

Active Adversary

Lecture 7

CCA Security

MAC

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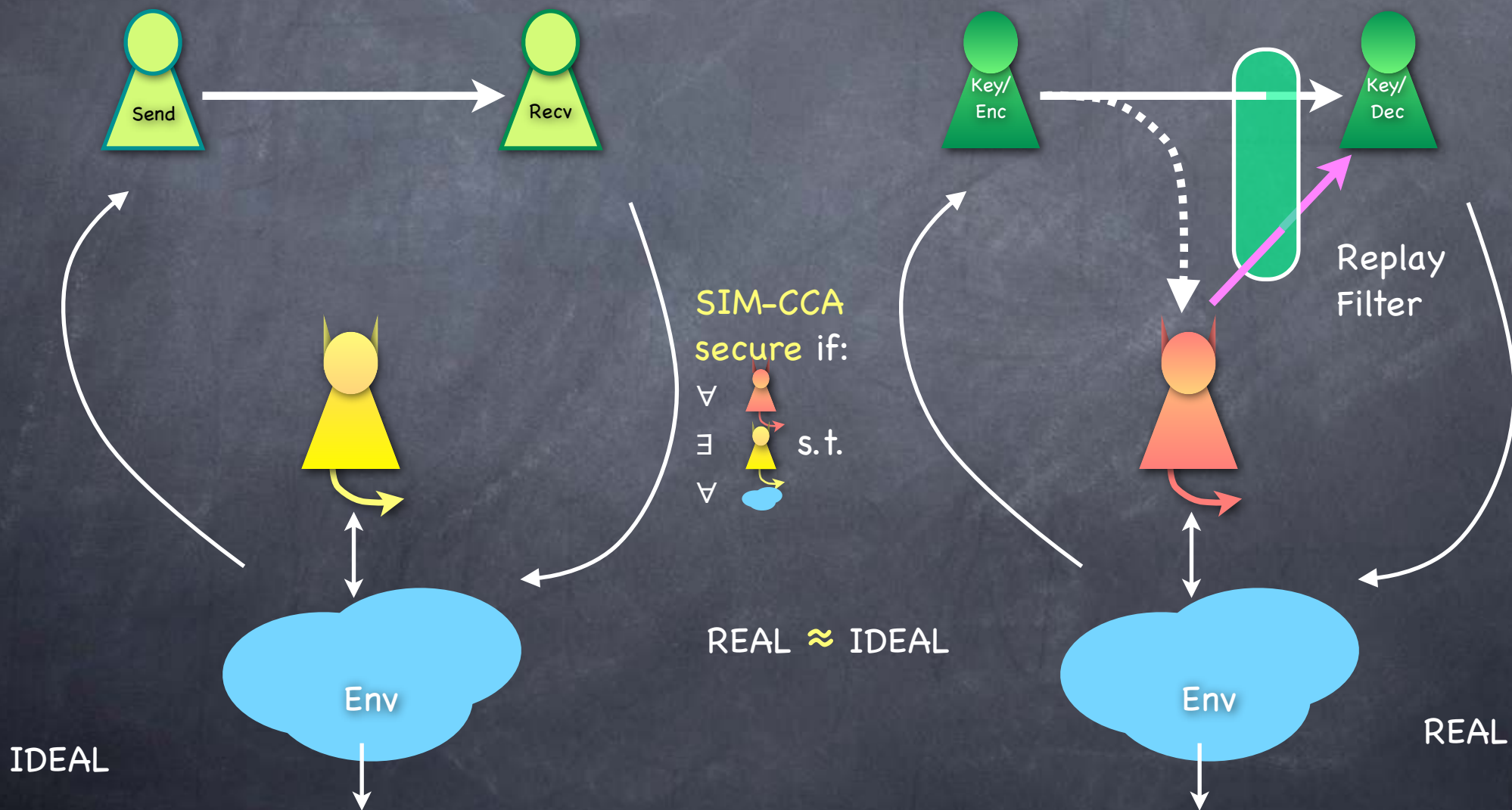
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 - What can Bob do?

