#### Parallel Numerical Algorithms

Chapter 3 - Parallel Programming

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CS 554 / CSE 512



- Functional languages
- Parallelizing compilers
- Object parallel
- Data parallel
- Shared memory
- Partitioned global address space
- Remote memory access



### **Functional Languages**

- Often implemented using dataflow, in which operations fire whenever their inputs are available, and results then become available as inputs for other operations
- Tend to require substantial extra overhead in work and storage, so have proven difficult to implement efficiently
- Have not been used widely in practice, though numerous experimental functional languages and dataflow systems have been developed



- Automatic or semi-automatic, loop-based approach has been most successful in exploiting modest levels of concurrency on shared-memory systems
- Many challenges remain before effective automatic parallelization of arbitrary serial code can be routinely realized in practice, especially for massively parallel, distributed-memory systems
- Parallelizing compilers can produce efficient "node code" for hybrid architectures with SMP nodes, thereby freeing programmer to focus on exploiting parallelism across nodes



#### **Outline**

- Parallel Programming Paradigms
- MPI Message-Passing Interface
  - MPI Basics
  - Communication and Communicators
  - Virtual Process Topologies
  - Performance Monitoring and Visualization
- OpenMP Portable Shared Memory Programming



- Express what to compute (i.e., mathematical relationships to be satisfied), but not how to compute it or order in which computations are to be performed
- Avoid artificial serialization imposed by imperative programming languages
- · Avoid storage references, side effects, and aliasing that make parallelization difficult
- Permit full exploitation of any parallelism inherent in computation



- Automatically parallelize programs written in conventional sequential programming languages
- Difficult to do for arbitrary serial code
- Compiler can analyze serial loops for potential parallel execution, based on careful dependence analysis of variables occurring in loop
- User may provide hints (directives) to help compiler determine when loops can be parallelized and how
- OpenMP is standard for compiler directives



- Parallelism encapsulated within distributed objects that bind together data and functions operating on data
- Parallel programs built by composing component objects that communicate via well-defined interfaces and protocols
- Implemented using object-oriented programming languages such as C++ or Java
- Often based on standards and supporting environments such as CORBA, DCE, CCA
- Examples include Charm++ and Legion



#### Data Parallel

- Simultaneous operations on elements of data arrays, typified by vector addition
- Low-level programming languages, such as Fortran 77 and C, express array operations element by element in some specified serial order
- Array-based languages, such as APL, Fortran 90, and MATLAB, treat arrays as higher-level objects and thus facilitate full exploitation of array parallelism



- · Classic shared-memory paradigm, originally developed for multitasking operating systems, focuses on control parallelism rather than data parallelism
- Multiple processes share common address space accessible to all, though not necessarily with uniform
- Because shared data can be changed by more than one process, access must be protected from corruption, typically by some mechanism to enforce mutual exclusion
- Shared memory supports common pool of tasks from which processes obtain new work as they complete previous tasks



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#### **Shared Memory**

- Most naturally and efficiently implemented on true shared-memory architectures, such as SMPs
- Can also be implemented with reasonable efficiency on NUMA (nonuniform memory access) shared-memory or even distributed-memory architectures, given sufficient hardware or software support
- With nonuniform access or distributed shared memory. efficiency usually depends critically on maintaining locality in referencing data, so design methodology and programming style often closely resemble techniques for exploiting locality in distributed-memory systems



#### Remote Memory Access

- One-sided, put and get communication to store data in or fetch data from memory of another process
- Does not require explicit cooperation between processes
- Must be used carefully to avoid corruption of shared data
- Included in MPI-2, to be discussed later

#### Data Parallel

- Data parallel languages provide facilities for expressing array operations for parallel execution, and some allow user to specify data decomposition and mapping to processors
- High Performance Fortran (HPF) is most visible attempt to standardize data parallel approach to programming
- Though naturally associated with SIMD architectures, data parallel languages have also been implemented successfully on general MIMD architectures
- Data parallel approach can be effective for highly regular problems, but tends to be too inflexible to be effective for irregular or dynamically changing problems



- - Most popular modern implementation of explicit shared-memory programming, typified by pthreads (POSIX threads)
  - Reduce overhead for context-switching by providing multiple program counters and execution stacks so that extensive program state information need not be saved and restored when switching control quickly among threads
  - Provide detailed, low-level control of shared-memory systems, but tend to be tedious and error prone
  - More suitable for implementing underlying systems software (such as OpenMP and run-time support for parallelizing compilers) than for user-level applications



