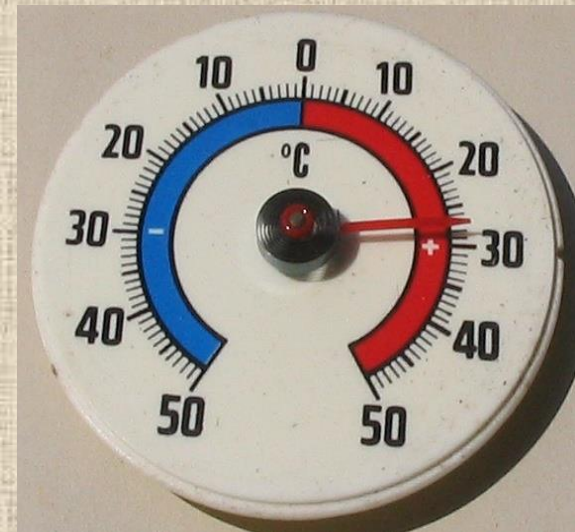


# Temperature. Sensors. Measuring technique.

*Eugene V. Colla*



# Outline

**Temperature Sensors**

**Measuring equipment and ideas**

**Sensor calibration**

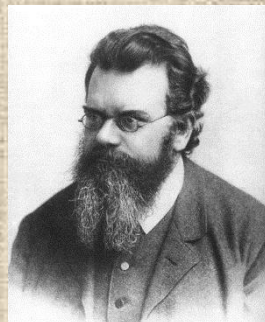
**Temperature scales**

# Notcontacting devices:

# Pyrometers



Jožef Stefan  
(1835-1893)



Ludwig Eduard Boltzmann  
(1844-1906)

## Stefan-Boltzmann law

$$P = e\sigma AT^4$$

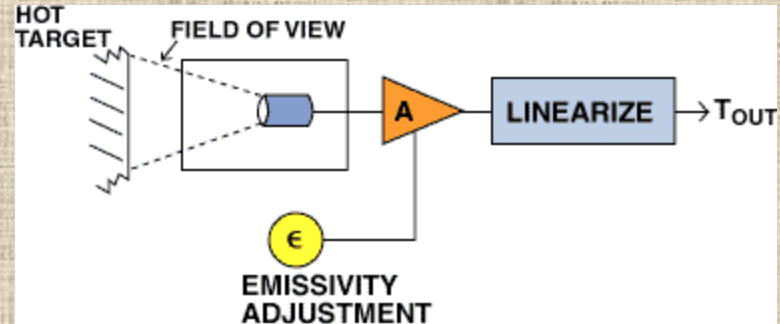
**e** – emissivity;

**$\sigma$**  - Stefan-Boltzmann constant

( $\sigma = 5.67 \times 10^{-8} \text{ Wm}^{-2}\text{K}^{-4}$ )

**A** - surface area

**T** - temperature



**OS643**



Range C°  
0÷260



Range C°  
-50÷1000



Range C°  
-40÷500

**Extech  
42580**

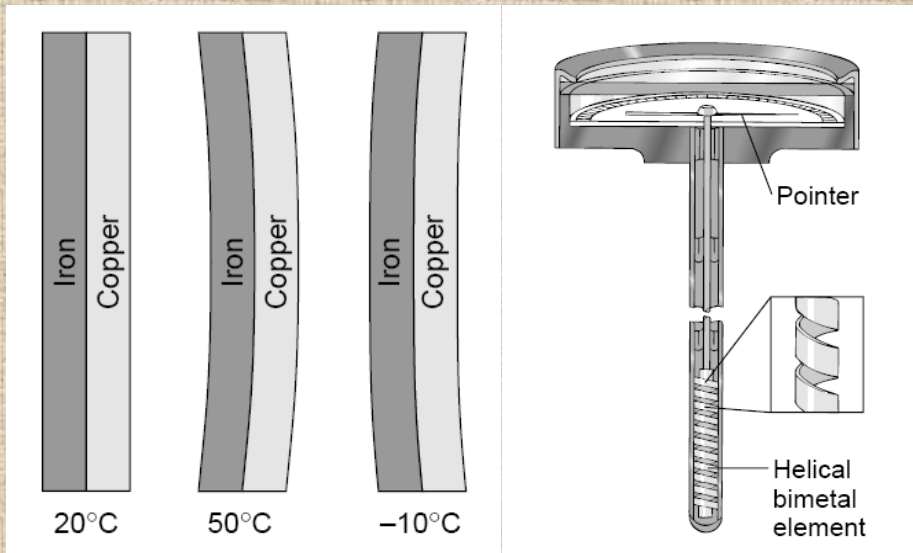


# Contacting devices: Bi-Metal Thermometers

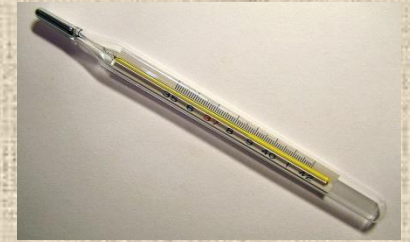


Typical temperature range  
 $-10^{\circ}\text{C} \div 200^{\circ}\text{C}$

- Very cheap
- No electronics
- Easy to use
- Moderate precision ( $\pm 1\%$  from full scale)