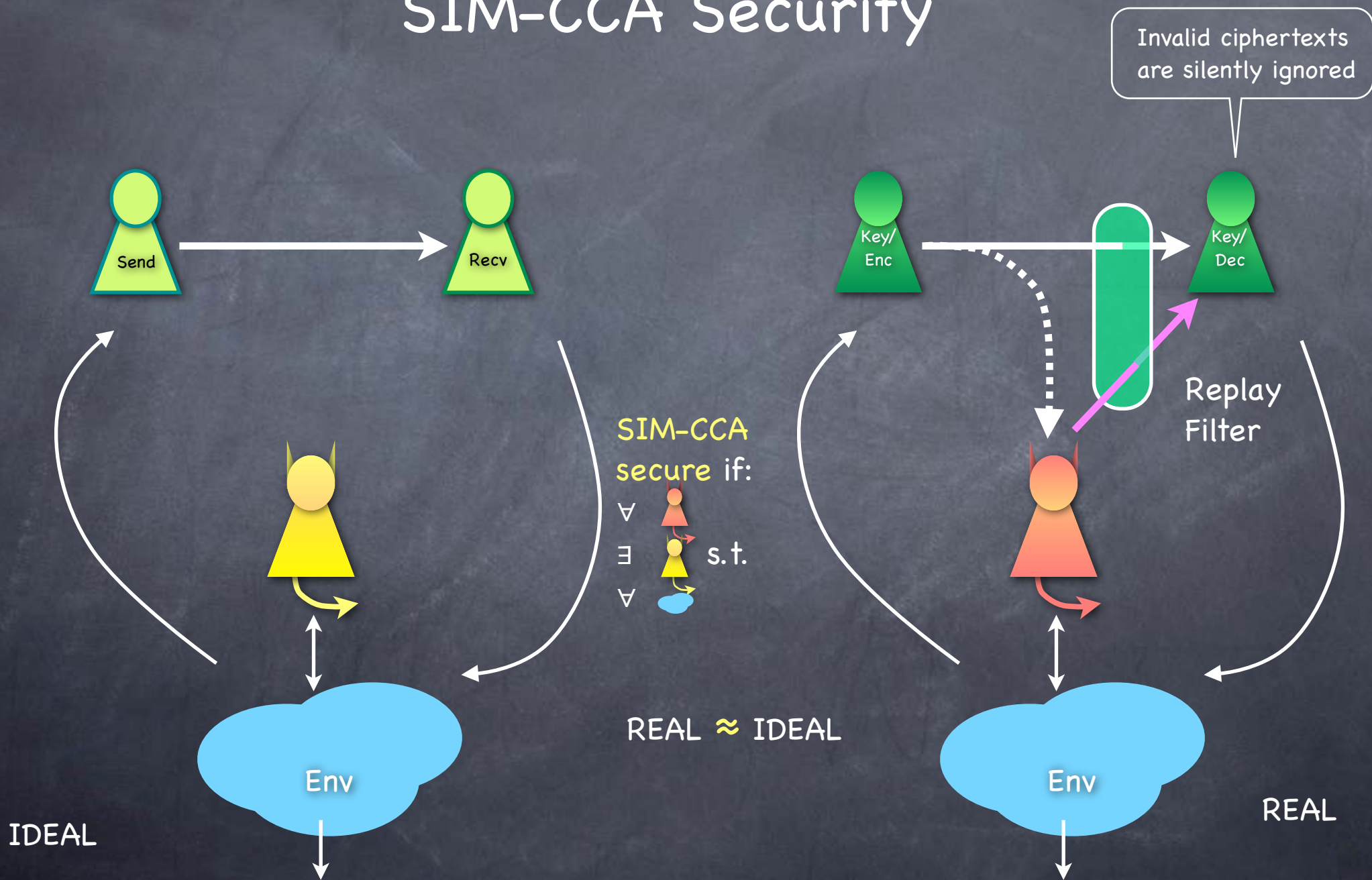
Symmetric-Key Encryption

SIM-CCA Security



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IND-CCA Security

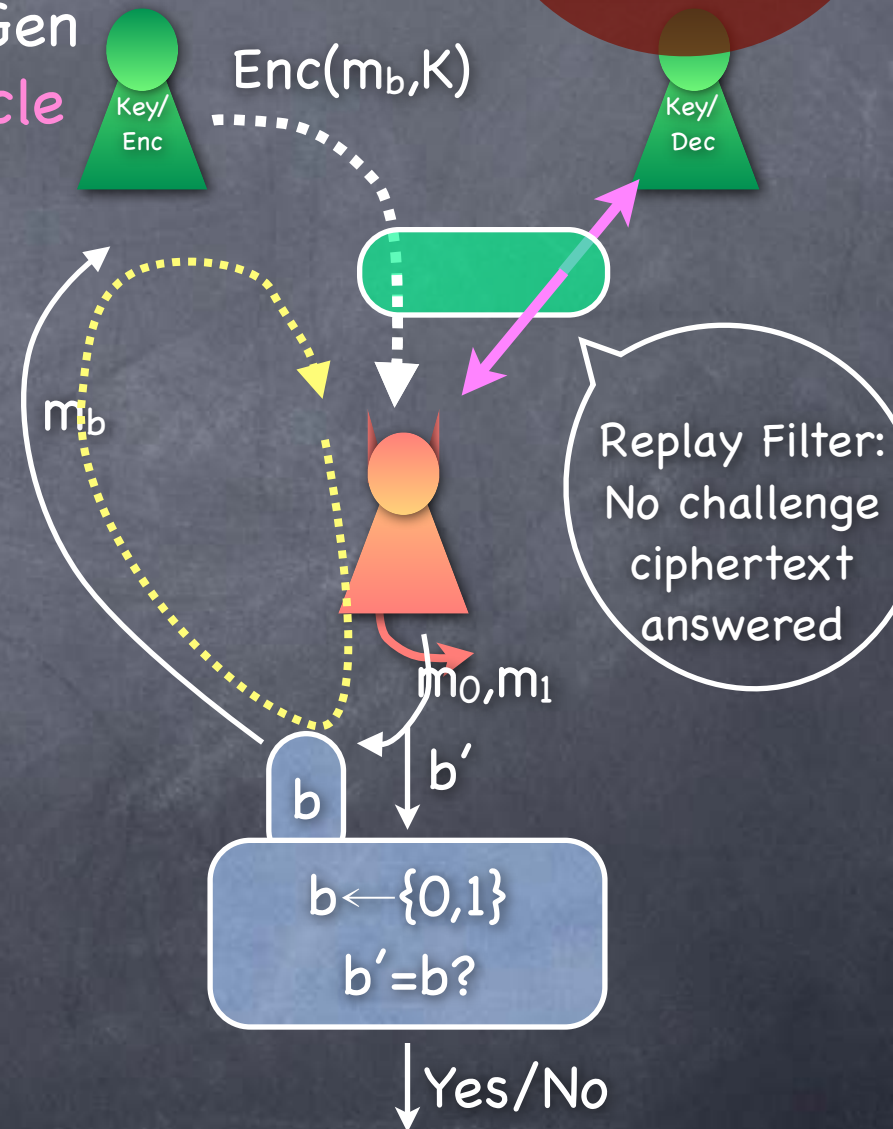
IND-CCA +
~correctness
equivalent to
SIM-CCA

- Experiment picks $b \leftarrow \{0,1\}$ and $K \leftarrow \text{KeyGen}$
Adv gets (guarded) access to Dec_K oracle

For as long as Adversary wants

- Adv sends two messages m_0, m_1 to the experiment
- Expt returns $\text{Enc}(m_b, K)$ to the adversary

- Adversary returns a guess b'
- Experiment outputs 1 iff $b'=b$
- IND-CCA secure if for all feasible adversaries $\Pr[b'=b] \approx 1/2$



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 - **MAC**: Message Authentication Code