#### Partitioned Global Address Space

- Partitioned global address space (PGAS) model provides global memory address space that is partitioned across processes, with a portion local to each process
- Enables programming semantics of shared memory while also enabling locality of memory reference that maps well to distributed memory hardware
- Example PGAS programming languages include Chapel, Co-Array Fortran, Titanium, UPC, X-10



- Two-sided, send and receive communication between processes
- Most natural and efficient paradigm for distributed-memory systems
- Can also be implemented efficiently in shared-memory or almost any other parallel architecture, so it is most portable paradigm for parallel programming
- "Assembly language of parallel computing" because of its universality and detailed, low-level control of parallelism
- Fits well with our design philosophy and offers great flexibility in exploiting data locality, tolerating latency, and other performance enhancement techniques





#### Message Passing

- Provides natural synchronization among processes (through blocking receives, for example), so explicit synchronization of memory access is unnecessary
- Facilitates debugging because accidental overwriting of memory is less likely and much easier to detect than with shared-memory
- Sometimes deemed tedious and low-level, but thinking about locality tends to result in programs with good performance, scalability, and portability
- Dominant paradigm for developing portable and scalable applications for massively parallel systems



- Closely matches computational model underlying our design methodology for developing parallel algorithms and provides natural framework for implementing them
- Although motivated by distributed-memory systems, works effectively on almost any type of parallel system
- Often outperforms other paradigms because it enables and encourages attention to data locality



MPI was developed in three major stages, MPI-1 (1994), MPI-2 (1997) and MPI-3 (2012)

Features of MPI-1 include

- point-to-point communication
- collective communication
- process groups and communication domains
- virtual process topologies
- environmental management and inquiry
- profiling interface
- bindings for Fortran and C



- MPI includes bindings for Fortran, C, and C++
- We will emphasize C bindings; Fortran usage is similar
- C versions of most MPI routines return error code as function value, whereas Fortran versions have additional integer argument, IERROR, for this purpose

#### MPI — Message-Passing Interface

- Provides communication among multiple concurrent processes
- Includes several varieties of point-to-point communication, as well as collective communication among groups of processes
- Implemented as library of routines callable from conventional programming languages such as Fortran, C, and C++
- Has been universally adopted by developers and users of parallel systems that rely on message passing



- Includes more than 125 functions, with many different options and protocols
- Small subset suffices for most practical purposes
- We will cover just enough to implement algorithms we will consider
- In some cases, performance can be enhanced by using features that we will not cover in detail



Additional features of MPI-2 include:

- dynamic process management
- input/output
- one-sided operations for remote memory access
- bindings for C++

Additional features of MPI-3 include:

- nonblocking collectives
- new one-sided communication operations
- Fortran 2008 bindings

We will cover very little of MPI-2 or MPI-3, which are not essential for algorithms we will consider



#### **Building and Running MPI Programs**

- Executable module must first be built by compiling user program and linking with MPI library
- One or more header files, such as mpi.h, may be required to provide necessary definitions and declarations
- MPI is generally used in SPMD mode, so only one executable must be built, multiple instances of which are executed concurrently
- Most implementations provide command, typically named mpirun, for spawning MPI processes
  - MPI-2 specifies mpiexec for portability
- User selects number of processes and on which processors they will run

#### Availability of MPI

- Custom versions of MPI supplied by vendors of almost all current parallel computers systems
- Freeware versions available for clusters and similar environments include
  - MPICH: http://www.mpich.org/
  - OpenMPI: http://www.open-mpi.org
- Both websites also provide tutorials on learning and using MPI
- MPI standard (MPI-1, -2, -3) available from MPI Forum http://www.mpi-forum.org



Information necessary to specify message and identify its source or destination in MPI include

- msg: location in memory where message data begins
- count: number of data items contained in message
- datatype: type of data in message
- source or dest: rank of sending or receiving process in communicator
- tag: identifier for specific message or kind of message
- comm: communicator



#### Minimal set of six MPI functions we will need

- int MPI\_Init(int \*argc, char \*\*\*argv);
   Initiates use of MPI
- int MPI\_Finalize(void); Concludes use of MPI
- int MPI\_Comm\_size(MPI\_Comm comm,
  int \*size);

On return,  $\mathtt{size}$  contains number of processes in communicator  $\mathtt{comm}$ 

 A few special MPI routines may be called before MPI\_Init or after MPI\_Finalize



#### Example: MPI Program for 1-D Laplace Example

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Parallel Programming Paradigms MPI — Message-Passing Interface enMP — Portable Shared Memory Programming MPI Basics
Communication and Communicators
Virtual Process Topologies
Performance Monitoring and Visualization

