## Image and Region Categorization

Computer Vision
CS 543 / ECE 549
University of Illinois

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#### Last classes

Object instance recognition: localizing an object instance in an image

 Face recognition: matching one face image to another

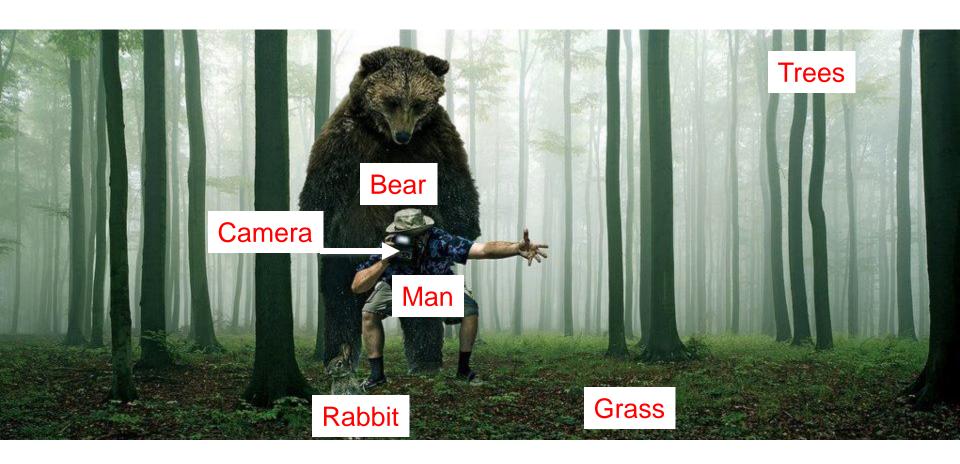
Today: mapping images and regions to categories

# Today's class: image and region categorization

- Overview of image and region categorization
  - Task description
  - What is a category

- Representation
  - Image histograms
  - Bag of Word model
  - Region categorization
- Classifiers

# What do you see in this image

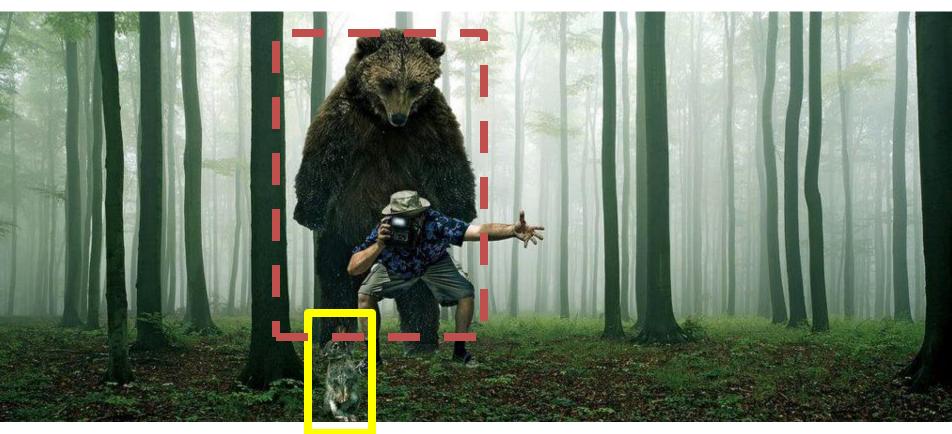


#### **Forest**

# Why do we care about categories?

From an object's category, we can make predictions about its behavior in the future, beyond of what is immediately perceived.

# describe, predict, or interact with the object based on visual cues



Is it dangerous?

How fast does it run?

Is it alive?

Does it have a tail?

Is it **soft**?

Can I poke with it?

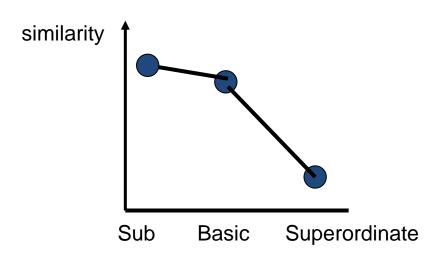
## Rosch's (1976) Levels of Categorization

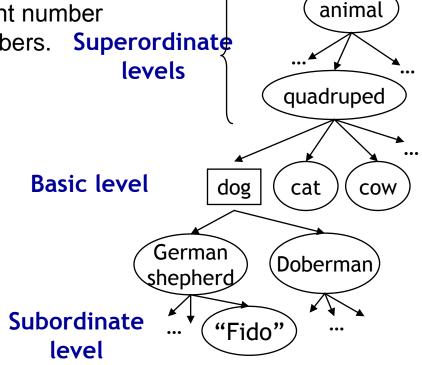
#### **Definition of Basic Level:**

• **Similar shape**: Basic level categories are the highest-level category for which their members have similar shapes.

• Similar motor interactions: ... for which people interact with its members using similar motor sequences.