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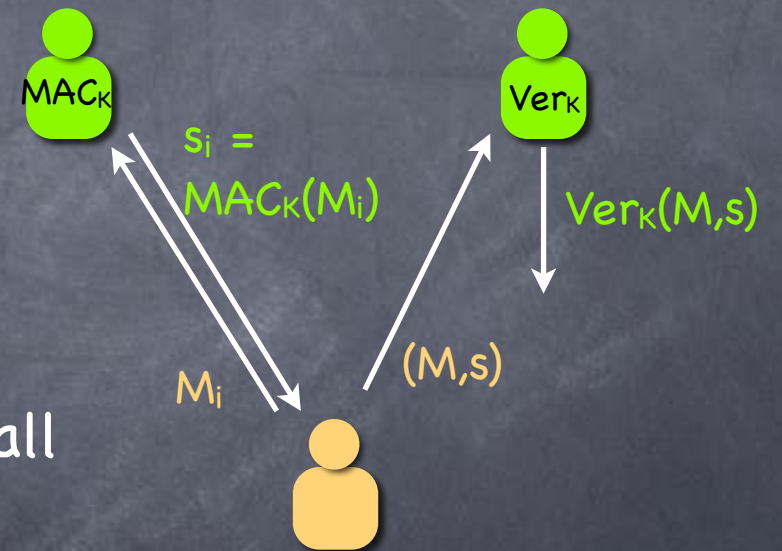
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- A triple (KeyGen, MAC, Verify)
- Correctness: For all K from KeyGen, and all messages M , $\text{Verify}_K(M, \text{MAC}_K(M))=1$
- Security: probability that an adversary can produce (M,s) s.t. $\text{Verify}_K(M,s)=1$ is negligible unless Alice produced an output $s=\text{MAC}_K(M)$



Advantage

$$= \Pr[\text{Ver}_K(M,s)=1 \text{ and } (M,s) \notin \{(M_i,s_i)\}]$$

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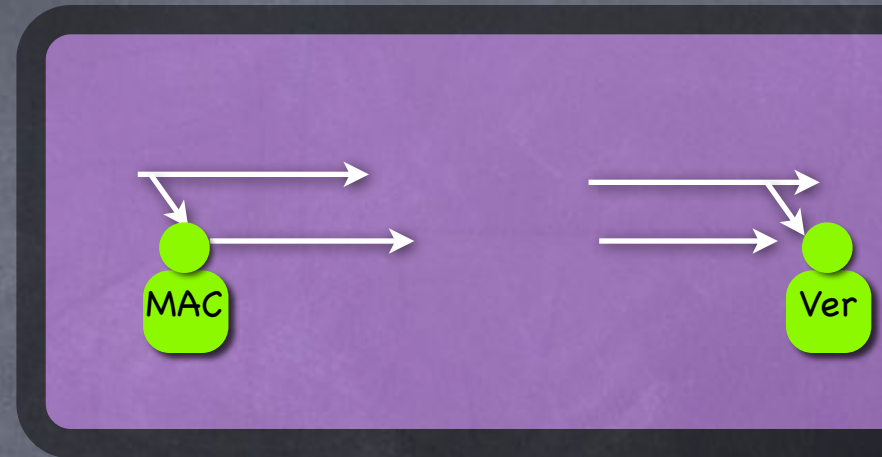
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- In principle, PRFs can be constructed (less efficiently) based on any One-Way Permutation or even any One-Way Function