#### Groups and Communicators

- Every MPI process belongs to one or more groups
- Each process is identified by its *rank* within given group
- Rank is integer from zero to one less than size of group (MPI\_PROC\_NULL is rank of no process)
- Initially, all processes belong to MPI\_COMM\_WORLD
- Additional groups can be created by user
- Same process can belong to more than one group
- Viewed as communication domain or context, group of processes is called communicator



- Available MPI data types include
  - C: char, int, float, double
  - Fortran: integer, real, double precision, complex
- Use of MPI data types facilitates heterogeneous environments in which native data types may vary from machine to machine
- Also supports user-defined data types for contiguous or noncontiguous data



• int MPI\_Comm\_rank (MPI\_Comm comm,
 int \*rank);
 On return, rank contains rank of calling process in
 communicator comm, with 0 < rank < size-1</pre>

• int MPI\_Send(void \*msg, int count,
 MPI\_Datatype datatype, int dest, int tag,
 MPI\_Comm comm);

On return, msg can be reused immediately

 int MPI\_Recv(void \*msg, int count, MPI\_Datatype datatype, int source, int tag, MPI\_Comm comm, MPI\_Status \*status);
 On return, msg contains requested message

turn, msg contains requested message

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Parallel Programming Paradigms
MPI Basics
Communication and Communicators

#### Example: MPI Program for 1-D Laplace Example

#### Standard Send and Receive Functions

- Standard send and receive functions are blocking, meaning they do not return until resources specified in argument list can safely be reused
- In particular, MPI\_Recv returns only after receive buffer contains requested message
- MPI\_Send may be initiated before or after matching MPI\_Recv initiated
- Depending on specific implementation of MPI, MPI\_Send may return before or after matching MPI\_Recv initiated



- MPI functions covered thus far suffice to implement almost any parallel algorithm with reasonable efficiency
- Dozens of other MPI functions provide additional convenience, flexibility, robustness, modularity, and potentially improved performance
- But they also introduce substantial complexity that may be difficult to manage
- For example, some facilitate overlapping of communication and computation, but place burden of synchronization on



#### Communication Functions for Various Modes

Mode	Blocking	Nonblocking
standard	MPI_Send	MPI_Isend
buffered	MPI_Bsend	MPI_Ibsend
synchronous	MPI_Ssend	MPI_Issend
ready	MPI_Rsend	MPI_Irsend

- MPI Recv and MPI Irecv are blocking and nonblocking functions for receiving messages, regardless of mode
- MPI\_Buffer\_attach used to provide buffer space for buffered mode

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Parallel Programming Paradigms MPI — Message-Passing Interface OpenMP — Portable Shared Memory Programming	MPI Basics Communication and Communicators Virtual Process Topologies Performance Monitoring and Visualization		
Standard Mode			

- Standard mode does not specify whether messages are buffered
  - Buffering allows more flexible programming, but requires additional time and memory for copying messages to and
  - Given implementation of MPI may or may not use buffering for standard mode, or may use buffering only for messages within certain range of sizes
  - To avoid potential deadlock when using standard mode, portability demands conservative assumptions concerning order in which sends and receives are initiated
  - User can exert explicit control by using buffered or synchronous mode

## Standard Send and Receive Functions

- For same source, tag, and comm, messages are received in order in which they were sent
- Wild card values MPI ANY SOURCE and MPI ANY TAG can be used for source and tag, respectively, in receiving message
- Actual source and tag can be determined from MPI\_SOURCE and MPI\_TAG fields of status structure (entries of status array in Fortran, indexed by parameters of same names) returned by MPI\_Recv



#### Communication modes for sending messages

- buffered mode: send can be initiated whether or not matching receive has been initiated, and send may complete before matching receive is initiated
- synchronous mode: send can be initiated whether or not matching receive has been initiated, but send will complete only after matching receive has been initiated
- ready mode: send can be initiated only if matching receive has already been initiated
- standard mode: may behave like either buffered mode or synchronous mode, depending on specific implementation of MPI and availability of memory for buffer space



- Nonblocking functions include request argument used subsequently to determine whether requested operation has completed
- Nonblocking is different from asynchronous
- MPI\_Wait and MPI\_Test wait or test for completion of nonblocking communication
- MPI\_Probe and MPI\_Iprobe probe for incoming message without actually receiving it
- Information about message determined by probing can be used to decide how to receive it
- MPI\_Cancel cancels outstanding message request, useful for cleanup at end of program or after major phase of computation