Common attributes: ... there are a significant number of attributes in common between pairs of members. Superordinate levels





## Levels of Categorization

- Rosch et al found that
  - People can tell whether an object belongs to a basic-level category faster

People tend to predict the basic category (e.g., "dog") before superordinate ("animal") or subordinate ("golden retriever") categorie

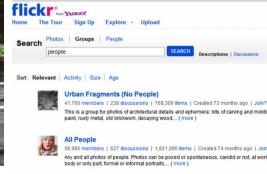
#### Visual categorization

- Given a small number of training images of a category, recognize a-priori unknown instances of that category and assign the correct category label.
- Many different ways to categorize









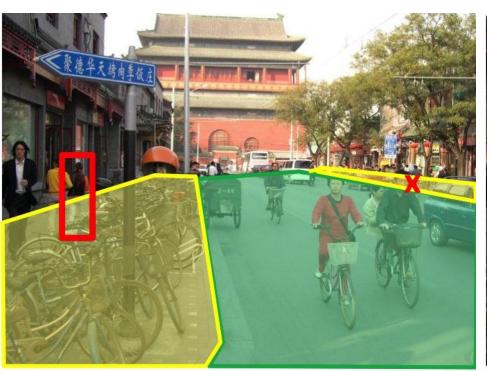
#### Region categorization

- Categorize each image regions
- Image parsing
- Semantic scene labeling



Source: Fei-Fei Li, Rob Fergus, Antonio Torralba.

#### Inference about the scene





#### Image categorization



12,184,113 images, 17624 synsets indexed

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#### Region categorization



#### Categorization in computer vision













































- In class variation
- Similar looking categories
- Size variation
- Background clutter
- Occlusion

















































