

Name: \_\_\_\_\_

Quiz 5

Fall 2016

Distributed Algorithms

20 points

20 minutes

1. (6 points) Consider vector consensus for  $n$  processes with  $d$  dimensional inputs, in a synchronous system.

(a) State true or false: When  $d > 1$ , vector consensus can be achieved by performing consensus separately on each dimension of the input. \_\_\_\_\_

(b) Suppose that  $n = 4$  and  $d = 2$ . Suppose that the inputs at 3 non-faulty processes are  $(1,1)$ ,  $(2,1)$  and  $(1,2)$ , and the remaining process is faulty.

For each output below, specify whether it will satisfy the *validity* condition:

(i)  $(1.5, 1)$  \_\_\_\_\_

(ii)  $(2, 2)$  \_\_\_\_\_

2. (6 points) State True or False:

(i) With Ben-Or's algorithm, each non-faulty process always decides its output within  $2^n$  phases, where  $n$  is the number of processes. \_\_\_\_\_

(ii) With Ben-Or's algorithm, when two processes decide the output, their decision values are *exactly* equal. \_\_\_\_\_

(iii) With Ben-Or's algorithm, the decision value chosen by any process is always the input of some process. \_\_\_\_\_

3. (8 points)

(a) Consider two processes  $P_1$  and  $P_2$ , each with a 4-bit input. It is known that the input of process  $P_1$  is either 0000 or 1111. The input of process  $P_2$  may equal any of the 16 possible 4-bit values.

What is the least number of bits of communication necessary for  $P_1$  to determine whether its input equals the input of  $P_2$ ? \_\_\_\_\_

(b) Consider 10 processes  $P_1, P_2, \dots, P_{10}$  each with a  $k$ -bit input that can take any of the  $2^k$  possible values. Assume that  $k > 100$ . Suppose that the given processes are connected by a broadcast channel. When a message is sent over the broadcast channel by any process, all the processes receive it.

By transmitting at most  $2k$  bits on the broadcast channel, can all the processes determine whether their inputs are equal? \_\_\_\_\_