- Communication operations that are executed repeatedly with same argument list can be streamlined
  - Persistent communication binds argument list to request, and then request can be used repeatedly to initiate and complete message transmissions without repeating argument list each time
  - Once argument list has been bound using  ${\tt MPI\_Send\_init} \ \ \textbf{or} \ {\tt MPI\_Recv\_init} \ \ \textbf{(or similarly for}$ other modes), then request can subsequently be initiated repeatedly using MPI\_Start

Collective Communication

Communication and Communicators

- MPI\_Bcast
- MPI\_Reduce
- MPI\_Allreduce
- MPI\_Alltoall
- MPI\_Allgather
- MPI\_Scatter
- MPI\_Gather
- MPI Scan
- MPI\_Barrier



#### Virtual Process Topologies

- MPI provides virtual process topologies corresponding to regular Cartesian grids or more general graphs
- Topology is optional additional attribute that can be given to communicator
- Virtual process topology can facilitate some applications, such as 2-D grid topology for matrices or 2-D or 3-D grid topology for discretized PDEs
- Virtual process topology may also help MPI achieve more efficient mapping of processes to given physical network



- MPI\_Topo\_test determines what type of topology, if any, has been defined for given communicator
- Inquiry functions provide information about existing graph topology, such as number of nodes and edges, lists of degrees and edges, number of neighbors of given node, or list of neighbors of given node
- Inquiry functions obtain information about existing Cartesian topology, such as number of dimensions, number of processes for each dimension, and whether each dimension is periodic



#### MPI Profiling Interface

- MPI provides profiling interface via name shift for each function
- For each MPI function with prefix MPI\_, alternative function with prefix PMPI\_ provides identical functionality
- Profiling library can intercept calls to each standard MPI function name, record appropriate data, then call equivalent alternate function to perform requested action
- MPI\_Pcontrol provides profiling control if profiling is in use, but otherwise does nothing, so same code can run with or without profiling, depending on whether executable module is linked with profiling or nonprofiling MPI libraries
- Data collected by profiling can be used for performance analysis or visualization

Communication and Communicators

#### Manipulating Communicators

- MPI\_Comm\_create
- MPI Comm dup
- MPI\_Comm\_split
- MPI\_Comm\_compare
- MPI\_Comm\_free



- MPI\_Dist\_graph\_create creates general graph topology, based on number of nodes, node degrees, and graph edges specified by user
- MPI\_Cart\_create creates Cartesian topology based on number of dimensions, number of processes in each dimension, and whether each dimension is periodic (i.e., wraps around), as specified by user
- Hypercubes are included, since k-dimensional hypercube is simply  $\emph{k}\text{-dimensional}$  torus with two processes per
- MPI\_Cart\_shift provides shift of given displacement along any given dimension of Cartesian topology



- MPI\_Wtime returns elapsed wall-clock time in seconds since some arbitrary point in past
- Elapsed time for program segment given by difference between MPI\_Wtime values at beginning and end
- Process clocks are not necessarily synchronized, so clock values are not necessarily comparable across processes, and care must be taken in determining overall running time for parallel program (see MPI\_WTIME\_IS\_GLOBAL)
- MPI\_Wtick returns resolution of MPI\_Wtime clock



- MPICL is instrumentation package for MPI based on PICL tracing facility and MPI profiling interface http://www.csm.ornl.gov/picl/
- In addition to tracing MPI events, MPICL also provides tracing of user-defined events
- Resulting trace file contains one event record per line, with each event record containing numerical data specifying event type, timestamp, process rank, message length, etc
- Trace data output format is suitable for input to ParaGraph visualization tool



## MPI — Message-Passing Interface

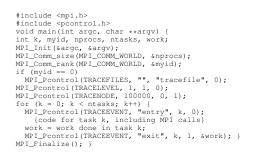
# #include <mpi.h>

Example: MPICL Tracing

## #include <mpi.h> void main(int argc, char \*\*argv) { int k, myid, nprocs, ntasks, work; MPI\_Init(&argc, &argv); MPI\_Comm\_size(MPI\_COMM\_WORLD, &nprocs); MPI\_Comm\_rank(MPI\_COMM\_WORLD, &myid); if (myid == 0) tracefiles("", "tracefile", 0); tracelevel(1, 1, 0); tracelevel(1, 1, 0); traceconde(100000, 0, 1); for (k = 0; k < ntasks; k++) { tracevent("entry", k, 0); {code for task k, including MPI calls} work = work done in task k; tracevent("exit", k, 1, &work); } MPI\_Finalize(); }</pre> MPI Finalize(); }