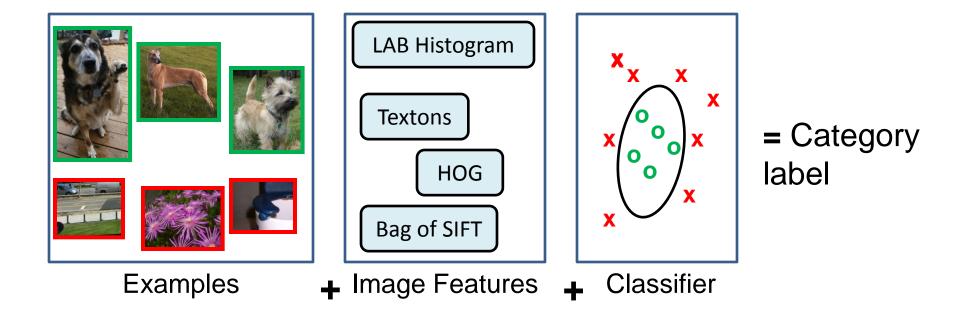




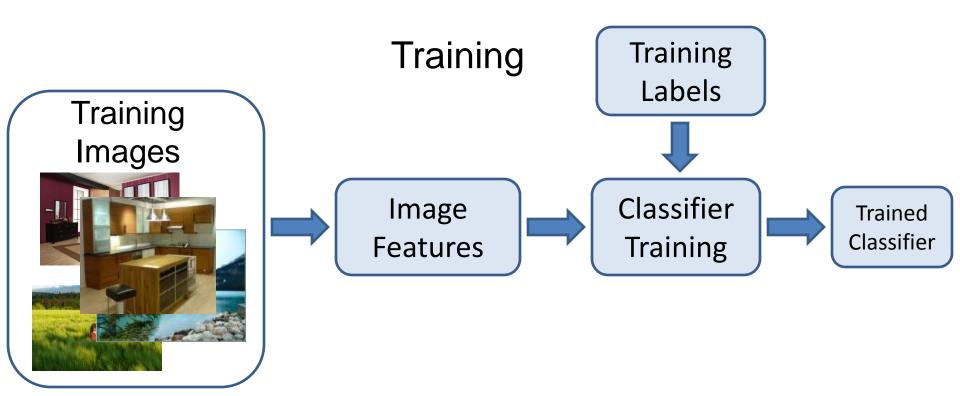




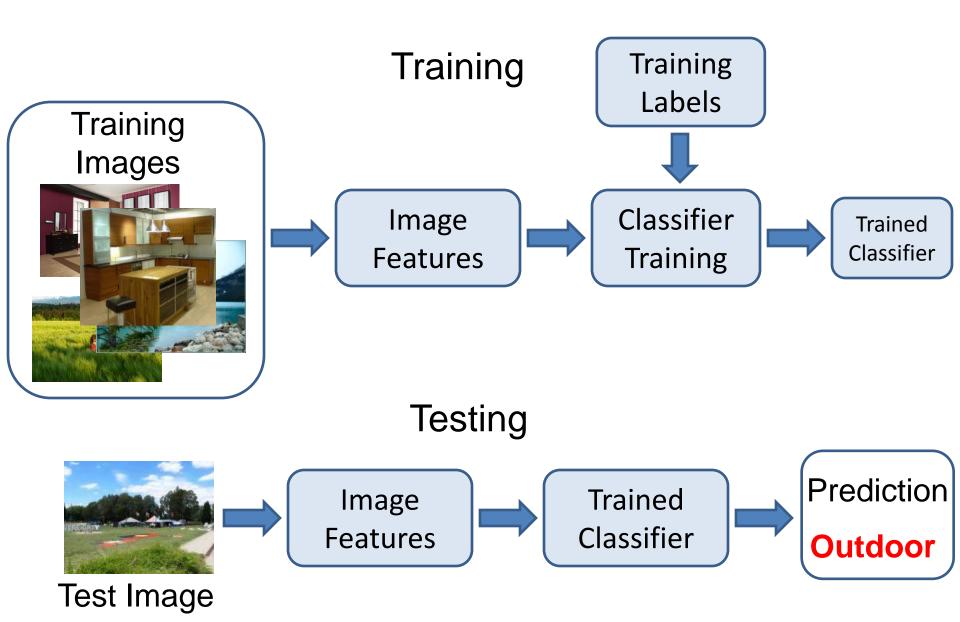
# Supervised learning



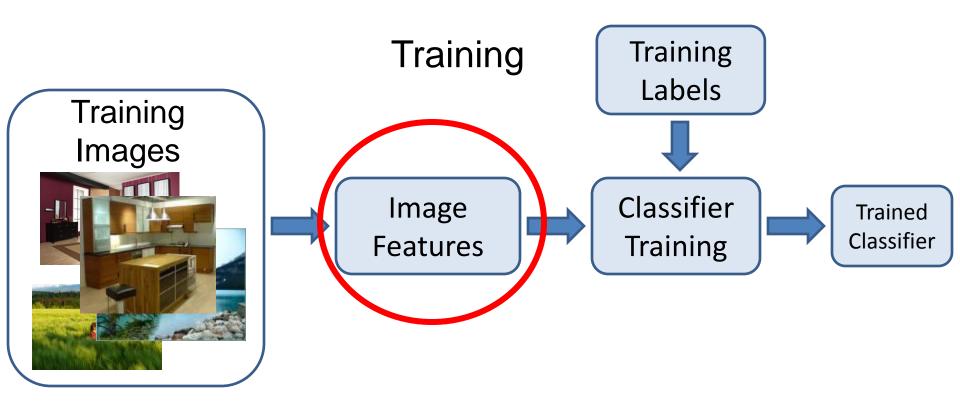
# Training phase



## Testing phase



## Part I: Image features



# Right features depend on what you want to know

- Object: 2D shape
  - Local shape info, shading, shadows, texture
- Scene : overall layout
  - linear perspective, gradients
- Material properties: albedo, feel, hardness, ...
  - Color, texture
- Motion
  - Optical flow, tracked points

### General Principles of Representation

#### Coverage

Ensure that all relevant info is captured



#### Concision

Minimize number of features without sacrificing coverage

#### Directness

Ideal features are independently useful for prediction

### Image representations

- Templates
  - Intensity, gradients, etc.

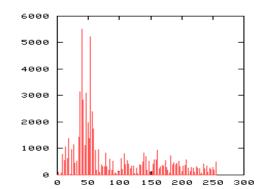






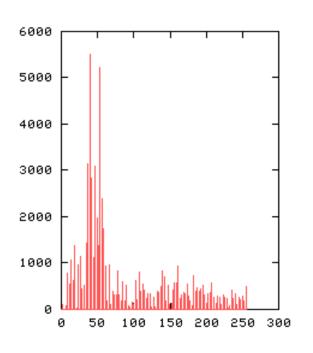
Gradient template

- Histograms
  - Color, texture, SIFT descriptors, etc.



Average of features

#### Image Representations: Histograms



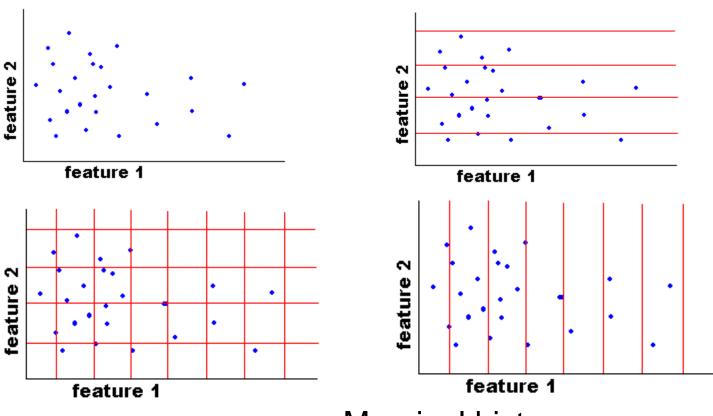


#### Global histogram

- Represent distribution of features
  - Color, texture, depth, ...

