

**Reading Assignment:**

FPE, Sections 7.1–7.5, 7.7–7.8.

**Problems:** (all computations using Matlab)

*Modeling & full-state feedback:*

1. Consider the SISO model,

$$Y(s) = \frac{s+1}{s^2+2s+2}U(s)$$

Obtain a second-order state-space model (without Matlab).

Obtain a state-feedback compensator  $u = -Kx + r$ , placing the closed loop poles at  $-4$  and  $-25$ .

2. Consider the satellite position model with delay,

$$G_p(s) = \frac{1-s/2}{1+s/2} \frac{1}{s^2}.$$

Obtain a third-order state-space model (without Matlab).

Obtain a state-feedback compensator  $u = -Kx + r$ , placing the closed loop poles at  $-4$ ,  $-13$  and  $-25$ .

*Observers & sensitivity*

3. Return to the feedback system considered in Problem 1:
  - (a) Construct a stable observer to estimate  $x$  based on measurements of  $(u, y)$ .
  - (b) Obtain a state-feedback compensator  $u = -K\hat{x} + K_r r$ , where  $K$  was obtained in your prior work, and  $K_r$  is chosen so that the DC gain  $Y/R$  is equal to unity.
  - (c) Obtain a step response using Matlab.
4. Return to the feedback system considered in Problem 2:
  - (a) Construct a stable observer, and using this obtain a compensator of the form  $U = -G_c Y + G_r R$ .
  - (b) Obtain a Nyquist plot for  $G_c G_p$  using Matlab, and estimate the gain and phase margins.