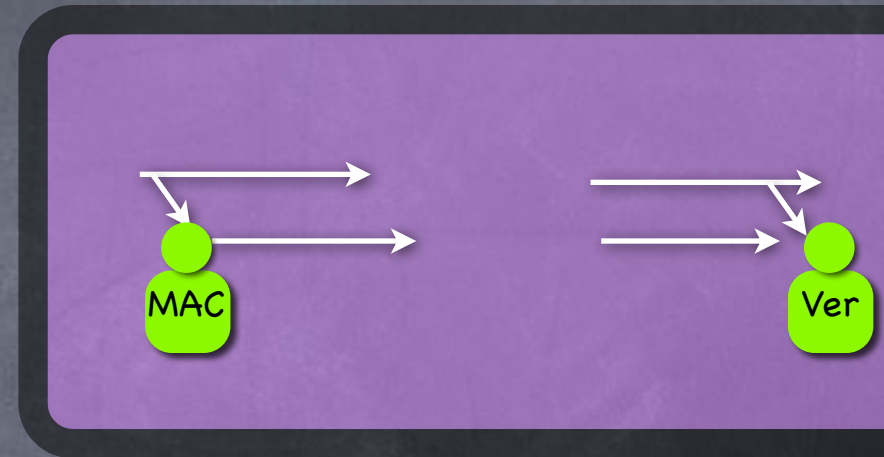
Making a MAC

One-time MAC



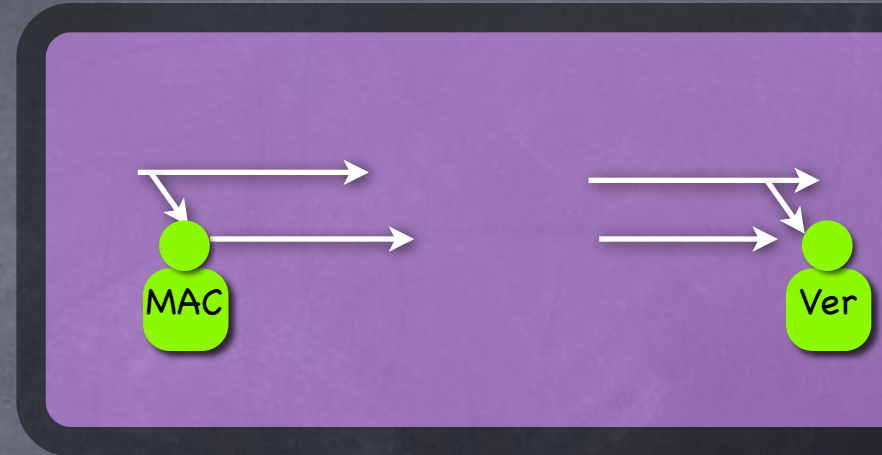
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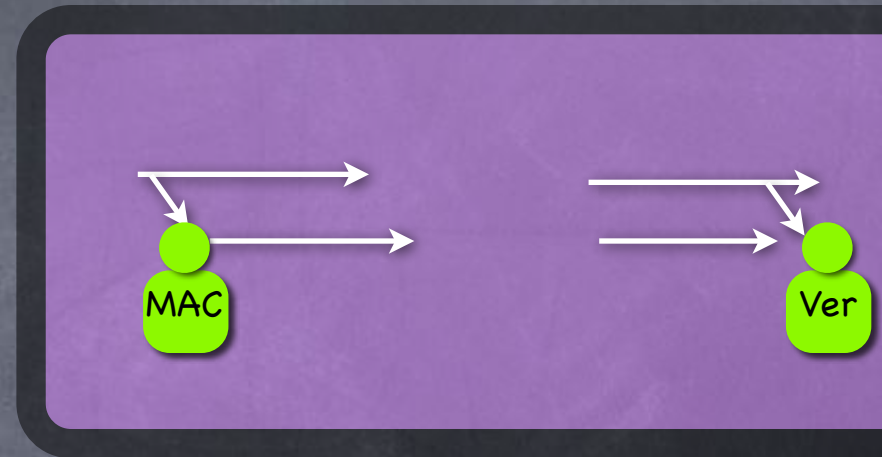
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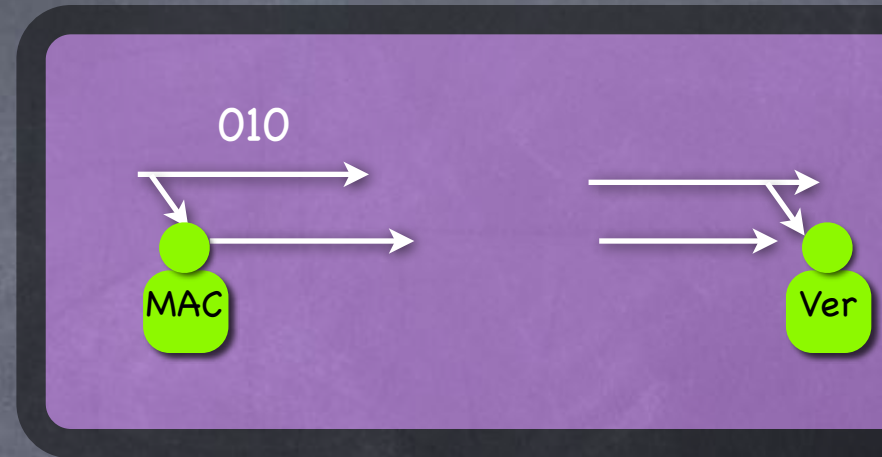
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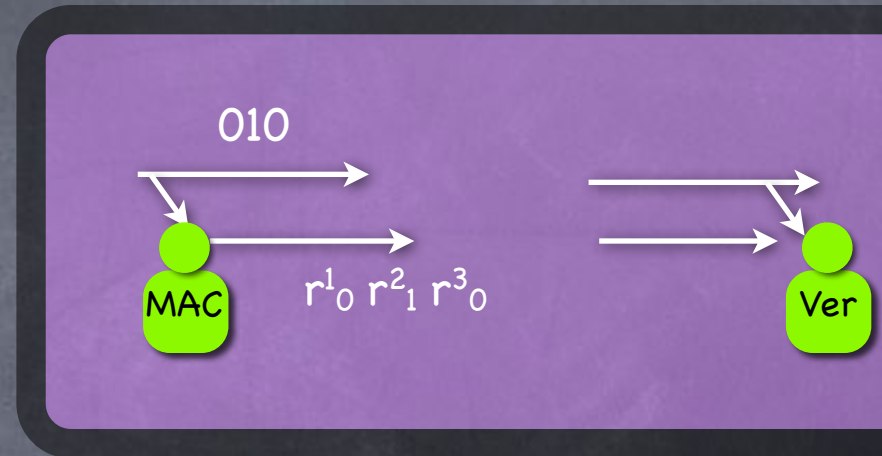
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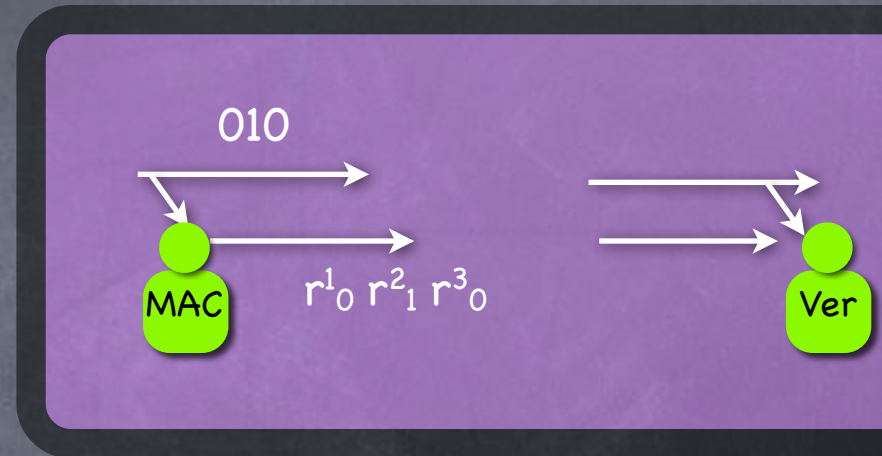
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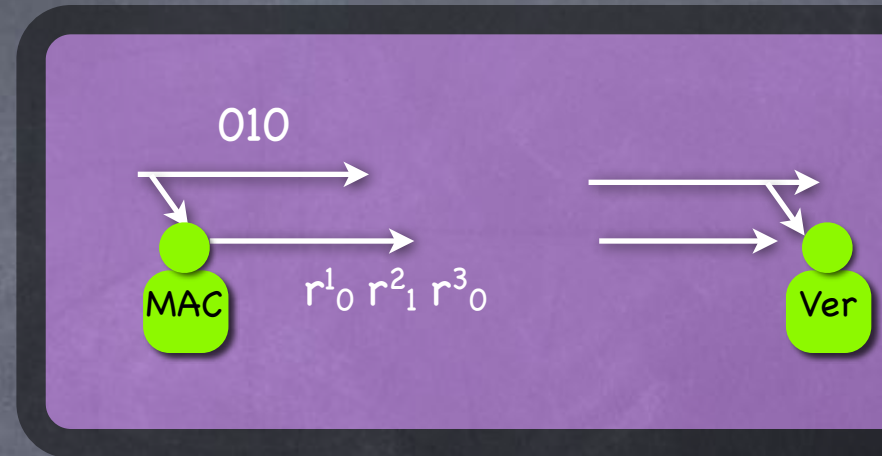
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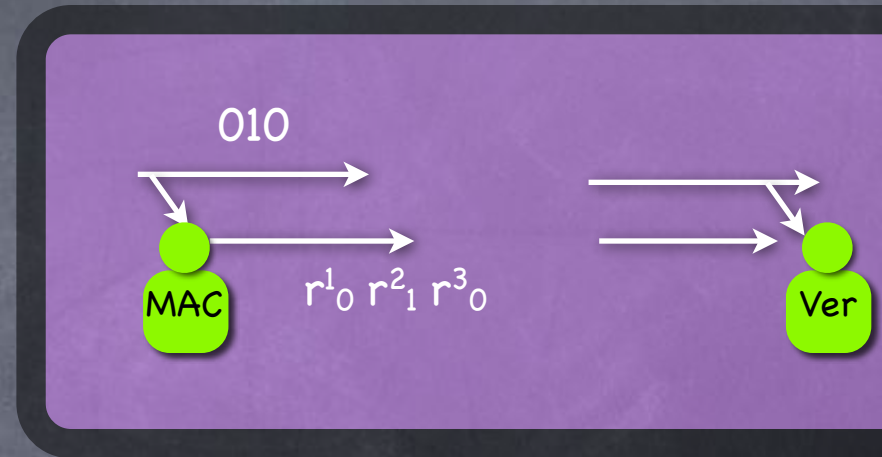