### Image Representations: Histograms

Histogram: Probability or count of data in each bin



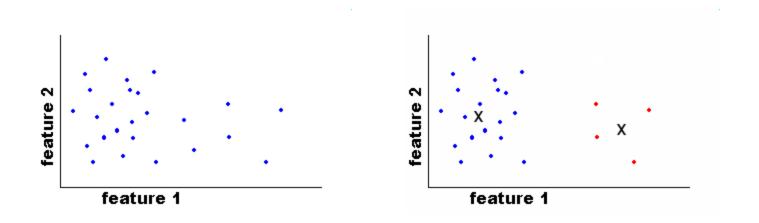
- Joint histogram
  - Requires lots of data
  - Loss of resolution to avoid empty bins

#### Marginal histogram

- Requires independent features
- More data/bin than joint histogram

#### Image Representations: Histograms

#### Clustering



Use the same cluster centers for all images

### Computing histogram distance

$$histint(h_i, h_j) = 1 - \sum_{m=1}^{K} \min(h_i(m), h_j(m))$$

Histogram intersection (assuming normalized histograms)

$$\chi^{2}(h_{i}, h_{j}) = \frac{1}{2} \sum_{m=1}^{K} \frac{\left[h_{i}(m) - h_{j}(m)\right]^{2}}{h_{i}(m) + h_{j}(m)}$$

Chi-squared Histogram matching distance



Cars found by color histogram matching using chi-squared

#### Histograms: Implementation issues

- Quantization
  - Grids: fast but applicable only with few dimensions
  - Clustering: slower but can quantize data in higher dimensions

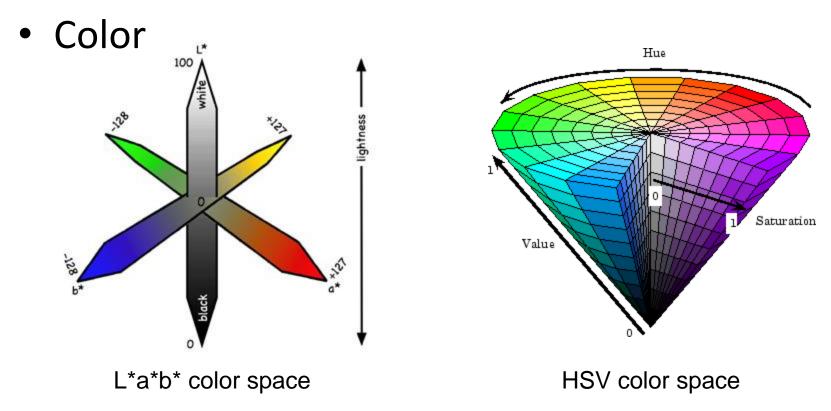


Many Bins
Need more data
Finer representation

#### Matching

- Histogram intersection or Euclidean may be faster
- Chi-squared often works better
- Earth mover's distance is good for when nearby bins represent similar values

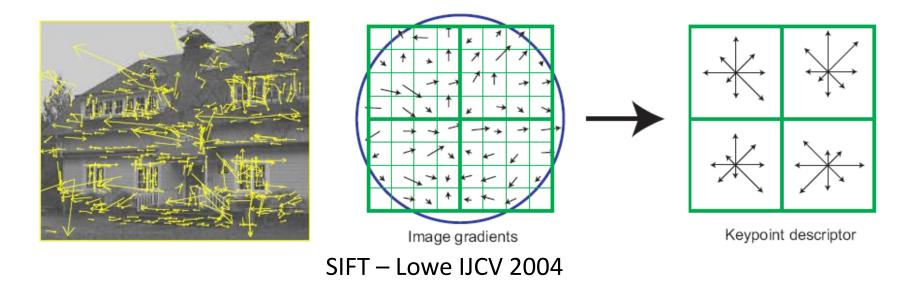
# What kind of things do we compute histograms of?



Texture (filter banks or HOG over regions)

# What kind of things do we compute histograms of?

Histograms of descriptors



"Bag of words"

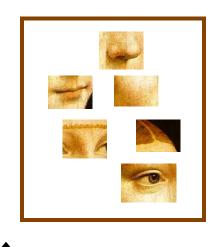
#### **Analogy to documents**

Of all the sensory impressions proceeding to the brain, the visual experiences are the dominant ones. Our perception of the world around us is based essentially on the messages that r For a long tig sensory, brain, image wa centers i visual, perception, movie s etinal, cerebral cortex, image discove eye, cell, optical know th nerve, image perceptic more com Hubel, Wiesel following the to the various de ortex. Hubel and Wiesel nademonstrate that the message about image falling on the retina undergoes wise analysis in a system of nerve cell. stored in columns. In this system each d has its specific function and is responsible a specific detail in the pattern of the retinal image.

China is forecasting a trade surplus of \$90bn (£51bn) to \$100bn this year, a threefold increase on 2004's \$32bn. The Commerce Ministry said the surplus would be created by a predicted 30% compared w China, trade, \$660bn. T annoy the surplus, commerce, China's exports, imports, US, deliber agrees vuan, bank, domestic, yuan is foreign, increase, governo trade, value also need demand so country. China yuan against the don. permitted it to trade within a narrow the US wants the yuan to be allowed freely. However, Beijing has made it ch it will take its time and tread carefully be allowing the yuan to rise further in value.