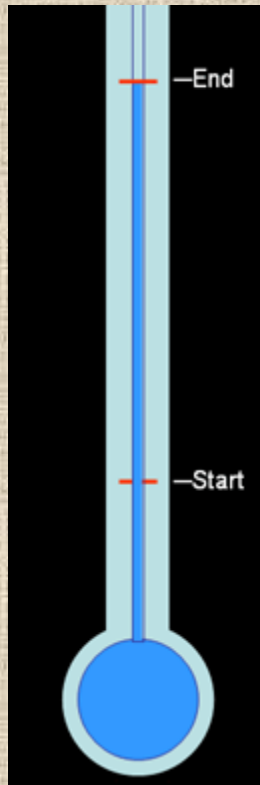


# Contacting devices: Volume Expansion Thermometer



$$\Delta V = V \beta \Delta T$$

$\beta$  –coefficient of volume expansion



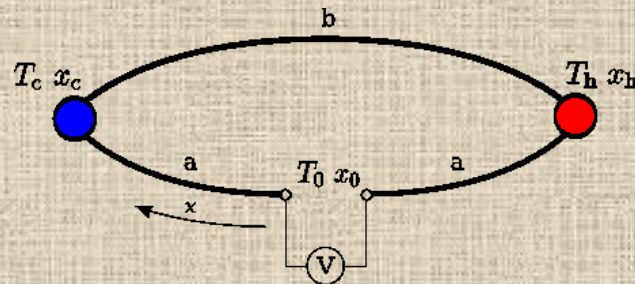
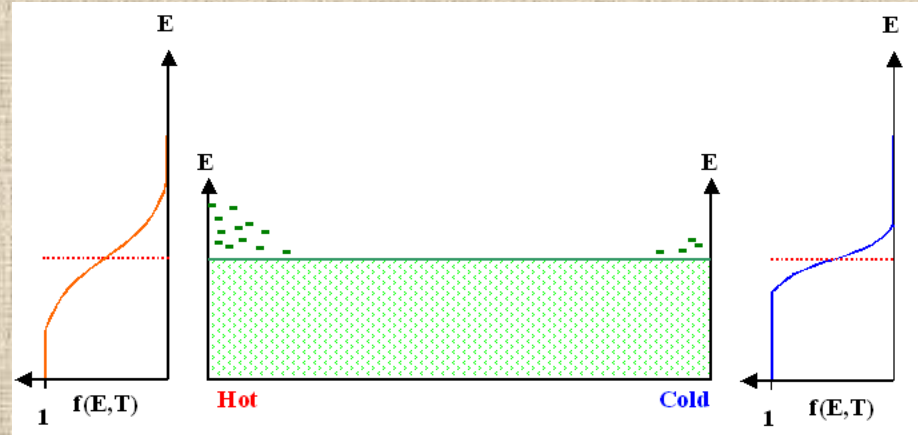
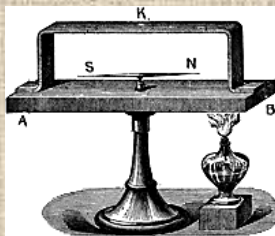
Average Expansion Coefficients for Some Materials Near Room Temperature

Material	Average Coefficient of Linear Expansion ( $\alpha$ ) ( $^{\circ}\text{C}^{-1}$ )	Material	Average Coefficient of Volume Expansion ( $\beta$ ) ( $^{\circ}\text{C}^{-1}$ )
Aluminum	$24 \times 10^{-6}$	Acetone	$1.5 \times 10^{-4}$
Brass and bronze	$19 \times 10^{-6}$	Alcohol, ethyl	$1.12 \times 10^{-4}$
Copper	$17 \times 10^{-6}$	Benzene	$1.24 \times 10^{-4}$
Glass (ordinary)	$9 \times 10^{-6}$	Gasoline	$9.6 \times 10^{-4}$
Glass (Pyrex)	$3.2 \times 10^{-6}$	Glycerin	$4.85 \times 10^{-4}$
Lead	$29 \times 10^{-6}$	Mercury	$1.82 \times 10^{-4}$
Steel	$11 \times 10^{-6}$	Turpentine	$9.0 \times 10^{-4}$
Invar (Ni-Fe alloy)	$0.9 \times 10^{-6}$	Air <sup>a</sup> at 0°C	$3.67 \times 10^{-3}$
Concrete	$12 \times 10^{-6}$	Helium <sup>a</sup>	$3.665 \times 10^{-3}$

# Contacting devices: Seebeck Effect. Thermocouples



**Thomas Johann Seebeck**  
(1770-1831)



$$S = \frac{dU}{dT}$$

$$U_S = \int_{T_0}^{T_c} S_A dT + \int_{T_c}^{T_H} S_B dT + \int_{T_H}^{T_0} S_A dT = \int_{T_c}^{T_H} (S_B - S_A) dT$$

**S -Seebeck coefficient**



# Contacting devices: Seebeck Effect. Thermocouples

## Seebeck coefficients

Material	Seebeck Coeff. *	Material	Seebeck Coeff. *	Material	Seebeck Coeff. *
Aluminum	3.5	Gold	6.5	Rhodium	6.0
Antimony	47	Iron	19	Selenium	900
Bismuth	-72	Lead	4.0	Silicon	440
Cadmium	7.5	Mercury	0.60	Silver	6.5
Carbon	3.0	Nichrome	25	Sodium	-2.0
Constantan	-35	Nickel	-15	Tantalum	4.5
Copper	6.5	Platinum	0	Tellurium	500
Germanium	300	Potassium	-9.0	Tungsten	7.5

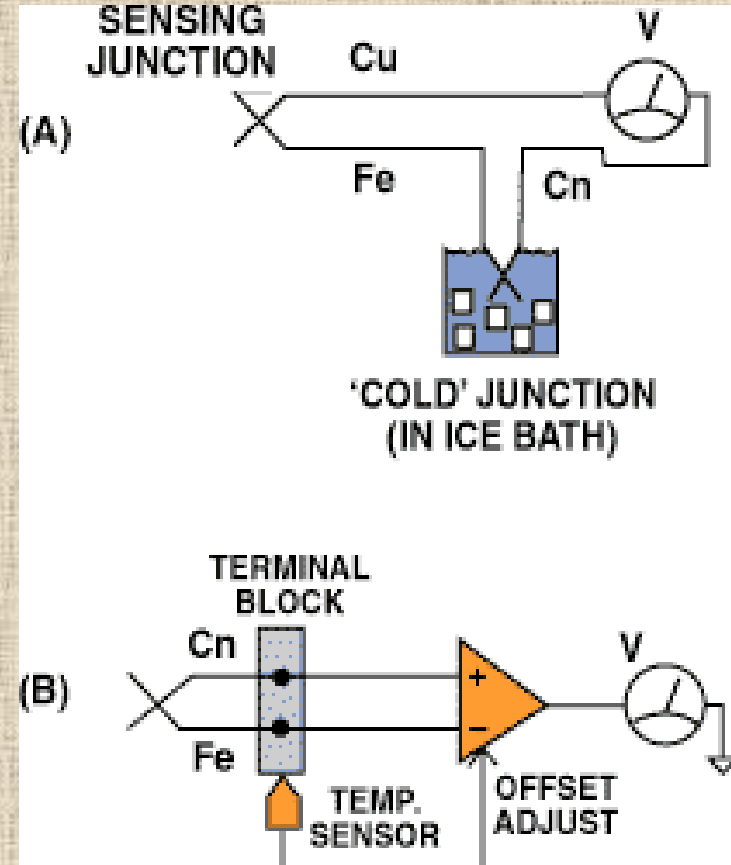
\*: Units are  $\mu\text{V}/^\circ\text{C}$ ; all data provided at a temperature of  $0^\circ\text{C}$

Type T (copper-constantan) has thermoemf at  $0^\circ\text{C}$   $41.5\mu\text{V}/^\circ\text{C}$ ;

# Contacting devices:

Thermocouple Type	Names of Materials	Useful Application Range
<b>B</b>	Platinum 30% Rhodium (+) Platinum 6% Rhodium (-)	2500 -3100F 1370-1700C
<b>C</b>	W5Re Tungsten 5% Rhenium (+) W26Re Tungsten 26% Rhenium (-)	3000-4200F 1650-2315C
<b>E</b>	Chromel (+) Constantan (-)	200-1650F 95-900C
<b>J</b>	Iron (+) Constantan (-)	200-1400F 95-760C
<b>K</b>	Chromel (+) Alumel (-)	200-2300F 95-1260C
<b>N</b>	Nicrosil (+) Nisil (-)	1200-2300F 650-1260C
<b>R</b>	Platinum 13% Rhodium (+) Platinum (-)	1600-2640F 870-1450C
<b>S</b>	Platinum 10% Rhodium (+) Platinum (-)	1800-2640F 980-1450C
<b>T</b>	Copper (+) Constantan (-)	-330-660F -200-350C