MPI — Message-Passing Interface

#### Example: MPICL Tracing Using MPI Pcontrol





- Trace data gathered by MPICL during execution of MPI program are replayed pictorially to provide dynamic depiction of behavior of parallel program as well as graphical performance summaries
- Trace file is produced by MPICL in node order, but must be in time order for input to ParaGraph
- Appropriate reordering can be accomplished by following Unix command:

sort +2n -3 +1rn -2 +0rn -1 tracefile.raw > tracefile.trc



#### MPI Performance Analysis Tools

 Jumpshot and SLOG http://www.mcs.anl.gov/perfvis/

 Intel Trace Analyzer (formerly Vampir) http://www.hiperism.com/PALVAMP.htm

IPM: Integrated Performance Monitoring

http://ipm-hpc.sourceforge.net/

 mpiP: Lightweight, Scalable MPI Profiling http://mpip.sourceforge.net/

TAU: Tuning and Analysis Utilities

http://www.cs.uoregon.edu/research/tau/home.php

#### **MPICL Tracing Commands**

- tracefiles (char \*tempfile, char \*permfile, int verbose);
- tracelevel(int mpicl, int user, int trace);
- tracenode (int tracesize, int flush, int sync);
- traceevent (char \*eventtype, int eventid, int nparams, int \*params);



- All MPICL tracing facilities can also be accessed through standard MPI\_Pcontrol function
- Value of level argument to MPI\_Pcontrol determines which MPICL tracing command is invoked, as specified in  $\begin{tabular}{ll} \textbf{header file} & \texttt{pcontrol.h} \\ \end{tabular}$



#### ParaGraph Visualization Tool

ParaGraph is graphical display tool for visualizing behavior and performance of parallel programs that use MPI http: //www.csar.illinois.edu/software/paragraph/

ParaGraph provides graphical answers to questions such as

- Is particular process busy or idle at any given time?
- Which processes are communicating with each other?
- What part of program is executing at any given time?



- Performance data can be viewed from many different visual perspectives to gain insights that might be missed by any single view
- ParaGraph provides about thirty different visual displays, most of which are one of three basic types:
  - processor utilization
  - interprocessor communication
  - user-defined tasks
- Most displays change dynamically to provide graphical animation of program behavior
- ParaGraph is extensible so users can add new displays, specific to given application

#### OpenMP

- Shared memory model, SPMD
- Extends C and Fortran with directives (annotations) and functions
- Relies on programmer to provide information that may be difficult for compiler to determine
- No concurrency except when directed; typically, most lines of code run on single processor/core
- Parallel loops described with directives

```
#pragma omp parallel for default(none) shared() private()
!SOMP PARALLEL DO DEFAULT (NONE) SHARED() PRIVATE()
  do i=1, n
!$OMP END PARALLEL DO
```

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OpenMP — Portable Shared Memory Programming

#### Race Conditions

#### Example:

```
sum = 0.0;
agma omp parallel for private(i)
for (i=0; i<n; i++) { sum += u[i]; }
```

Race condition: result of updates to sum depend on which thread wins race in performing store to memory

OpenMP provides reduction clause for this case:

```
sum = 0.0;
#pragma omp parallel for reduction(+:sum) private(i)
for (i=0; i<n; i++) { sum += u[i]; }</pre>
```

Not hypothetical example: on one dual-processor system, first loop computes wrong result roughly half of time



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MPI — Message-Passing Interface OpenMP — Portable Shared Memory Programming

#### More OpenMP

- omp\_get\_thread\_num() returns number of active threads within parallel region
- omp\_get\_num\_procs() returns number of available cores

General parallel blocks of code (excuted by all available threads) described as

```
#pragma omp parallel
!SOMP PARALLEL
!$OMP END PARALLEL
```



OpenMP — Portable Shared Memory Programming

#### Example: OpenMP Program for 1-D Laplace Example

```
#include <omp.h>
int main(int argc, char **argv) {
  int k, i, nit=10;
  float alpha = 1.0, beta = 2.0;
  float u0[MAX_U], u1[MAX_U];
  float * restrict u0p=u0, * restrict u1p=u1, *tmp;
tmp = ulp; ulp = u0p; u0p = tmp; /* swap pointers */
```

OpenMP — Portable Shared Memory Programming

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