## Bag of visual words

Image patches

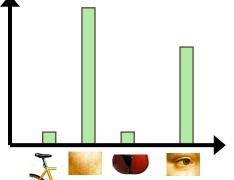


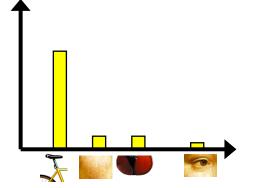


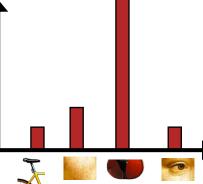






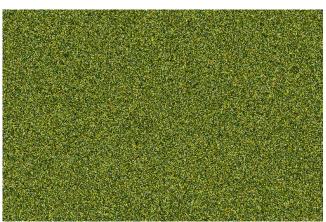


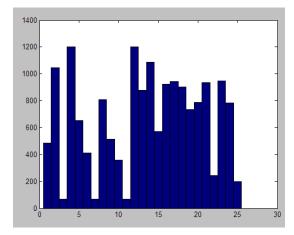




## But what about layout?



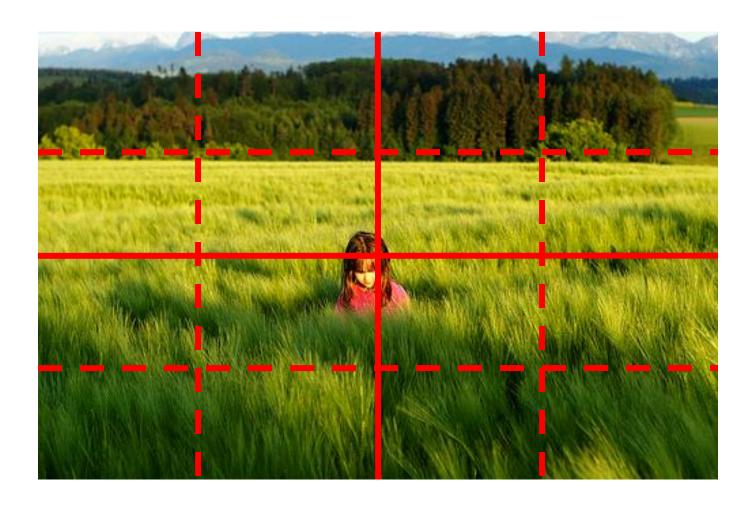






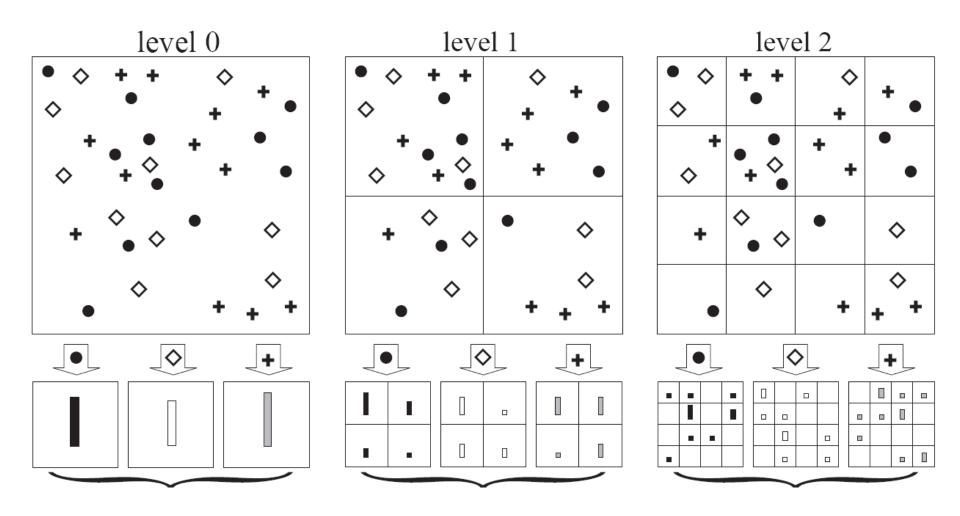
All of these images have the same color histogram

# Spatial pyramid



Compute histogram in each spatial bin

# Spatial pyramid



High number of features – PCA to reduce dimensionality

### Image Categorization: Bag of Words

#### Training

- 1. Extract keypoints and descriptors for all training images
- 2. Cluster descriptors
- 3. Quantize descriptors using cluster centers to get "visual words"
- 4. Represent each image by normalized counts of "visual words"
- 5. Train classifier on labeled examples using histogram values as features

#### Testing

- 1. Extract keypoints/descriptors and quantize into visual words
- 2. Compute visual word histogram
- 3. Compute label or confidence using classifier

