ECE 313: Exam III

Wednesday, July 25, 2018 10-10.50 a.m. 1013 ECEB

Name: (in BLOCK CAPITALS)

NetID: _____

Signature:

Instructions

This exam is closed book and closed notes except that one $8.5" \times 11"$ sheet of notes is permitted: both sides may be used. Calculators, laptop computers, PDAs, iPods, cellphones, e-mail pagers, headphones, etc. are not allowed.

example, write $\frac{3}{4}$ instead of $\frac{24}{32}$ or 0.75).

SHOW YOUR WORK; BOX YOUR ANSWERS. Answers without appropriate justification will receive very little credit. If you need extra space, use the blank page at the end of the exam.

Grading	
1. 25 points	
2. 20 points	1
3. 25 points	
4. 30 points	
Total (100 points)	

1. [25 points] Let X be a random variable with CDF given below, where c_1 is a constant.

$$F_X(u) = \begin{cases} \frac{1}{8}e^{c_1u+1} & u < -1\\ \frac{1}{4} & -1 \le u < 1\\ 1 - \frac{3}{4u} & u \ge 1 \end{cases}$$

NOTE: you can leave your answers in terms of c_1 , except for part (a).

(a) Obtain all possible values of c_1 .

(b) Obtain $P\{X = 2\}$.

(c) Obtain $P\{-1 < X < 1\}$.

(d) Obtain $P\{X \ge 1\}$.

- 2. [20 points] The two parts of this problem are unrelated
 - (a) Let $X \sim N(-1,4)$. Determine $P\{X^3 < 27\}$ in terms of the Q function.

(b) Let $Y \sim Binomial(1000, 0.25)$. Use the Gaussian approximation with continuity correction to determine $P\{|Y - 250| < 60\}$ in terms of the Q function.

- 3. [25 points] A celebrity couple, Alex and Morgan, Tweets regularly. The time that it takes for their Tweets to be taken down depends on who actually Tweets. If Alex Tweets, the time that it takes for the Tweet to be taken down is uniformly distributed from zero to three hours, while the time that it takes for a Tweet from Morgan to be taken down is exponentially distributed with parameter 2/hour. Assume that each Tweet has probability $\frac{1}{3}$ of being posted by Alex.
 - (a) Suppose a Tweet is posted and it has not been taken down after four hours. What is the conditional probability it will still not be taken down for at least three more hours?

(b) Suppose another Tweet is posted and it has not been taken down after two hours. What is the conditional probability it will still not be taken down for at least three more hours?

(c) Determine the expected value of the time that it takes for one of their Tweets to be taken down.

- 4. [30 points] Let X have pdf $f_X(u) = -\frac{2}{9}u$ for $u \in [-3, 0]$ and zero else.
 - (a) Determine $P\{X = -2\}$.

(b) Determine $P\{-2 < X \le 1\}$.

(c) Determine $E\left[\frac{1}{X}\right]$.

(d) Let $Z = -(X + 2)^2$, determine its pdf, $f_Z(c)$, for all c.

You may use this sheet for additional calculations but do not separate this sheet from the rest of the exam.

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