

# Password Cracking

eCrime and Internet Service Abuse +  
Applied Cryptography  
Combined Lecture

Let  $U$  be the set of users

And let  $p$  be the user's password

$$\forall u_i \in U,$$

store  $\{u_i, C_i\}$

where  $C_i = E_p(\text{Nonce})$

## P. Oechslin's Attack

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# P. Oechslin's Attack

$E_p(\text{Nonce})$  vs.  $H(p)$

1. Both take in a secret  $p$  and output a value indistinguishable from random
2. Both make it cryptographically hard to recover  $p$

The attack will work on either method

We will use the  $H(k)$  notation today



# Math

Let  $H()$  be a cryptographic hash function

Let  $P$  be the set of all possible passwords.

Let  $p_i$  be a password from the set  $P$ .

Let  $h_i = H(p_i)$

Let  $H$  be the set of the corresponding  $h_i$  for all  $p_i$

$|H| == |P|$

# Hash Table

For every  $p_i$  in  $P$ :

    Compute & Store  $h_i$

Time complexity to generate:  $\Theta(|P|)$

Time complexity to lookup:  $\Theta(\log(|P|))$

Space complexity:  $\Theta(|P|)$

# How big is $|P|$ ?

Consider an exactly 7-character password with upper and lower case letters.

$$\text{Permutation}(48,7) = 587,068,342,272$$

How long would it take to generate every SHA-256 hash?

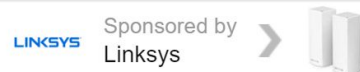
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## AntMiner S1 DUAL Blade 200 GH/s ASIC Bitcoin Miner (OVERCLOCKED FOR YOU)

by AntMiner

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LIKE NEW, OVERCLOCKED 200GH/S, SHIPS SAME DAY



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# How big is $|P|$ ?

Consider an exactly 7-character password with upper and lower case letters.

$$\text{Permutation}(48,7) = 587,068,342,272$$

$$200\text{Gh} = 200,000,000 \text{ hashes per second}$$

$$P(48,7)/200\text{Gh} = \sim 50 \text{ Minutes on a } \$400 \text{ machine}$$

# How big is $|P|$ ?

Consider an exactly 7-character password with upper and lower case letters.

Sha-256 hash = 32 bytes

32 bytes \*  $|P|$  = 17 TB

# Idea

Can we trade lookup time for storage reduction?

# Hash Chains

Define a reduction function  $R$  that maps from hash-output space back into  $P$ .

For each chain, select a random  $p_i$  from  $P$  as your starting point.

$$\text{Chain}_i = [p_i \rightarrow R(H(p_i)) \rightarrow \{\text{repeat } t \text{ times}\} \rightarrow \text{final\_value}]$$

Repeat until you have coverage.



# Reduction Function

Its input is the output of a hash function: 0x59ae5403928df849394...

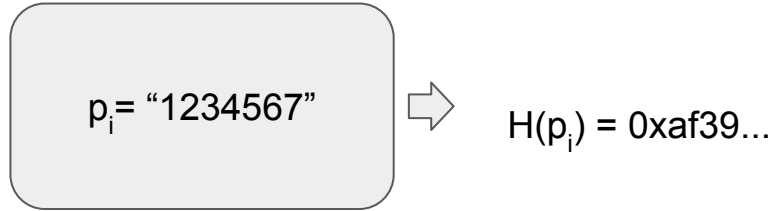
Its output is a string that is a possible password: “a#2%33pq”