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- More efficient one-time MACs exist (later)

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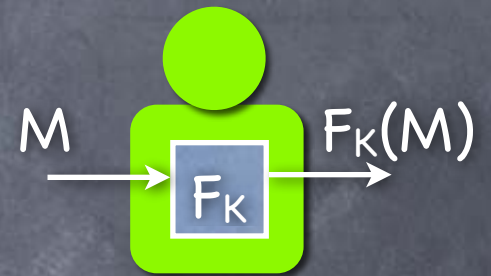
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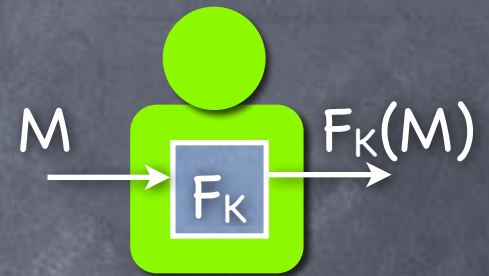
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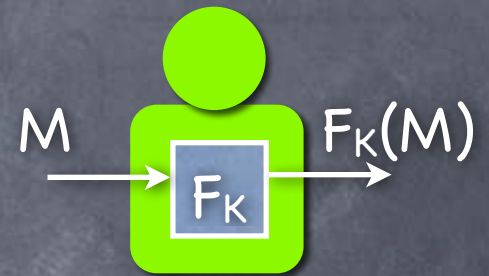
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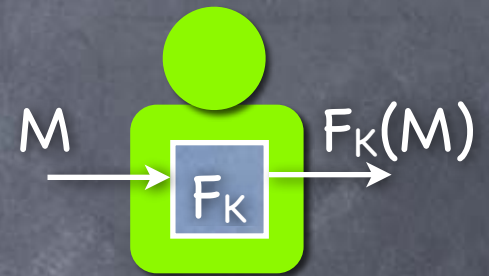
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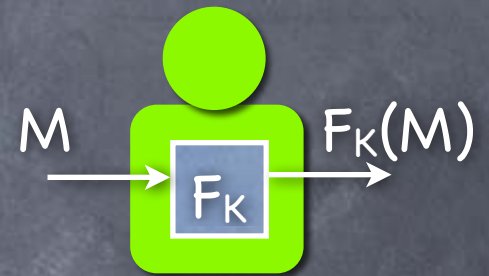
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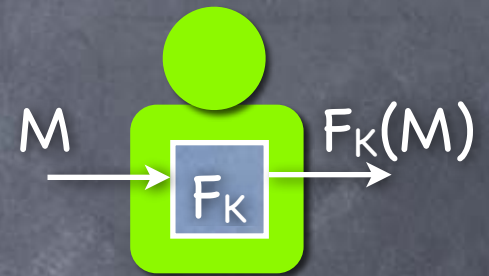
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- If random function R used as MAC, then probability of forgery, $\epsilon_{MAC}^* = 2^{-m(k)}$



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- Can we use a PRF with a fixed block-length (i.e., a block cipher)?

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- Inefficient! Tag length increases with message length