#### Often used features

Scene: GIST, Spatial pyramid BoW, color

Object: Spatial pyramid BoW, HOG, color

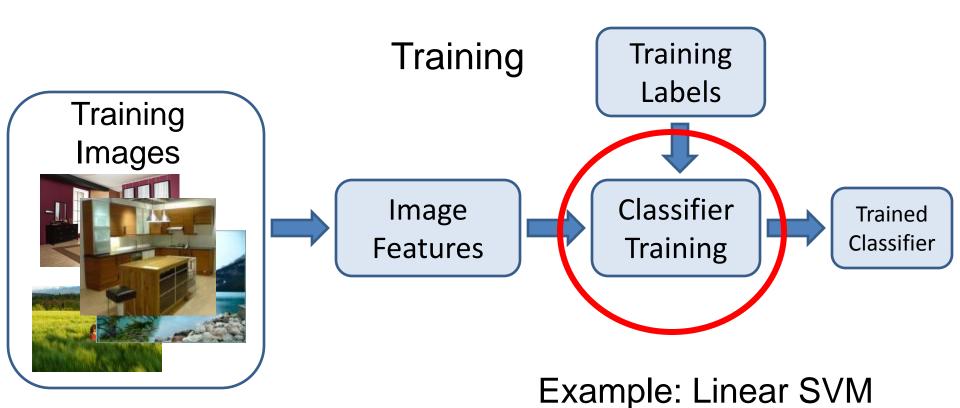
Material: texture, color

#### Things to remember about representation

 Most features can be thought of as templates, histograms (counts), or combinations

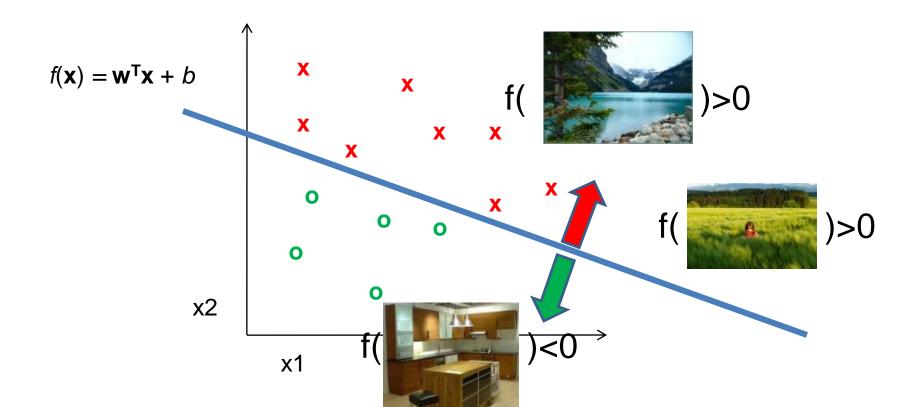
- Think about the right features for the problem
  - Coverage
  - Concision
  - Directness

#### Part 2: Classifiers



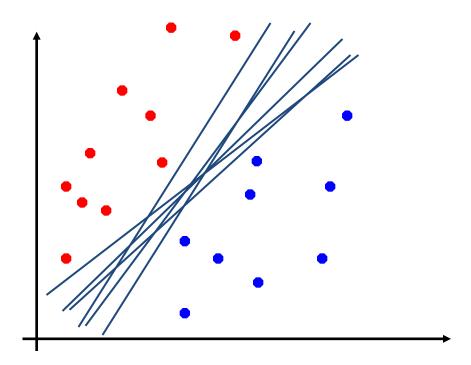
#### Linear classifier

Finding the linear hyperplane that separate examples of different categories



#### **Linear Separators**

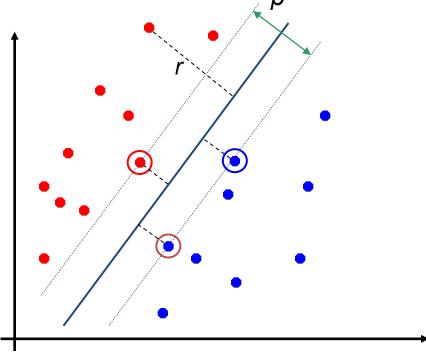
Which of the linear separators is optimal?



#### Classification Margin

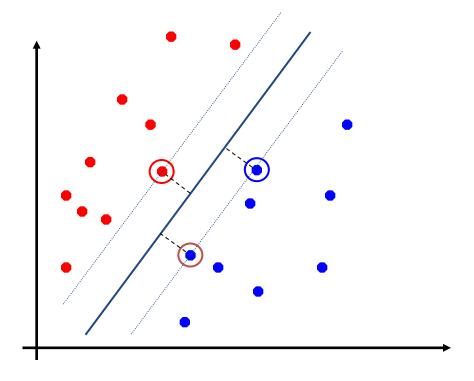
- Distance from example  $\mathbf{x}_i$  to the separator is  $r = \frac{\mathbf{w}^T \mathbf{x}_i + b}{\|\mathbf{w}\|}$
- Examples closest to the hyperplane are support vectors.

