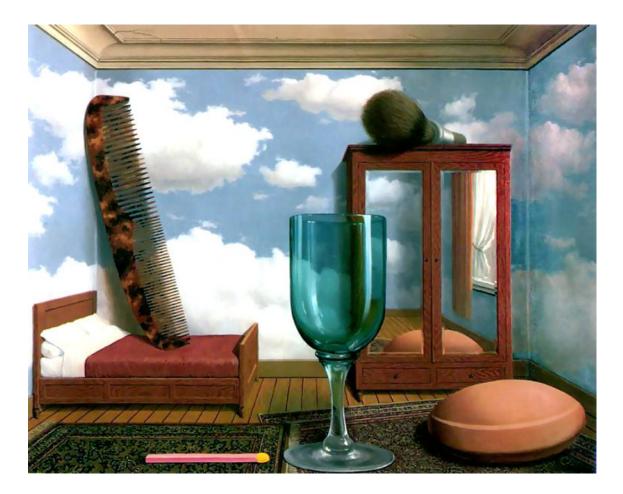
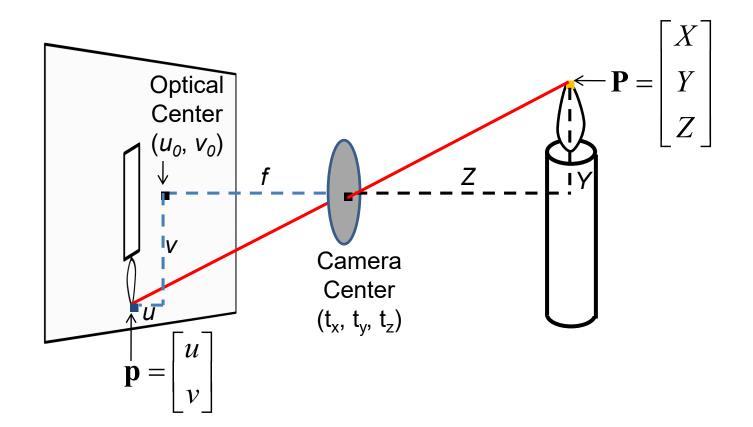
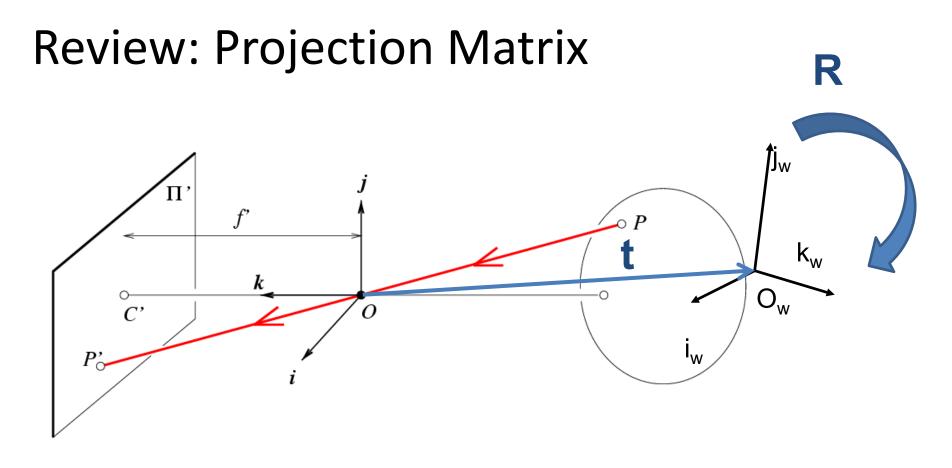
Single-view Metrology and Cameras



Computational Photography Derek Hoiem, University of Illinois

Review: Pinhole Camera





$$\mathbf{X} = \mathbf{K} \begin{bmatrix} \mathbf{R} & \mathbf{t} \end{bmatrix} \mathbf{X} \Longrightarrow w \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} f & s & u_0 \\ 0 & \alpha f & v_0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_x \\ r_{21} & r_{22} & r_{23} & t_y \\ r_{31} & r_{32} & r_{33} & t_z \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

Take-home question review

Suppose the camera axis is in the direction of (x=0, y=0, z=1) in its own coordinate system. What is the camera axis in world coordinates given the extrinsic parameters *R*, *t*

Suppose a camera at height y=h (x=0,z=0) observes a point at (u,v) known to be on the ground (y=0). Assume R is identity. What is the 3D position of the point in terms of f, u₀, v₀?