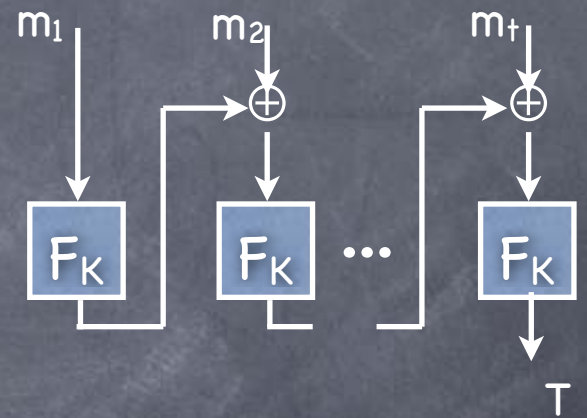
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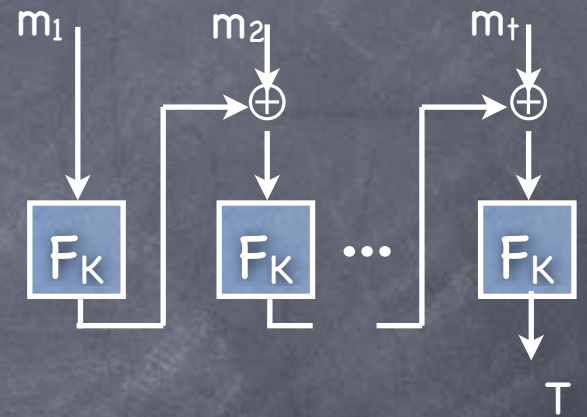
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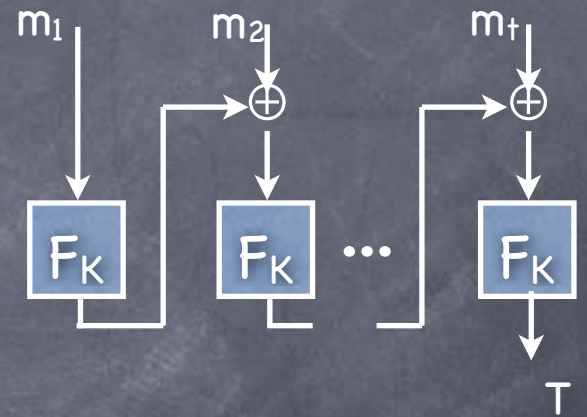
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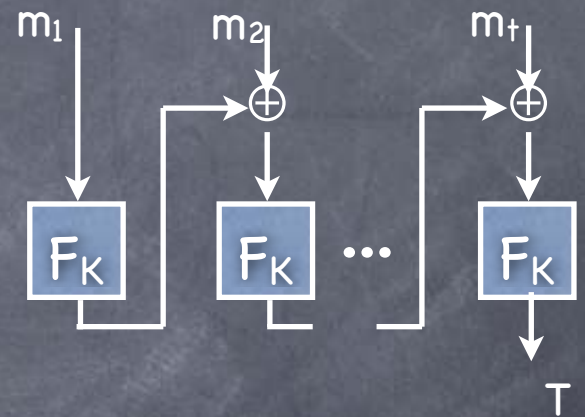
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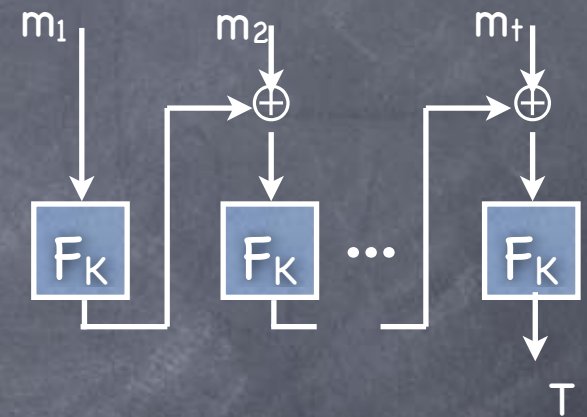
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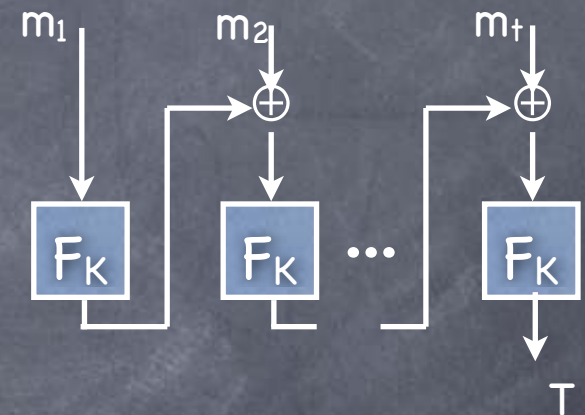
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- Else attacks possible (by extending a previously signed message)



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- **Later**: Hash-based HMAC used in TLS and IPSec ← IETF Standard. 1997

SKE in Practice

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 - But often breaks if used this way
- NIST Standard: For multi-message encryption, use a block-cipher in CTR mode

Also used to denote the random nonce chosen for encryption using a block-cipher

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 - As a PRP (or at least, against key recovery)