• Margin  $\rho$  of the separator is the distance between support vectors.



# Maximum Margin Classification

 Implies that only support vectors matter; other training examples are ignorable.



## Linear SVM Mathematically

• Let training set  $\{(\mathbf{x}_i, y_i)\}_{i=1..n}$ ,  $\mathbf{x}_i \in \mathbb{R}^d$ ,  $y_i \in \{-1, 1\}$  be separated by a hyperplane with margin  $\rho$ . Then for each training example  $(\mathbf{x}_i, y_i)$ :

$$\mathbf{w}^{\mathsf{T}}\mathbf{x}_{i} + b \le -\rho/2$$
 if  $y_{i} = -1$   
 $\mathbf{w}^{\mathsf{T}}\mathbf{x}_{i} + b \ge \rho/2$  if  $y_{i} = 1$   $\iff$   $y_{i}(\mathbf{w}^{\mathsf{T}}\mathbf{x}_{i} + b) \ge \rho/2$ 

- For every support vector  $\mathbf{x}_s$  the above inequality is an equality. After rescaling  $\mathbf{w}$  and b by  $\rho/2$  in the equality, we obtain that distance between each  $\mathbf{x}_s$  and the hyperplane is  $r = \frac{\mathbf{y}_s(\mathbf{w}^T\mathbf{x}_s + b)}{\|\mathbf{w}\|} = \frac{1}{\|\mathbf{w}\|}$
- Then the margin can be expressed through (rescaled) w and b as:

$$\rho = 2r = \frac{2}{\|\mathbf{w}\|}$$

# Solving the Optimization Problem

Quadratic programming with linear constraints

minimize 
$$\frac{1}{2} \|\mathbf{w}\|^2$$

s.t. 
$$y_i(\mathbf{w}^T\mathbf{x}_i + b)$$
 3 1

Lagrangian Function



minimize 
$$L_p(\mathbf{w}, b, \alpha_i) = \frac{1}{2} ||\mathbf{w}||^2 - \sum_{i=1}^n \alpha_i (y_i(\mathbf{w}^T \mathbf{x}_i + b) - 1)$$

s.t. 
$$\alpha_i \ge 0$$

# Solving the Optimization Problem

minimize 
$$L_p(\mathbf{w}, b, \alpha_i) = \frac{1}{2} \|\mathbf{w}\|^2 - \sum_{i=1}^n \alpha_i \left( y_i (\mathbf{w}^T \mathbf{x}_i + b) - 1 \right)$$
  
s.t.  $\alpha_i \ge 0$ 

$$\frac{\partial L_p}{\partial \mathbf{w}} = 0 \qquad \mathbf{w} = \sum_{i=1}^n \alpha_i y_i \mathbf{x}_i$$

$$\frac{\partial L_p}{\partial b} = 0 \qquad \sum_{i=1}^n \alpha_i y_i = 0$$

## Solving the Optimization Problem

minimize 
$$L_p(\mathbf{w}, b, \alpha_i) = \frac{1}{2} \|\mathbf{w}\|^2 - \sum_{i=1}^n \alpha_i \left( y_i(\mathbf{w}^T \mathbf{x}_i + b) - 1 \right)$$

s.t. 
$$\alpha_i \ge 0$$

Lagrangian Dual Problem

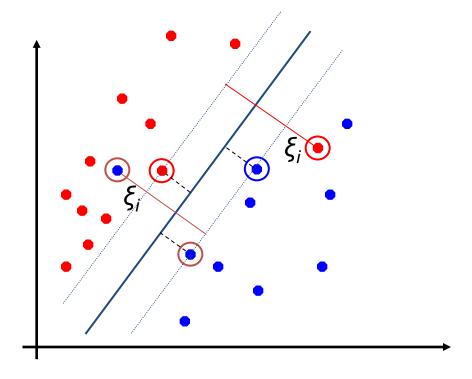


maximize 
$$\sum_{i=1}^{n} \alpha_i - \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_i \alpha_j y_i y_j \mathbf{x}_i^T \mathbf{x}_j$$

s.t. 
$$\alpha_i \ge 0$$
 , and  $\sum_{i=1}^n \alpha_i y_i = 0$ 

#### Soft Margin Classification

- What if the training set is not linearly separable?
- Slack variables  $\xi_i$  can be added to allow misclassification of difficult or noisy examples, resulting margin called *soft*.



## Large Margin Linear Classifier

Formulation:

minimize 
$$\frac{1}{2} \|\mathbf{w}\|^2 + C \sum_{i=1}^n \xi_i$$

such that

$$y_i(\mathbf{w}^T \mathbf{x}_i + b) \ge 1 - \xi_i$$
$$\xi_i \ge 0$$

Parameter C is a trade off factor

## Large Margin Linear Classifier

Formulation: (Lagrangian Dual Problem)

maximize 
$$\sum_{i=1}^{n} \alpha_i - \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_i \alpha_j y_i y_j \mathbf{x}_i^T \mathbf{x}_j$$

such that

$$0 \le \alpha_i \le C$$

$$\sum_{i=1}^{n} \alpha_i y_i = 0$$

#### Linear SVMs: Recap

- The classifier is a separating hyperplane.
- Most "important" training points are support vectors; they define the hyperplane.
- Quadratic optimization algorithms can identify which training points  $\mathbf{x}_i$  are support vectors with non-zero Lagrangian multipliers  $\alpha_i$ .