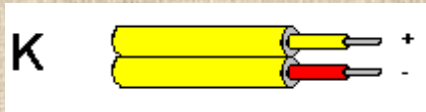
# Thermocouples



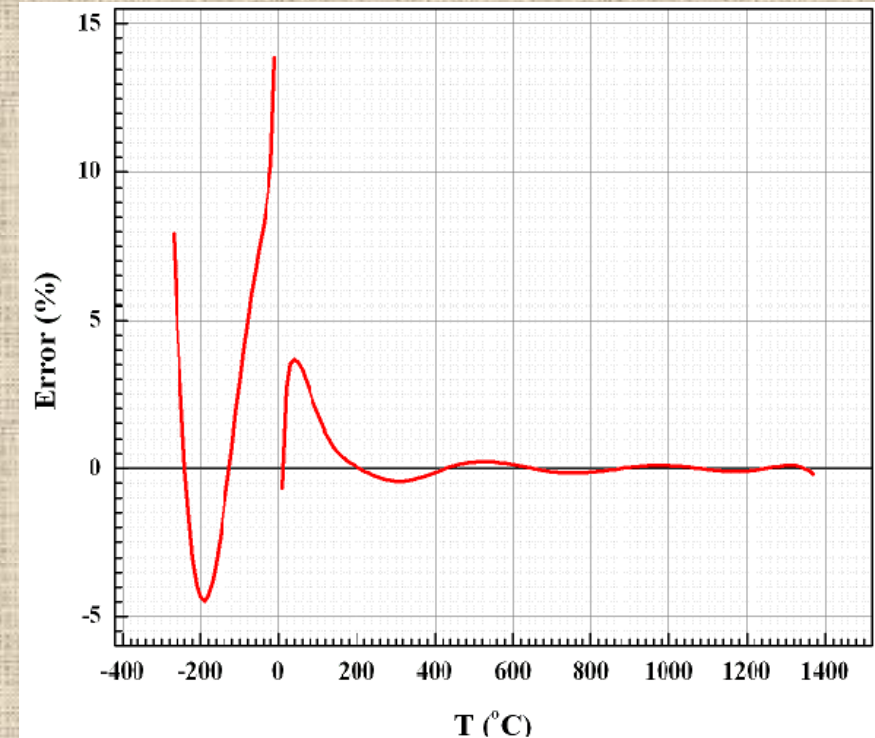
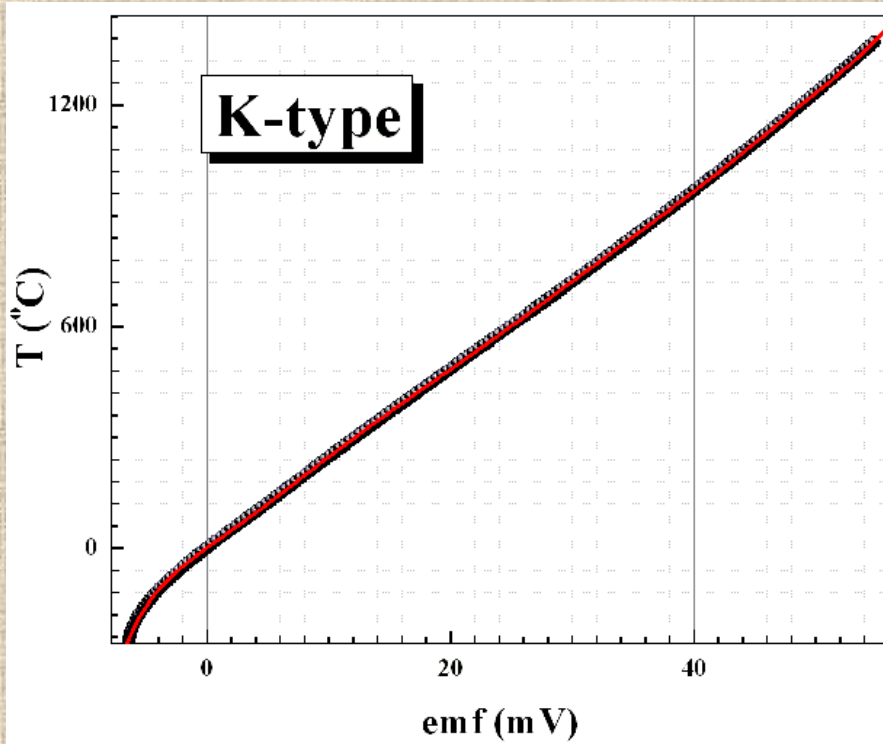


# Contacting devices:

emf (T) dependence



# Thermocouples

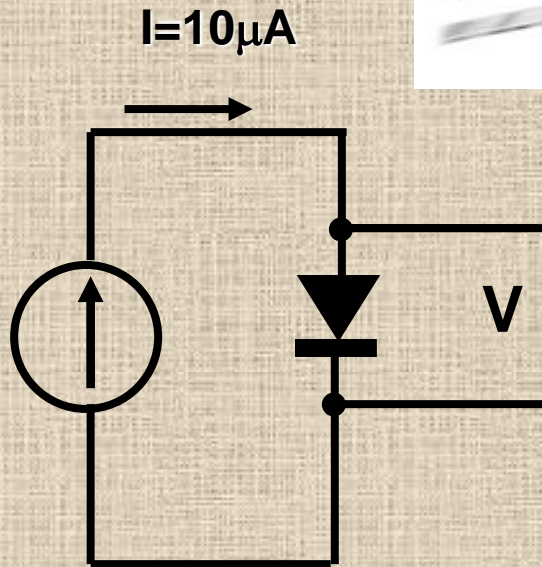


9<sup>th</sup> order polynomial fit

To reduce the error we have to split the temperature range in to a couple of segments