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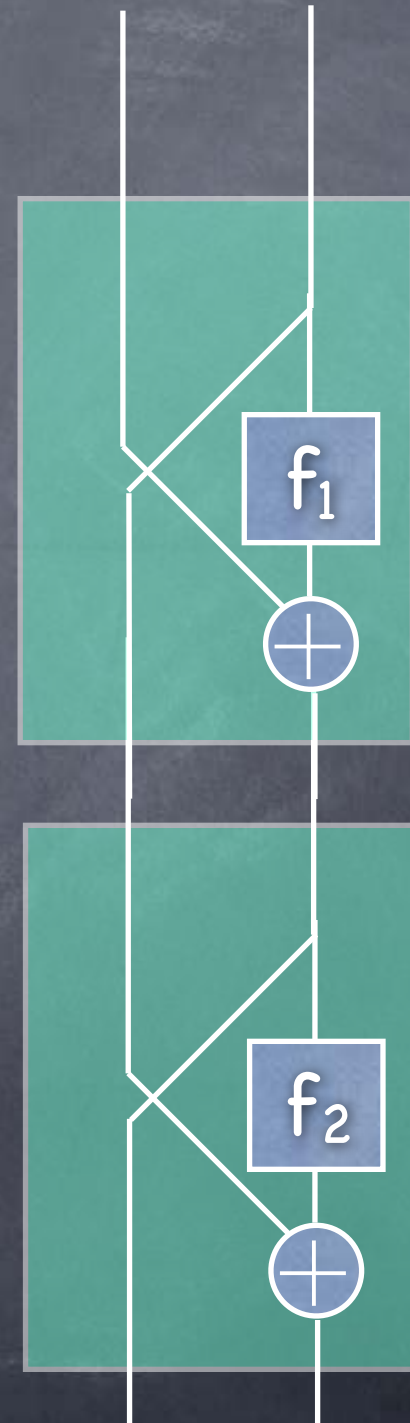
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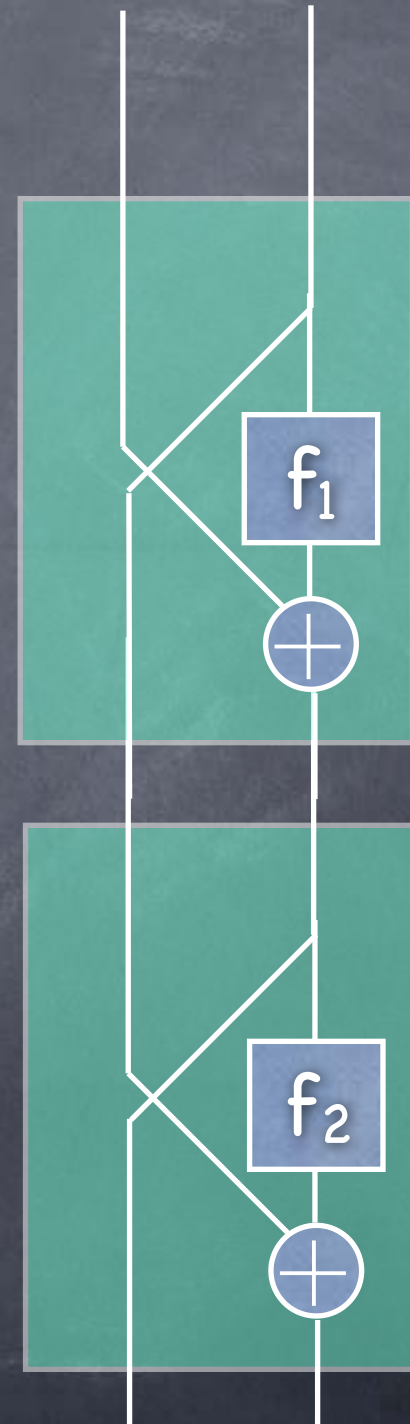
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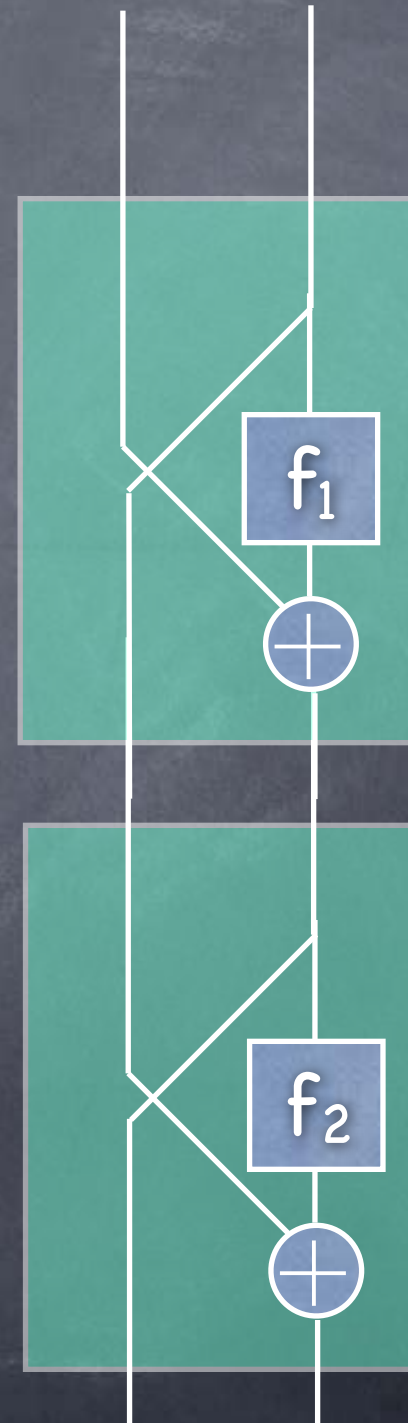
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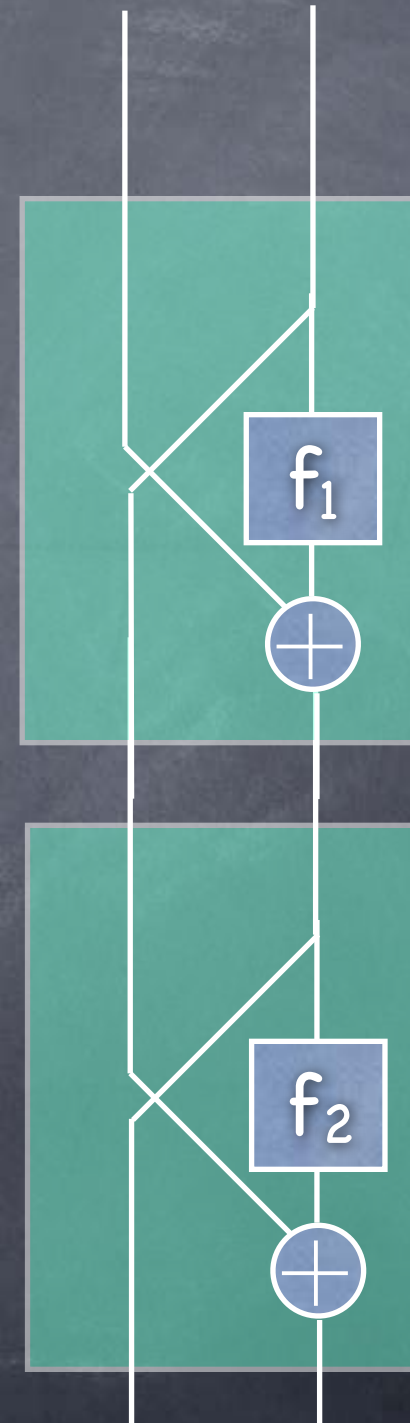
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- Triple DES: 3 successive applications of DES (or DES^{-1}) with 3 keys

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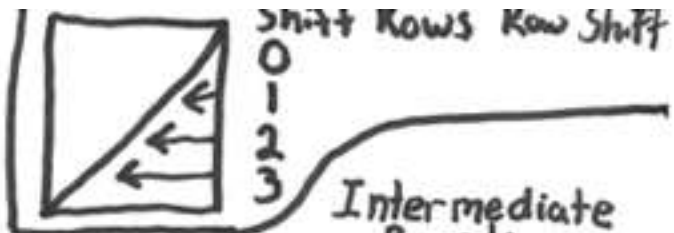
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 - No "simple" hardness assumption known to imply any sort of security for AES