*Simple example, treat the last 7 bytes of the hash as ascii.*

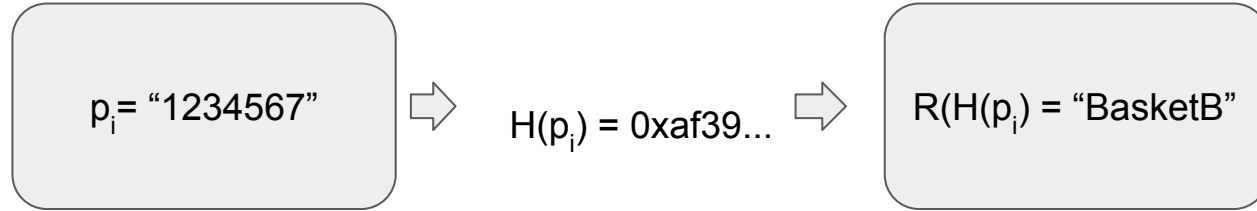
# Hash Chains

$p_i = \text{"1234567"}$

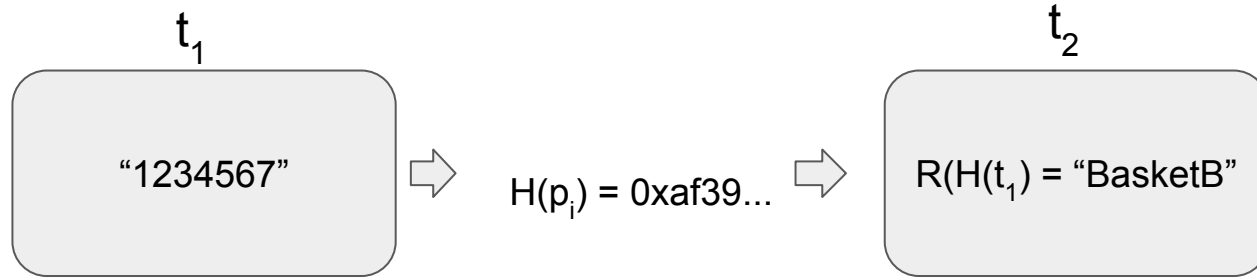
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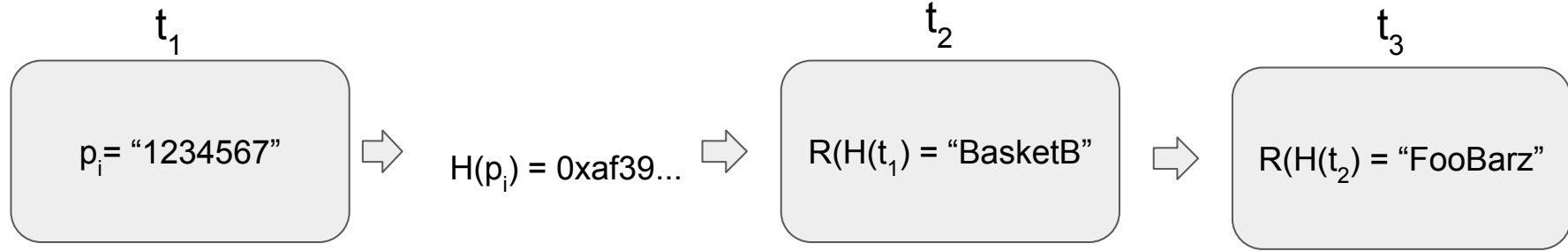
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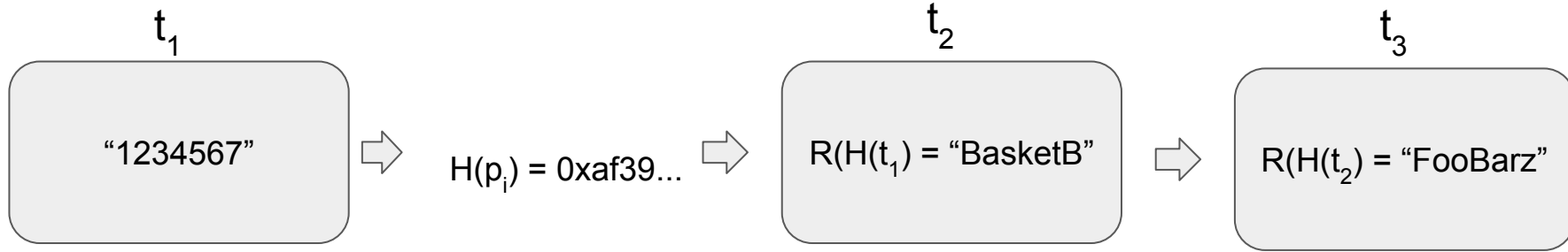
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*\*If I store  $t_1$  then I can re-compute the whole chain.*

*\*If I store  $t_n$  (the last link) then I can check if any password is in the chain.*

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Start with a hash - apply  $R()$  to it and see if it matches any of the stored end-links



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If you find a match, the true password lies in that chain.

If you never see a match, your chains do not contain the answer.

# Collisions

Hash chains collide when they contain duplicate values.

Once two chains have a duplicate value, all subsequent values must also be the same. They will contain duplicate information.

The greater coverage of  $P$  you try to get, the more collisions will happen.

There can also be cycles within a single chain.

# Choosing a Smart Reduction Function

- Avoid Cycles/Collision
- Map to likely values in P
- Different Reduction Function for each chain

# Rainbow Tables

Build a series of unique reduction functions  $R_i$  applied at  $t_i$  on the chain.

Collisions will diverge unless they are collisions in the exact same step on the chain. Collisions are  $|R|$  times less likely to occur.

# Salting

Hash( Password|Salt )

Dilutes the value of pre-computed tables

Why Not Just Ask Nicely?



# Why Not Just Ask Nicely?

To: you@gmail.com

Re: Dan from Google - Your Account

Your google account has been {penalty} for {reasons}!

Sign in here to fix this urgent problem!

[google.com](evil.com)

-Dan from Google Customer Support

# Idea

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Are you then safe if you are not a valuable target?

Do you plan not to be a valuable target forever?

# Another Idea

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-> afableyellow

**Error: your password must contain at least 1 number and 1 special character**

-> afableyellow1!

**Registration Complete**



# Smart Guessing

Dictionary words

Dictionary words with substitutions

Keyboard patterns

Patterns (like number and special char at the end)

Leaked Password Lists

# 517,238,891 Leaked Passwords

## Pwned Passwords

Pwned Passwords are 517,238,891 real world passwords previously exposed in data breaches. This exposure makes them unsuitable for ongoing use as they're at much greater risk of being used to take over other accounts. They're searchable online below as well as being downloadable for use in other online system. [Read more about how HIBP protects the privacy of searched passwords.](#)

You've disabled JavaScript! If you submit a password in the form below, it will not be anonymised first.



1Password

Logo

Generate secure, unique passwords for every account

[Learn more at 1Password.com](#)

[Why 1Password?](#)

<https://haveibeenpwned.com>

# Password Crackers

HashCat

JohnTheRipper

Ophcrack

Aircrack

DavidGrohl

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But you have to reveal the salt as a public parameter

Attackers can start working on cracking tables for individual accounts right now!

# Preventing Pre-Computation (*Jarecki et al. 2018*)

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$$\text{ZK}\{(pwd): H = H(H(pwd, H'(pwd)^b), pwd)\}$$



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*Attackers have to guess full entropy  $b$  before they can generate any lookup tables*