# Contacting devices:

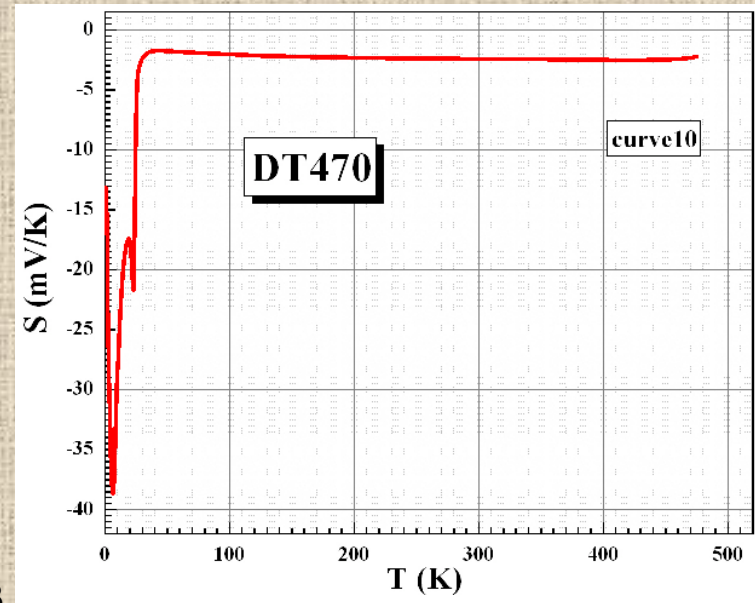
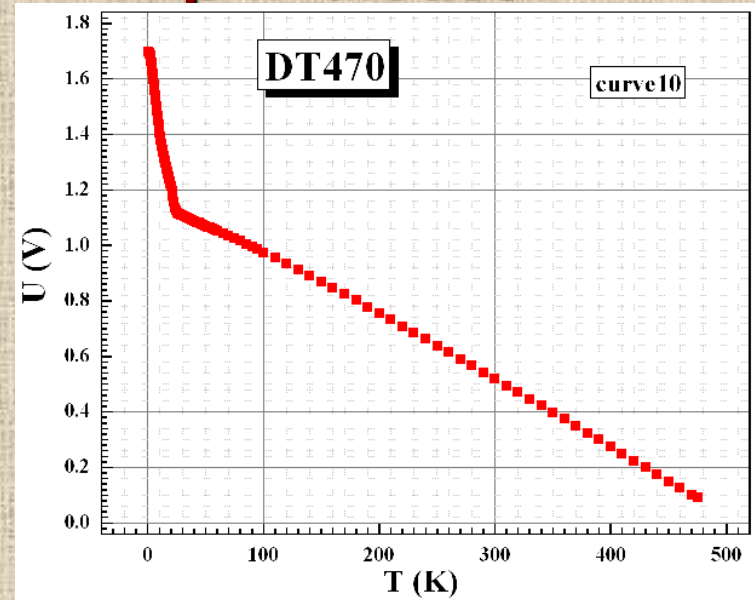
LakeShore



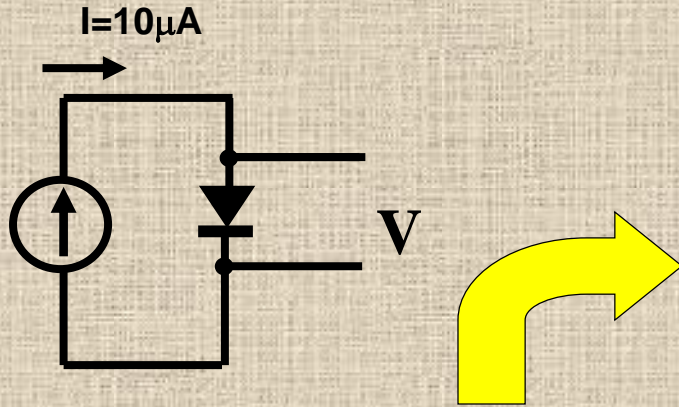
## DT-470-SD Features:

1. Monotonic temperature response from 1.4 K to 500 K.
2. Conformance to standard Curve 10 temperature response curve
3. Useful above 60 K in magnetic fields up to 5 T

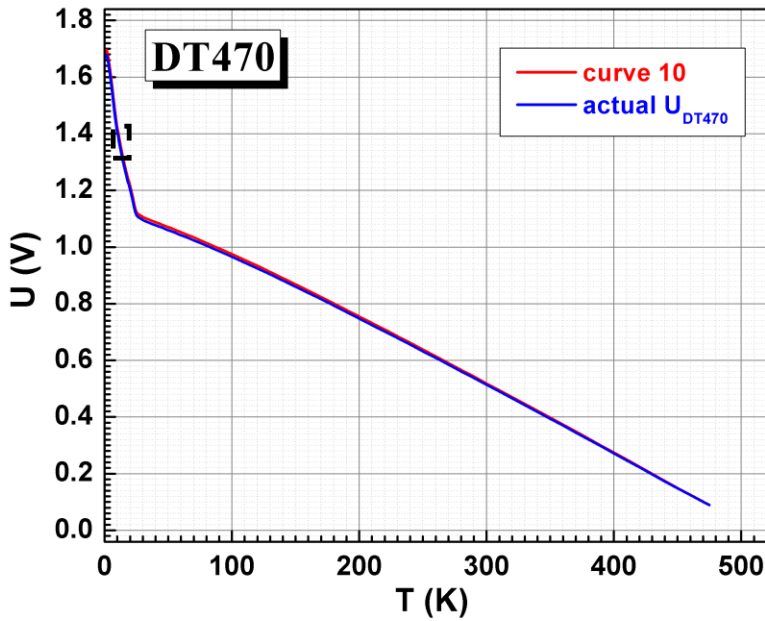
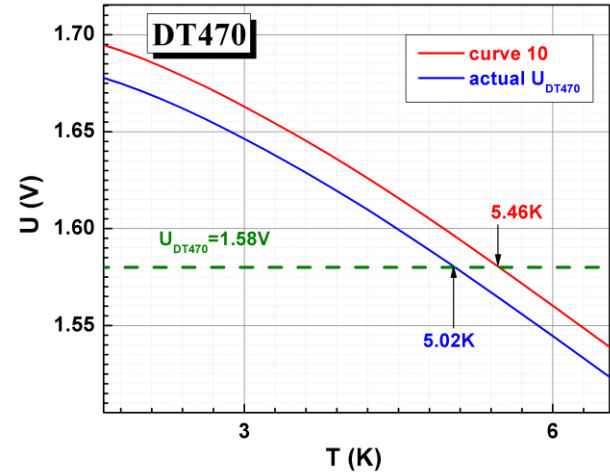
## p-n diodes



