

You may assume the following problems are NP-hard:

CIRCUITSAT: Given a boolean circuit, are there any input values that make the circuit output TRUE?

PLANARCIRCUITSAT: Given a boolean circuit drawn in the plane so that no two wires cross, are there any input values that make the circuit output TRUE?

3SAT: Given a boolean formula in conjunctive normal form, with exactly three literals per clause, does the formula have a satisfying assignment?

MAXINDEPENDENTSET: Given an undirected graph G , what is the size of the largest subset of vertices in G that have no edges among them?

MAXCLIQUE: Given an undirected graph G , what is the size of the largest complete subgraph of G ?

MINVERTEXCOVER: Given an undirected graph G , what is the size of the smallest subset of vertices that touch every edge in G ?

MINSETCOVER: Given a collection of subsets S_1, S_2, \dots, S_m of a set S , what is the size of the smallest subcollection whose union is S ?

MINHITTINGSET: Given a collection of subsets S_1, S_2, \dots, S_m of a set S , what is the size of the smallest subset of S that intersects every subset S_i ?

3COLOR: Given an undirected graph G , can its vertices be colored with three colors, so that every edge touches vertices with two different colors?

HAMILTONIANCYCLE: Given a graph G (either directed or undirected), is there a cycle in G that visits every vertex exactly once?

HAMILTONIANPATH: Given a graph G (either directed or undirected), is there a path in G that visits every vertex exactly once?

TRAVELINGSALESMAN: Given a graph G with weighted edges, what is the minimum total weight of any Hamiltonian path/cycle in G ?

STEINERTREE: Given an undirected graph G with some of the vertices marked, what is the minimum number of edges in a subtree of G that contains every marked vertex?

SUBSETSUM: Given a set X of positive integers and an integer k , does X have a subset whose elements sum to k ?

PARTITION: Given a set X of positive integers, can X be partitioned into two subsets with the same sum?

3PARTITION: Given a set X of $3n$ positive integers, can X be partitioned into n three-element subsets, all with the same sum?

DRAUGHTS: Given an $n \times n$ international draughts configuration, what is the largest number of pieces that can (and therefore must) be captured in a single move?

DOGE: Such N. Many P. Wow.