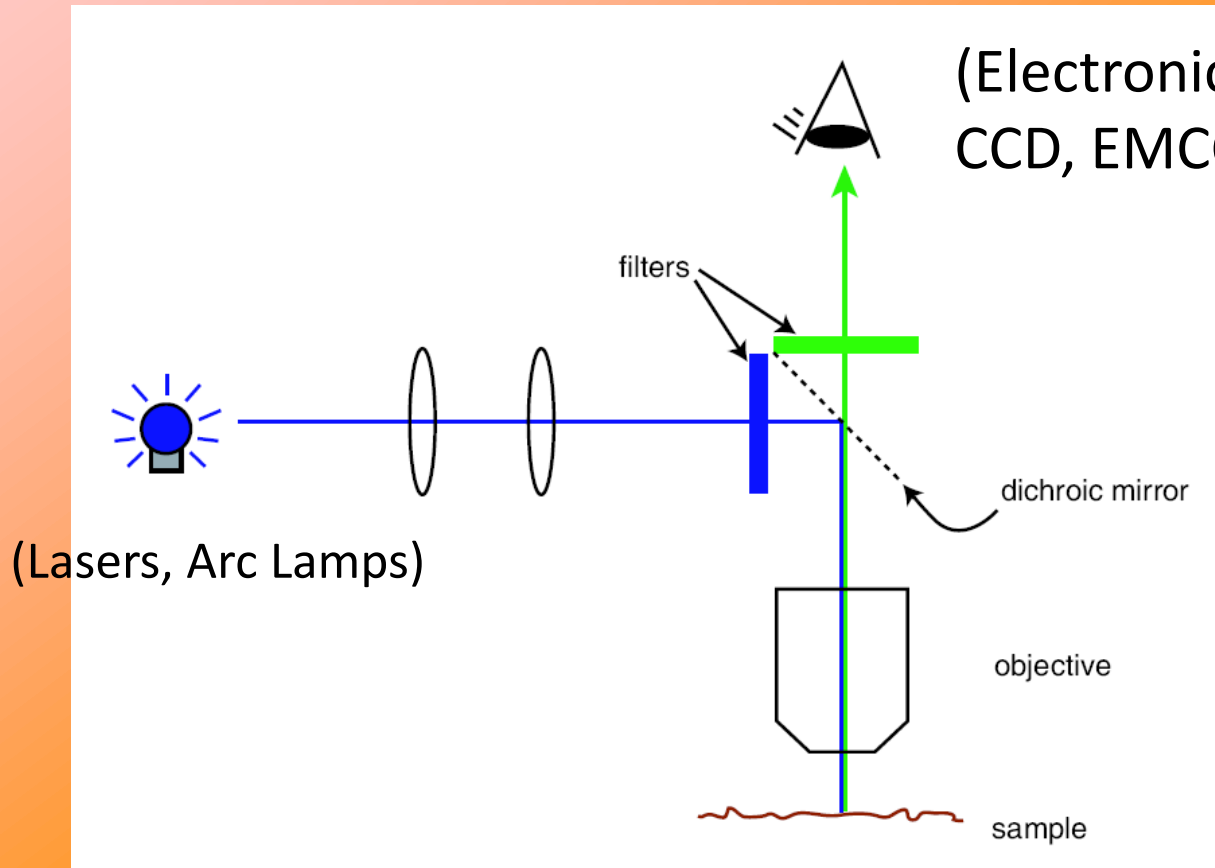
Shine light in, gets absorbed, reemits at longer wavelength



Photobleaching Important: Dye emits  $10^5 \rightarrow 10^7$  photons, then dies!