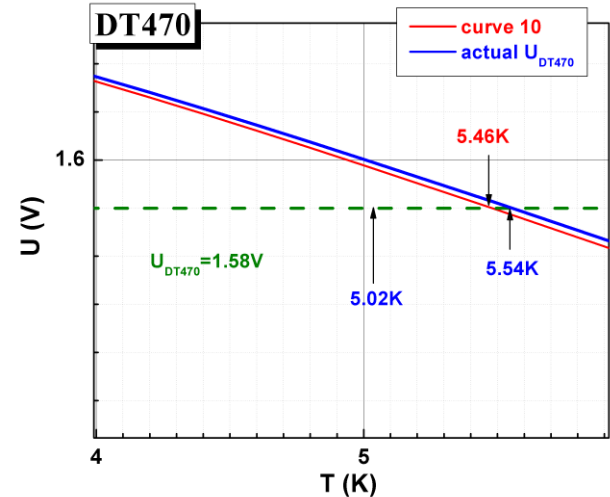
# Silicon diode DT470



# Calibration problems



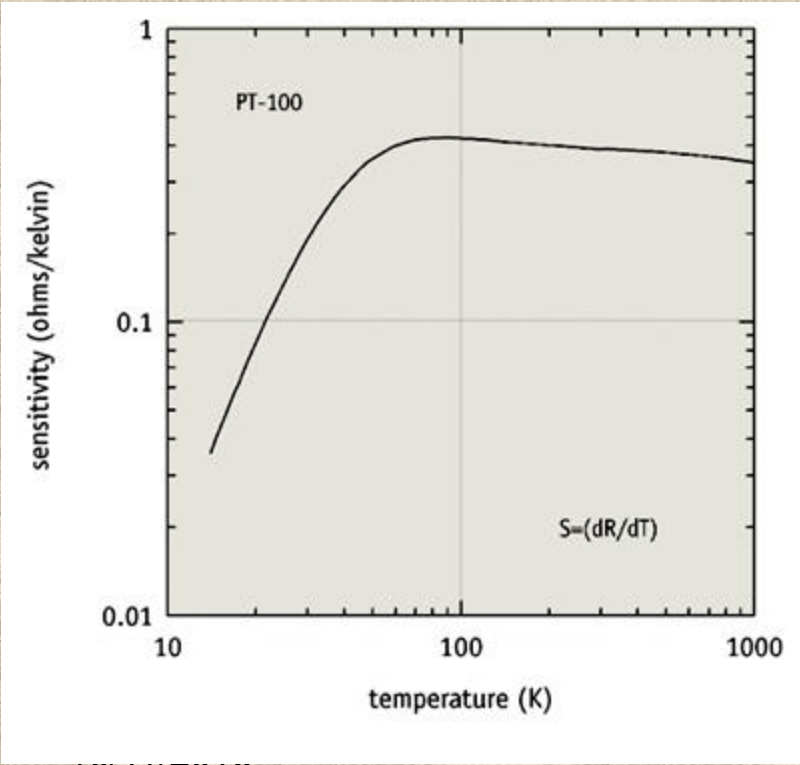
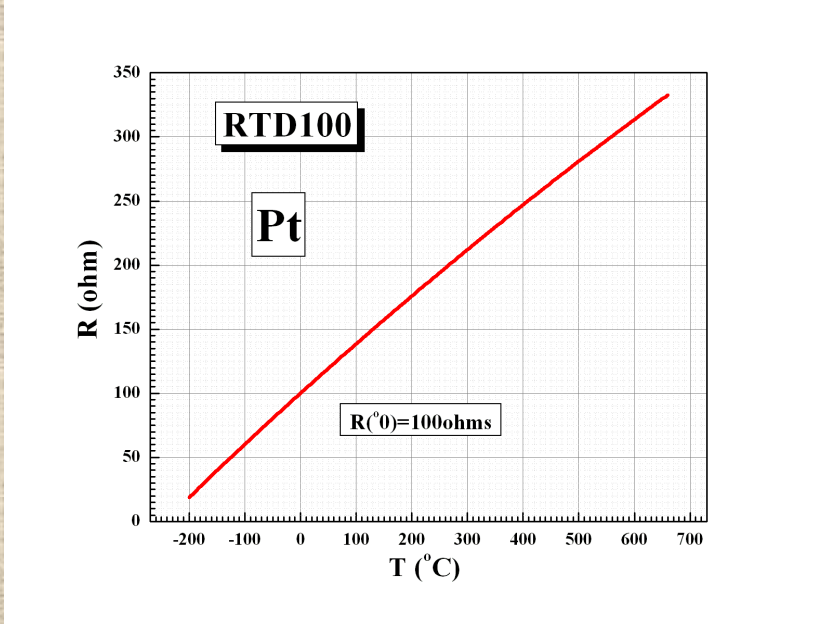
$$U^* = U_{DT470} \cdot k$$





# Contacting devices:

# Resistance Temperature Detectors

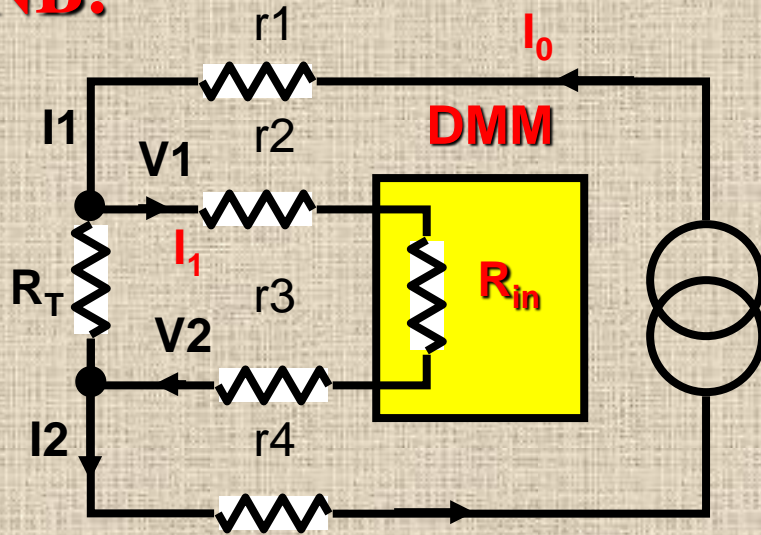


## RTD Features:

- 1. Temperature range: 14 K to 873 K
- 2. High reproducibility:  $\pm 5$  mK at 77 K
- 3. Low magnetic field dependence above 40 K
- 4. Excellent for use in ionizing radiation

# Measuring issue:

**NB!**



# Four probe technique



Most of DMM's have four probe option for resistance measurements.

If the sensor is mounted in cryostat the overall leads resistance could reach a couple of ohms. This will in case of RTD100 the resistance at 0°C is 100Ω give an error of a couple percent!

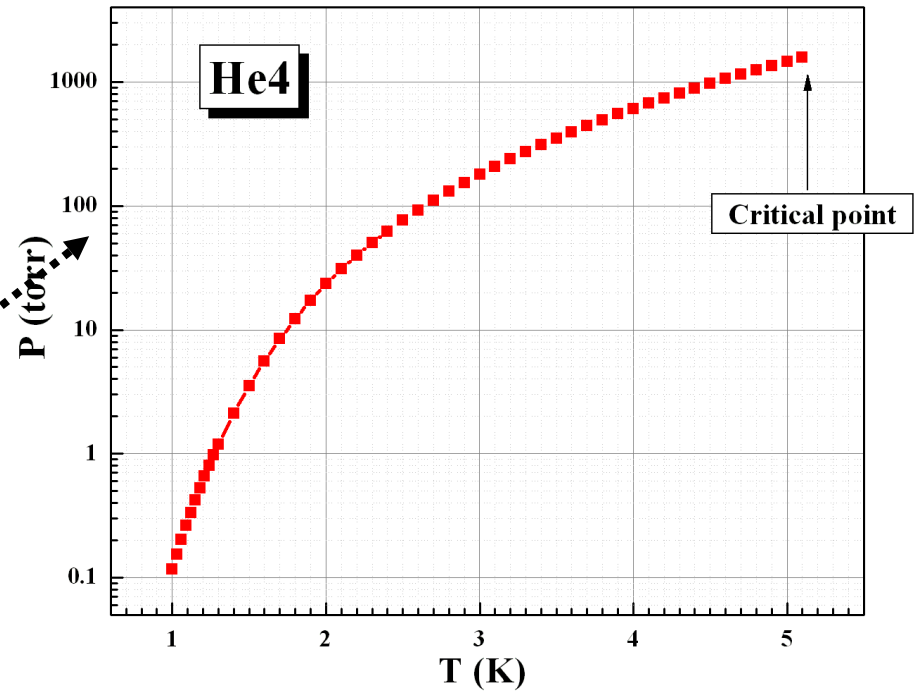
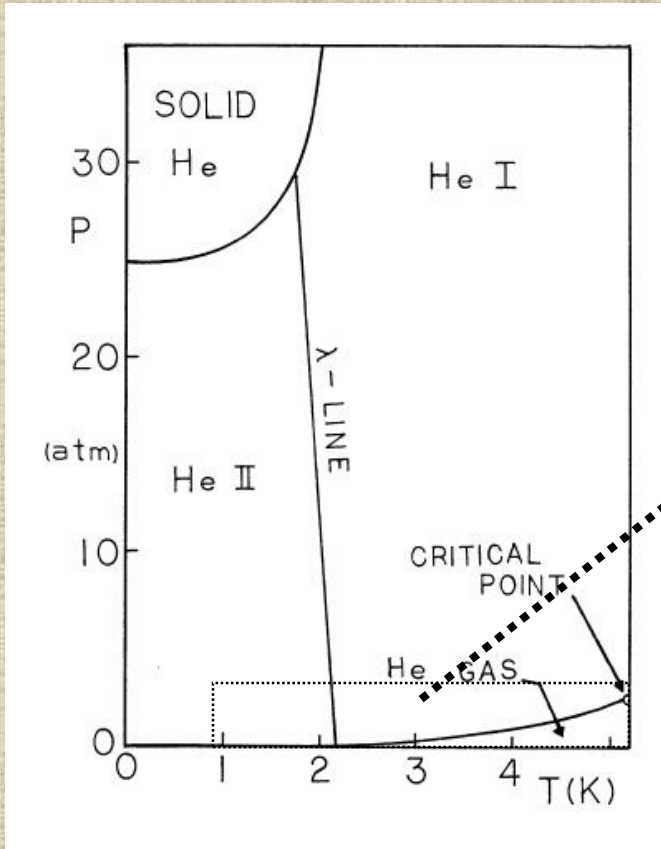
$$I_1 = I_0 * R_T / (r_2 + r_3 + R_{in}) \sim 0$$