AES Crib Sheet

(Handy for memorizing)



General Math

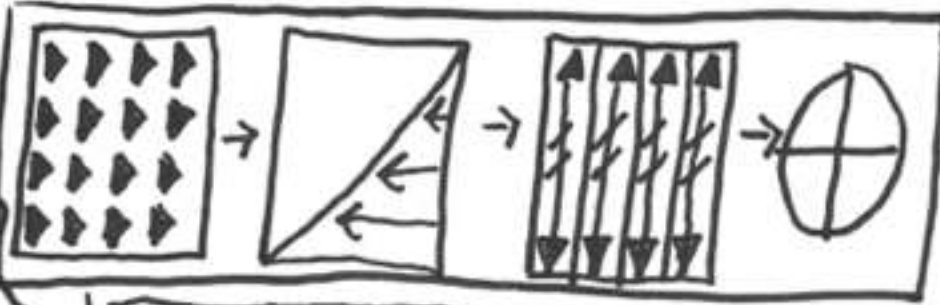
11B = AES Polynomial = $x^8 + x^4 + x^3 + x + 1$

Fast Multiply

$x \cdot a(x) = (a \ll 1) \oplus (a_7 = 1) ? 1B : 00$

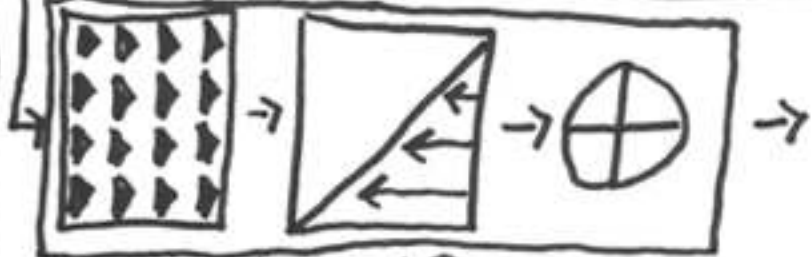
$\log(x \cdot y) = \log(x) + \log(y)$

Use $(x+1) = 03$ for log base



Intermediate Rounds

#	Key
9	128
11	192
13	256



?	?	?	?
?	?	?	?
?	?	?	?
?	?	?	?

Ciphertext

S-Box (SRD)

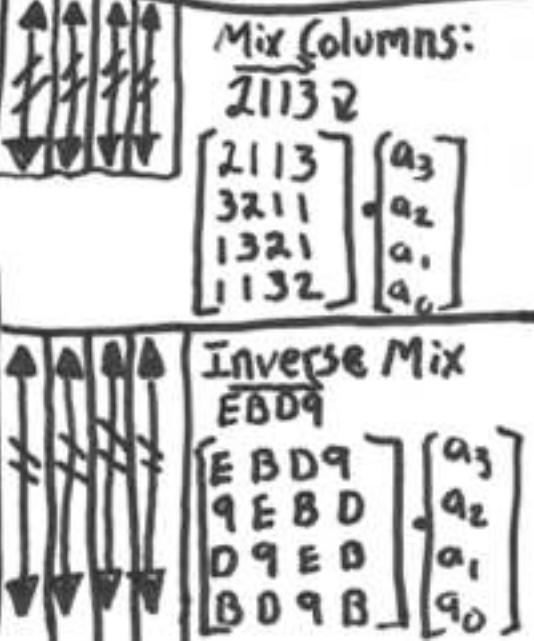
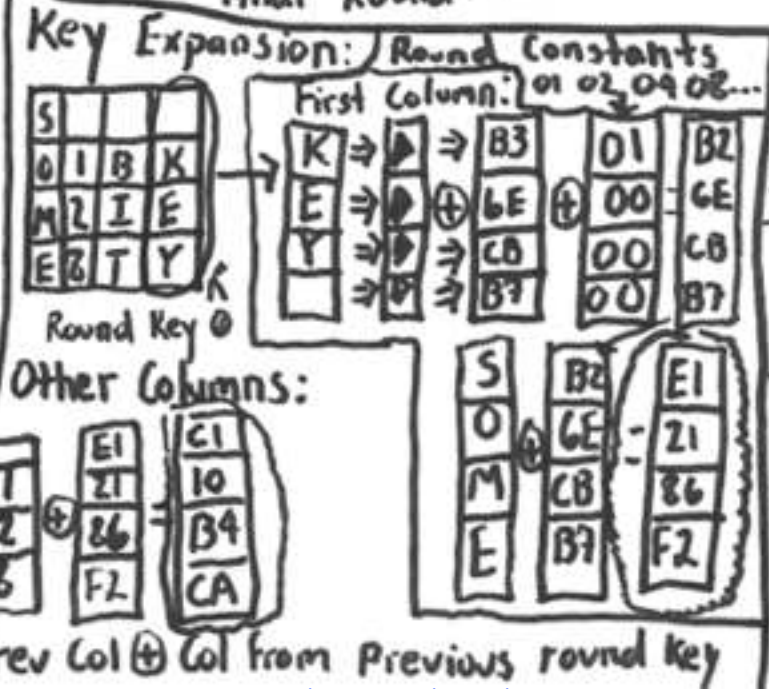
$SRD[a] = f(g(a))$

$g(a) = a^{-1} \text{ mod } m(x)$

Think $5^3 \oplus 6^3$

5 is and 3 0's $[0110\ 0011]^T$

11111000	a_7	⊕	00000001
01111100	a_6		
00111110	a_5		
00011111	a_4		
10001111	a_3		
11000111	a_2		
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 - Meet-in-the-middle, linear cryptanalysis, differential cryptanalysis, impossible differential cryptanalysis, boomerang attack, integral cryptanalysis, cube attack, ...

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 - One pass: IAPM, OCB, ... [patented]
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 - AE with Associated Data: Allows unencrypted (but authenticated) parts of the plaintext, for headers etc.

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 - e.g. RC4 in BitTorrent, Skype, PDF