

Study Guide for a No-Calculator Exam: *Fractions*

HINT #1. The numerator (top) and denominator (bottom) may be multiplied or divided by the same value without changing the fraction's numeric value.

example i. $\frac{9}{12} = \frac{\frac{9}{3}}{\frac{12}{3}} = \frac{3}{4} = 0.75$

example ii. $\frac{4}{5} = \frac{8}{10} = 0.8$

example iii. $\frac{150}{500} = \frac{150 \times 2}{500 \times 2} = \frac{300}{1000} = \frac{3}{10} = 0.3$

HINT #2. Dividing by powers of 10 is easy. Use HINT #1 to get powers of 10 in denominator.

example i. $\frac{150}{100} = 1.50$ (move the decimal point)

example ii. $\frac{8}{250} = \frac{8 \times 4}{250 \times 4} = \frac{32}{1000} = 32 \text{ m}$ ("milli")

example iii. $\frac{1}{3k} = \frac{1}{3} \text{ m} = 0.33 \text{ m}$

example iv. $\frac{16}{320k} = \frac{1}{20k} = \frac{1}{20} \text{ m} = \frac{1}{20} e^{-3} = .5e^{-4}$

HINT #3. "Powers" add when multiplied and subtract when divided.

example i. $\frac{150e^6}{50e^8} = \frac{150}{50} e^{(6-8)} = 3e^{-2} = 0.03$

example ii. $\frac{6e^9}{8e^{-9}} = \frac{6}{8} e^{18} = \frac{3}{4} e^{18} = .75e^{18}$

Worksheet #1

Reduce each fraction to a non-fractional value. You can *check* your answers with a calculator.

1. $\frac{8}{4} =$

2. $\frac{80}{4} =$

3. $\frac{8}{40} =$

4. $\frac{6}{2} =$

5. $\frac{6}{20} =$

6. $\frac{60}{20} =$

7. $\frac{6}{200} =$

8. $\frac{9}{2} =$

9. $\frac{90}{2} =$

10. $\frac{9}{20} =$

11. $\frac{9}{200} =$

12. $\frac{3}{2} =$

13. $\frac{30}{2} =$

14. $\frac{3}{200} =$

15. $\frac{3}{2000} =$

16. $\frac{5}{4} =$

17. $\frac{50}{40} =$

18. $\frac{50}{4} =$

19. $\frac{5}{400} =$

20. $\frac{7}{4} =$

21. $\frac{7}{40} =$

22. $\frac{7}{400} =$

Worksheet #2

Which fraction/value is **not** equivalent to the first? There may be more than one!

$\frac{0.4}{100}$ <p>a. $\frac{4}{1000}$ b. $\frac{0.04}{10}$ c. $\frac{0.04}{1000}$ d. $\frac{0.1}{25}$ e. 0.004</p>	$\frac{5}{200}$ <p>a. $\frac{10}{400}$ b. $\frac{1}{40}$ c. $\frac{1}{4 \times 10}$ d. 0.04 e. 0.025</p>	$\frac{7}{500}$ <p>a. $\frac{7}{1000}$ b. $\frac{14}{1000}$ c. $\frac{7/5}{100}$ d. $1.4e - 2$ e. 0.014</p>	$\frac{9}{300}$ <p>a. $\frac{9/3}{300/3}$ b. $\frac{3}{100}$ c. .09 d. 0.03 e. 30 m</p>
$\frac{3}{1200}$ <p>a. $\frac{1}{400}$ b. $\frac{9}{3600}$ c. $\frac{1}{4} \times \frac{1}{100}$ d. $0.25e - 2$ e. 0.00025</p>	$\frac{6}{300}$ <p>a. $\frac{2}{100}$ b. $\frac{20}{1000}$ c. 20 m d. 20000 μ e. $2e - 3$</p>	$\frac{7}{120}$ <p>a. $\frac{7}{12} \times \frac{1}{10}$ b. $1\frac{5}{7}e - 1$ c. $\approx 1.7e - 2$ d. ≈ 0.17 e. $\approx 170 m$</p>	$\frac{1}{20}$ <p>a. $\frac{10}{200}$ b. $\frac{10}{2000}$ c. $\frac{50}{1000}$ d. 50 m e. 0.05</p>
$\frac{4}{50}$ <p>a. $\frac{8}{100}$ b. $\frac{80}{1000}$ c. 80 m d. 0.08 e. $8e - 3$</p>	$\frac{120}{600}$ <p>a. $\frac{20}{300}$ b. $\frac{2}{3} \times \frac{10}{100}$ c. $\frac{2}{3} \times \frac{1}{10}$ d. 0.67 e. 0.067</p>	$\frac{64}{800}$ <p>a. $\frac{8}{100}$ b. .8 c. .08 d. 80 m e. 800m</p>	$\frac{3}{270}$ <p>a. $\frac{1}{90}$ b. $\frac{12}{1080}$ c. $\frac{1}{9}e - 1$ d. 0.111 e. 0.0111</p>
<p>Answers (left to right, top to bottom): c; d; a; c; e; e; b,c,d,e; b; e; a,b,c,d,e; b,e; d</p>			

Worksheet #3

Reduce each fraction to a non-fractional value. The first is done for you.

1. $\frac{.4}{100} = 0.004$	10. $\frac{8m}{50k} \times 50 =$
2. $\frac{.5}{200} =$	11. $\frac{12}{24m} \times 10 =$
3. $\frac{1.8}{200} =$	12. $\frac{6e-8}{9e-10} =$
4. $\frac{1.8}{10k} =$	13. $\frac{6e-8}{12e9} =$
5. $\frac{180}{10k} =$	14. $\frac{4e8}{8e8} =$
6. $\frac{4k}{10k} =$	15. $\frac{2e8}{12m} =$
7. $\frac{4k}{10m} =$	16. $\frac{1.6e-19}{1200} \times 300 =$
8. $\frac{.03}{10k} \times 100 =$	17. $\frac{16}{28m} \times 3k =$
9. $\frac{3}{40m} \times 200 =$	18. $\frac{16e8}{2000m} \times \frac{1}{8} =$

Answers (your format may vary):

1. 4m	10. 8e-6
2. 5m	11. 5k
3. 9m	12. 66.7
4. 0.18m	13. 0.5e-17
5. 18m	14. 0.5
6. 0.4	15. 0.167e11
7. 400,000	16. 4e-20
8. 0.3m	17. 1.71e6
9. 15	18. 100,000

Study Guide for a No-Calculator Exam: *Logarithms*

HINT #1. $\log_2 A = x$ such that $2^x = A$

example i. $\log_2 1 = 0$

example ii. $\log_2 2 = 1$

example iii. $\log_2 4 = 2$

HINT #2. $\log_2 \frac{1}{A} = -\log_2 A$

HINT #3. $\log_2 AB = \log_2 A + \log_2 B$

example i. $\log_2 6 = \log_2 2 + \log_2 3$

HINT #4. Use HINT#2 to fill in a table of logs when given logs of some of the factors in the table.

example i. Given $\log_2 3 = 1.6$, and using two examples from above, we find that $\log_2 6 = 1 + 1.6 = 2.6$.

example ii. $\log_2 12 = \log_2 2 + \log_2 2 + \log_2 3 = 1 + 1 + 1.6 = 3.6$

example iii. $\log_2 \frac{3}{7} = \log_2 3 - \log_2 7 = 1.6 - 2.8 = -1.2$, where $\log_2 7 = 2.8$ was known.