$$R_{in} \sim 10^{10} \Omega$$

# Vapor Pressure Thermometry

## He4 P-T phase diagram

$$T_{90}/K = A_0 + \sum_{i=1}^9 A_i [(\ln(p/\text{Pa}) - B)/C]^i \quad (3)$$

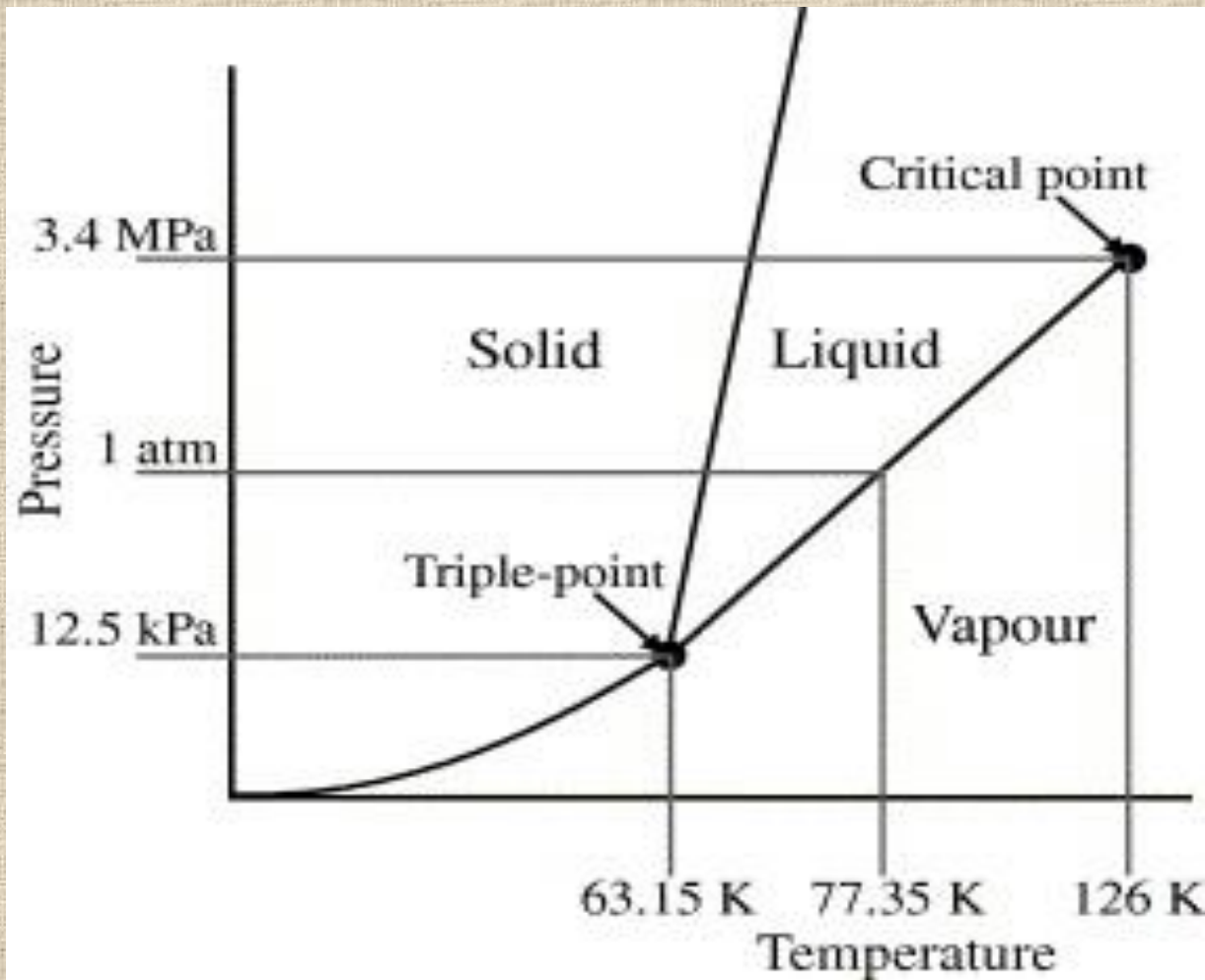


**Critical point of He4 T=5.19K ,P= 0.227 MPa**



# Vapor Pressure Thermometry

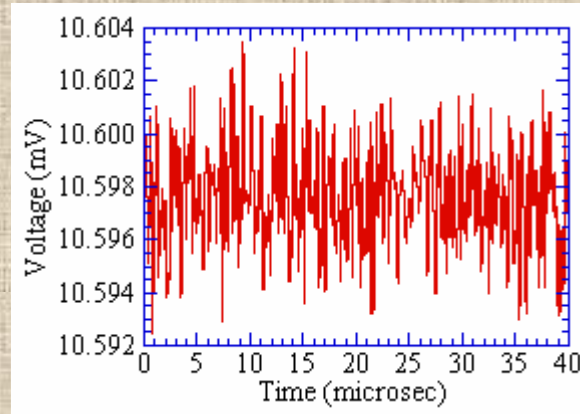
## Nitrogen P-T phase diagram



# Some more exotic techniques of measuring the temperature

## Johnson–Nyquist noise Thermometry

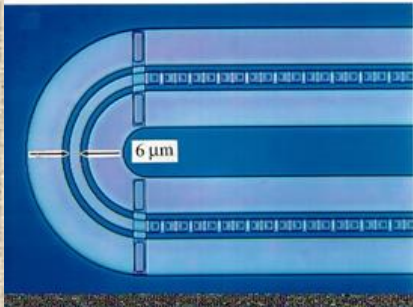
$$S^R = 4kTR(T)$$



John Bertrand Johnson  
(1887–1970)