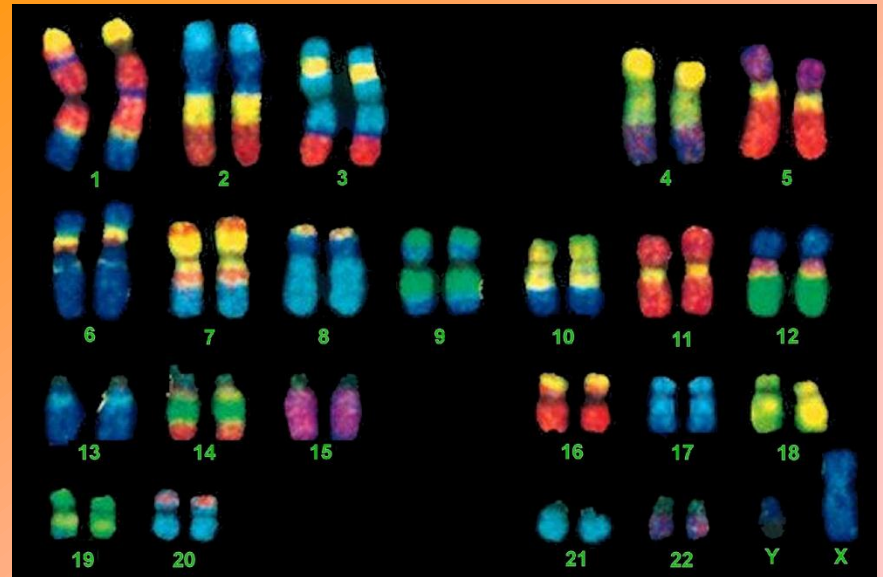
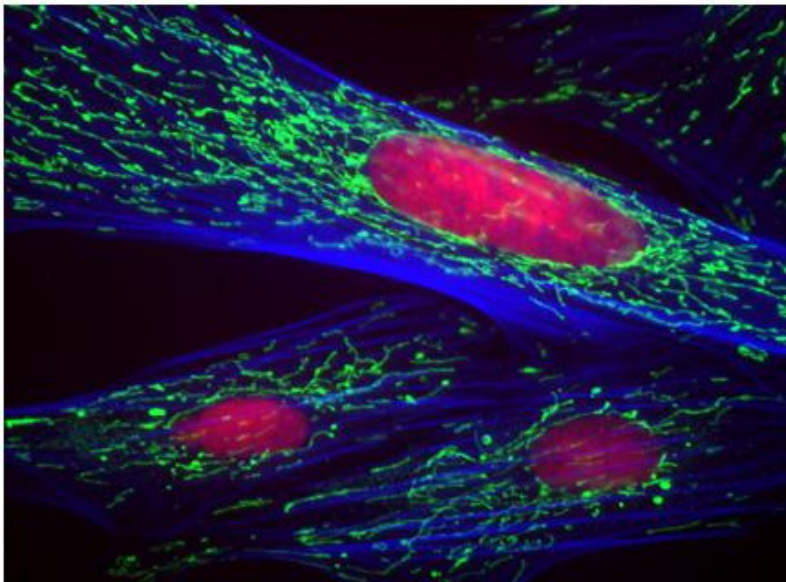
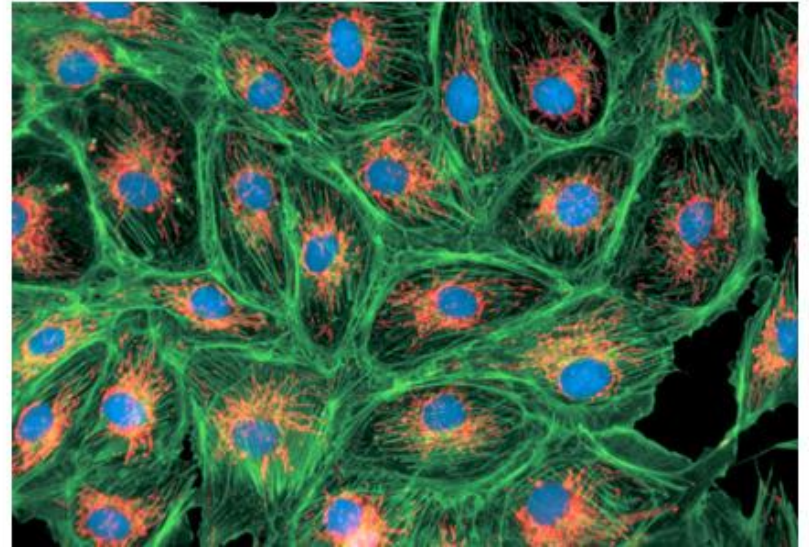
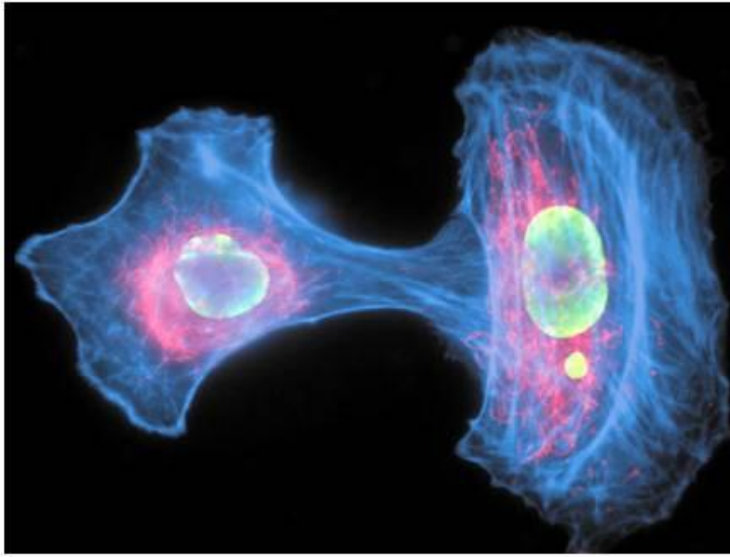


# Basic Set-up of Fluorescence Microscope



Nikon, Zeiss, Olympus, Leica—Microscope Manufacturer  
Andor, Hamamatsu, Princeton Instruments, other...make EMCCDs

# You can get beautiful pictures



# Fluorescence vs. standard light Microscopy

Which is more sensitive?

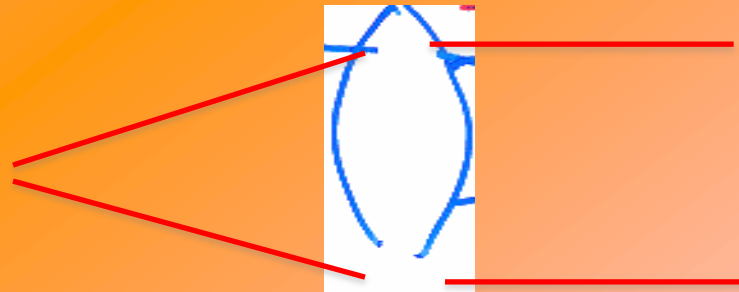
Answer: Fluorescence...no background!

# Wide-field and Point illumination

Point illumination: Come into objective with parallel illumination.



Widefield illumination: want to have parallel light hitting sample. Shine light at back-focal plane.



Back focal length

# Class evaluation

1. What was the most interesting thing you learned in class today?
2. What are you confused about?
3. Related to today's subject, what would you like to know more about?
4. Any helpful comments.

Answer, and turn in at the end of class.