# Multiclass classification (one vs all)

- Learning a function for each category:  $f_i(x)$ 
  - y=1: for examples in this category
  - y=-1: for examples not in this category
- Finding the class with the largest function value

$$c = \operatorname{arg\,max}_c f_c(x)$$

#### Measuring classification performance

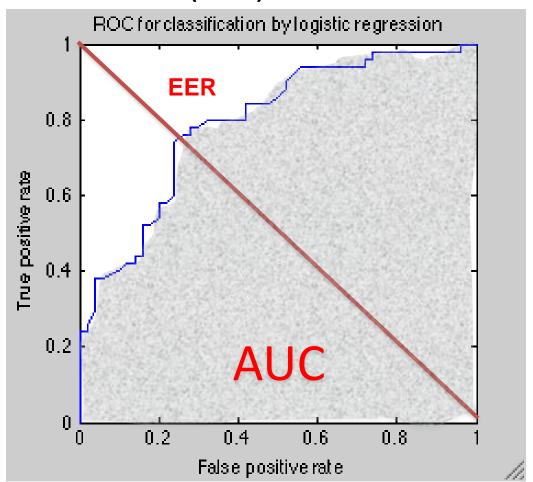
- Confusion matrix
- Accuracy
  - (TP+TN)/
     (TP+TN+FP+FN)
- True Positive Rate=Recall
  - TP/(TP+FN)
- False Positive Rate
  - FP/(FP+TN)
- Precision
  - TP/(TP+FP)
- F1 Score
  - 2\*Recall\*Precision/ (Recall+Precision)

		Predicted	
		Positive	Negative
Actual	Positive	True Positive	False Negative
	Negative	False Positive	True Negative

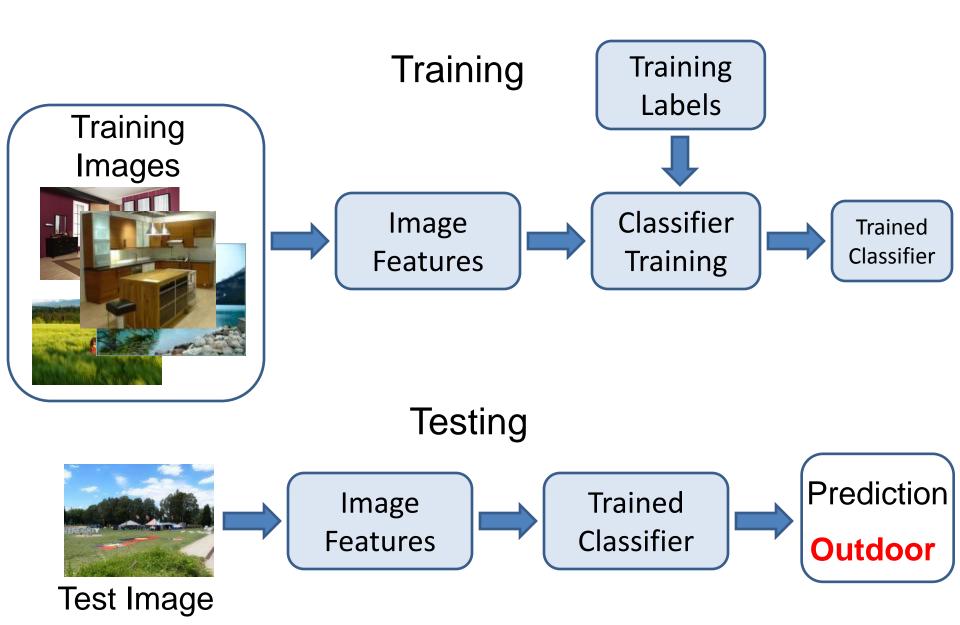
		Predicted class			
		Class1	Class2	Class3	
Actual class	Class1	40	1	6	
	Class2	3	25	7	
	Class3	4	9	10	

#### ROC curve

- Receiver\_operating\_characteristic
  - Area under the curve (AUC)
  - Equal Error Rate (EER)



#### Pipeline



#### Region Representation

- Segment the image
- Use features to represent each image segment



#### Region Representation

- Color, texture, BoW
  - Only computed within the local region

- Shape of regions
- Position in the image

# Working with regions

Spatial support is important – multiple segmentation

Spatial consistency – MRF smoothing

#### HW5, Prob2

Training and testing images for 8 categories

Implement representation: color histogram

- BoW model: preprocessed descriptors
  - Learning dictionary using K-Means
  - Learning classifier (NN, SVM)

Report final result (confusion matrix)