Harry Nyquist  
(1889–1976)



2004 IEEE Aerospace Conference Proceedings

### Johnson Noise Thermometry for Harsh Environments

R. Kisner<sup>1</sup>, C. L. Britton<sup>1,2</sup>, U. Jagdish<sup>1</sup>, J. B. Wilgen<sup>1</sup>, M. Roberts<sup>2</sup>, T. V. Blalock<sup>2,3</sup>, D. Holcomb<sup>1</sup>,  
M. Bobrek<sup>1,2</sup>, M. N. Ericson<sup>1,2</sup>

<sup>1</sup>Oak Ridge National Laboratory, MS6006, Oak Ridge, TN 37831-6006, BRITTONCL@ornl.gov

<sup>2</sup>Dept. of Electrical and Computer Engineering, The University of Tennessee, Knoxville TN

<sup>3</sup>Deceased

Courtesy by NIST

10/11/2016

Physics 403

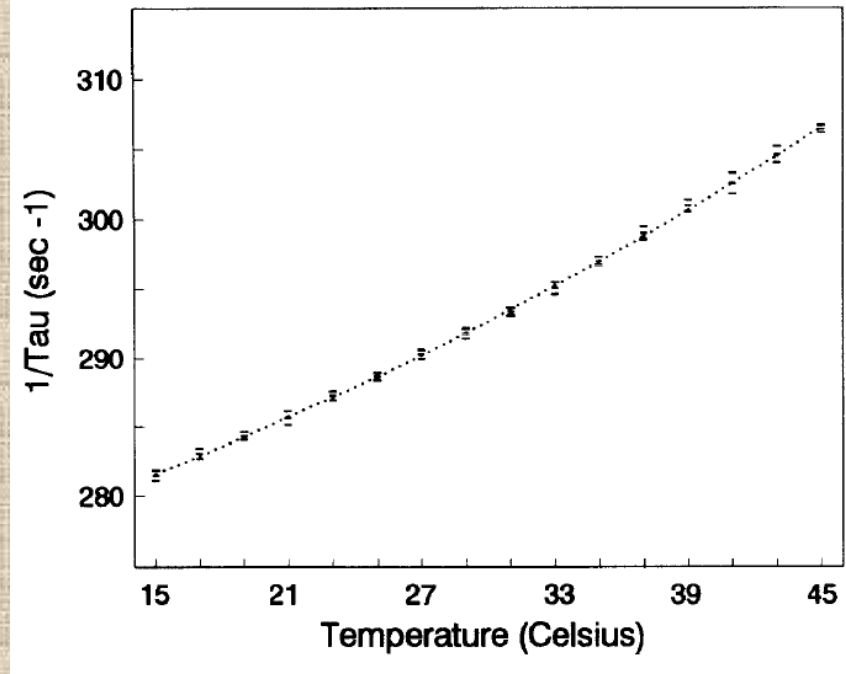
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# Some more exotic techniques of measuring the temperature

## Real time frequency domain fibreoptic temperature sensor using ruby crystals

J. R. Alcalá, S-C. Liao and J. Zheng

Department of Biomedical Engineering, Case Western Reserve University, Cleveland, OH 44106, USA

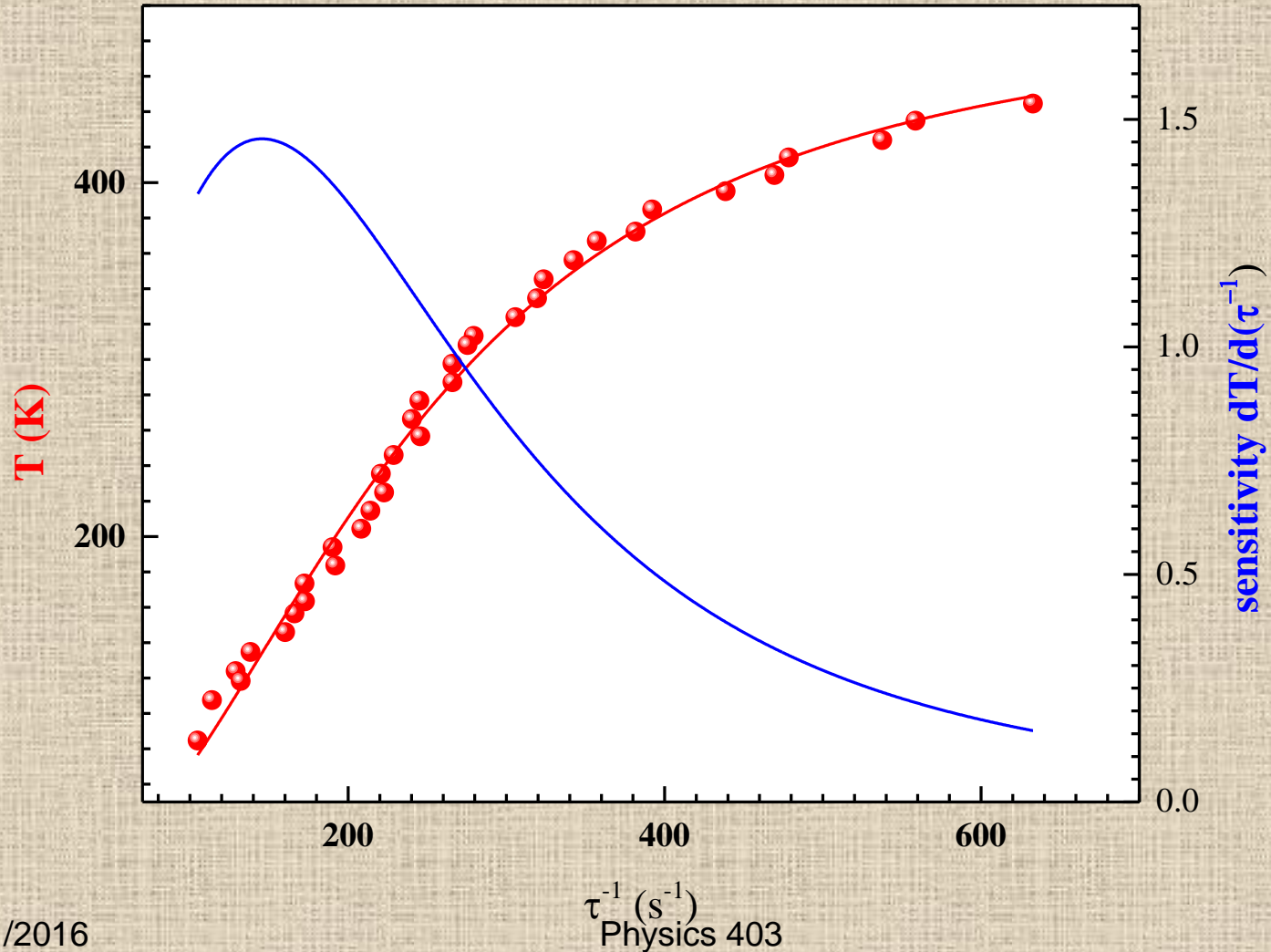


The use of optical methods, to invasively measure temperature, offers the advantage of electrical isolation, when compared to the traditional use of electronic thermometers. In some instances, optical techniques are necessary as in the case of clinical radio-frequency heat treatment, where interference from electromagnetic fields makes electronic thermometers unreliable. Optical tem-



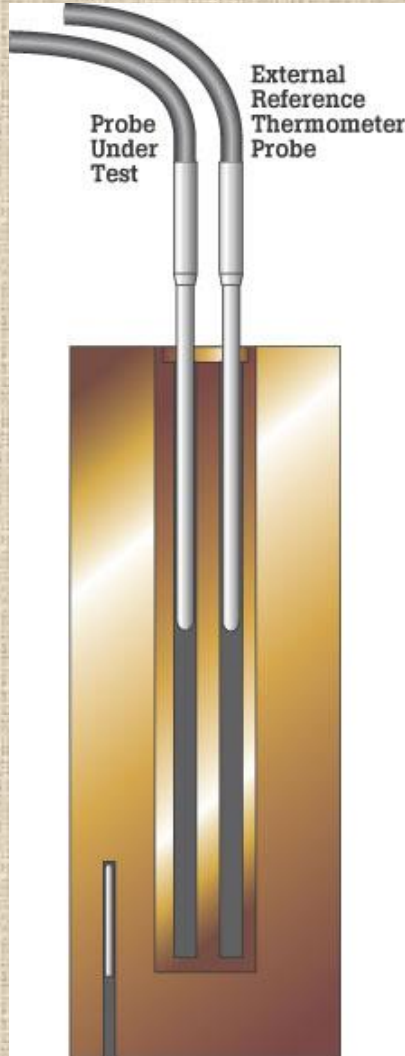
# Some more exotic techniques of measuring the temperature

Britton Jeter and Kyle Sendgikoski, P403, Spring 2014



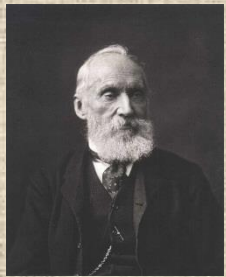
# Sensors Calibration

Official list of a fixed temperature points recommended for sensor calibration (ITS-90)



Temperature $T_{90}/\text{K}$	Temperature $t_{90}/^{\circ}\text{C}$	Substance	State
from 3 to 5	from - 270,15 to - 268,15	He - Helium	Saturated vapor pressure
83,805 8	- 189,344 2	Ar - Argon	Triple point
234,315 6	- 38,834 4	Hg - Mercury	Triple point
273,16	0,01	H <sub>2</sub> O - Water	Triple point
302,914 6	29,764 6	Ga - Gallium	Melting point
429,748 5	156,598 5	In - Indium	Solidification point
505,078	231,928	Sn - Tin	Solidification point
692,677	419,527	Zn - Zinc	Solidification point
933,473	660,323	Al - Aluminium	Solidification point
1 234,93	961,78	Ag - Silver	Solidification point
1 337,33	1 064,18	Au - Gold	Solidification point
1 357,77	1 084,62	Cu - Copper	Solidification point

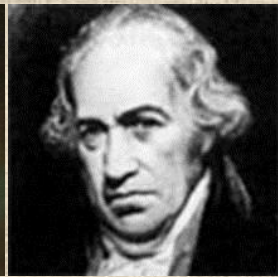
# Comparison of temperature scales



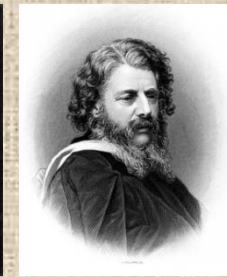
Kelvin



Celsius



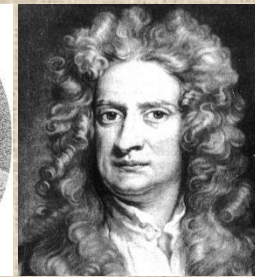
Fahrenheit



Rankine



Delisle



Newton



Réaumur



Rømer

Comment	Kelvin K	Celsius °C	Fahrenheit °F	Rankine °Ra (°R)	Delisle °D	Newton °N	Réaumur °R, (°Ré, °Re)	Rømer °Rø (°R)
<b>Absolute zero</b>	0	-273.15	-459.67	0	559.725	-90.14	-218.52	-135.90
<b>Lowest recorded natural temperature on Earth</b>	184	-89	-128	331	284	-29	-71	-39
<b>Water freezes (at standard pressure)</b>	273.15	0	32	491.67	150	0	0	7.5
<b>Average human body temperature <sup>2</sup></b>	310.0 ± 0.7	36.8 ± 0.7	98.2 ± 1.3	557.9 ± 1.3	94.8 ± 1.1	12.1 ± 0.2	29.4 ± 0.6	26.8 ± 0.4
<b>Highest recorded surface temperature on Earth</b>	331	58	136	596	63	19	46	38
<b>Water boils (at standard pressure)</b>	373.13	99.98	211.97	671.64	0	33	80	60
<b>Titanium melts</b>	1941	1668	3034	3494	-2352	550	1334	883
<b>The surface of the Sun</b>	5800	5526	9980	10440	-8140	1823	4421	2909



# Temperature scales: reference temperature points

Temperature scale	Temperature point #1	Temperature point #2	K to °X conversion
Rømer scale	0°Rø – temperature of freezing of brine	60°Rø – temperature of boiling water	$[^{\circ}\text{Rø}] = ([\text{K}] - 273.15) \times \frac{21}{4} + 7.5$
Réaumur scale	0°R – temperature of freezing water	80°R – temperature of boiling water	$[^{\circ}\text{Ré}] = ([\text{K}] - 273.15) \times \frac{4}{5}$
Delisle scale	0°D - temperature of boiling water	150°D - temperature of freezing water	$[^{\circ}\text{De}] = (373.15 - [\text{K}]) \times \frac{3}{2}$
Rankine scale	0°Ra – absolute zero	491.67°Ra temperature of water freezing. (1°Ra=1 °F)	$[^{\circ}\text{R}] = [\text{K}] \times \frac{9}{5}$
Fahrenheit scale	32 °F temperature of freezing water	212 °F temperature of boiling water	$[^{\circ}\text{F}] = [\text{K}] \times \frac{9}{5} - 459.67$
Newton scale	0°N – temperature of freezing water	33°N – temperature of boiling water	$[^{\circ}\text{N}] = ([\text{K}] - 273.15) \times \frac{33}{100}$
Celsius scale	0°C temperature of freezing water	100°C temperature of boiling water	$[^{\circ}\text{C}] = ([^{\circ}\text{R}] - 491.67) \times \frac{5}{9}$