Take-home question review

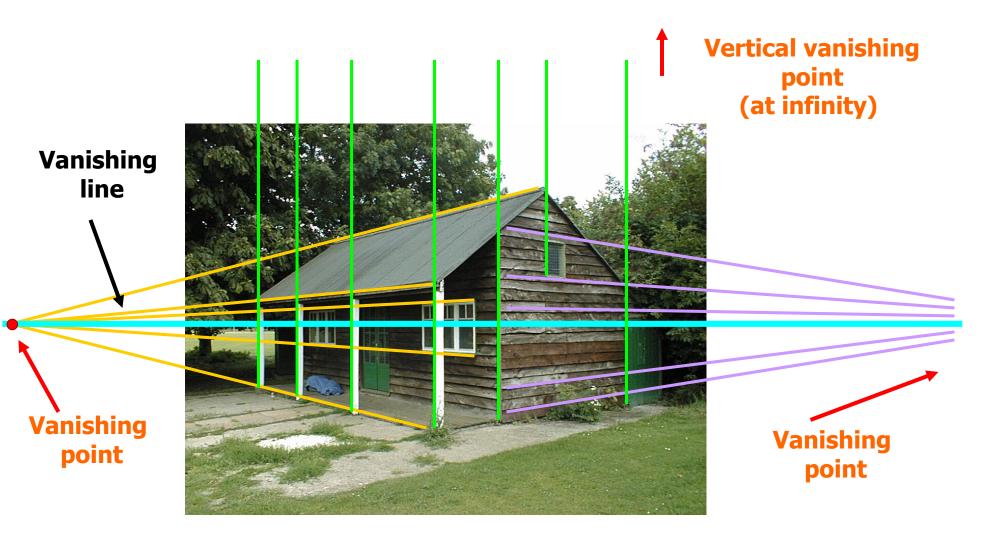
Suppose we have two 3D cubes on the ground facing the viewer, one near, one far.

- 1. What would they look like in perspective?
- 2. What would they look like in weak perspective?



Photo: Kathy from Flickr

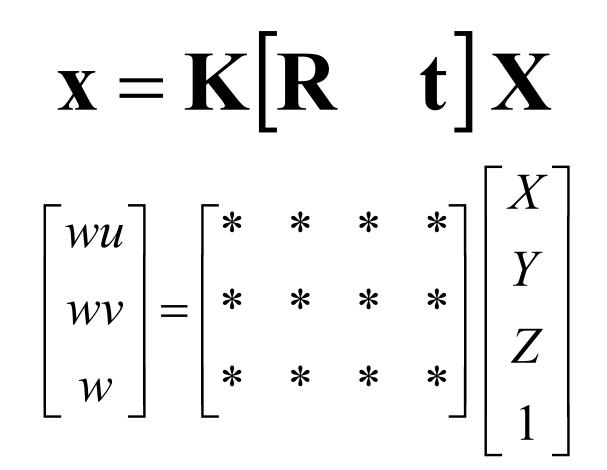
Review: Vanishing Points



This class

- How can we calibrate the camera?
- How can we measure the size of objects in the world from an image?
- What about other camera properties: focal length, field of view, depth of field, aperture, f-number?
- How to do "focus stacking" to get a sharp picture of a nearby object
- How the "vertigo effect" works

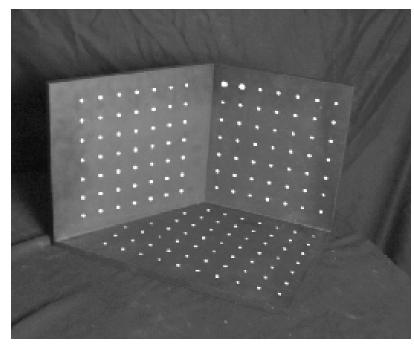
How to calibrate the camera?



Calibrating the Camera

Method 1: Use an object (calibration grid) with known geometry

- Correspond image points to 3d points
- Get least squares solution (or non-linear solution)

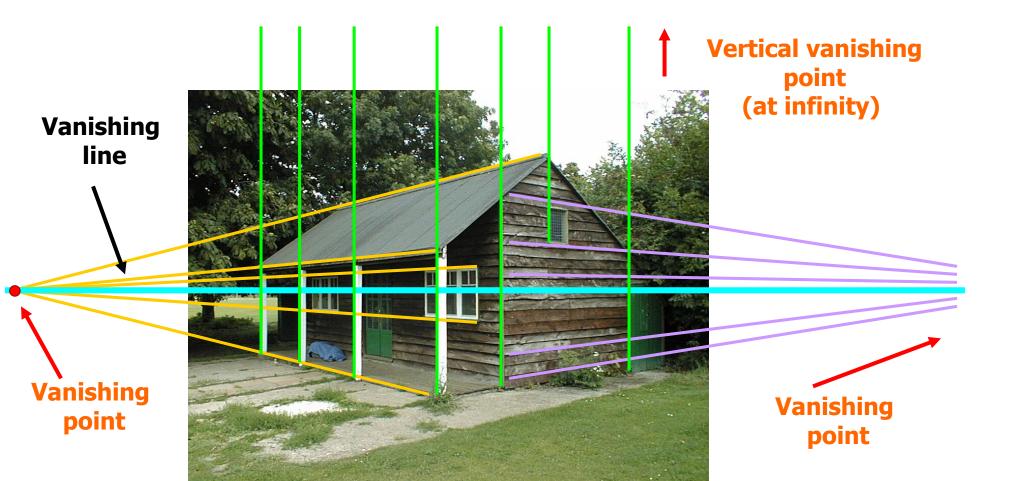


$$\begin{bmatrix} wu \\ wv \\ w \end{bmatrix} = \begin{bmatrix} m_{11} & m_{12} & m_{13} & m_{14} \\ m_{21} & m_{22} & m_{23} & m_{24} \\ m_{31} & m_{32} & m_{33} & m_{34} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

Calibrating the Camera

Method 2: Use vanishing points

- Find vanishing points corresponding to orthogonal directions



Take-home question (for later)

Suppose you have estimated finite three vanishing points corresponding to orthogonal directions:

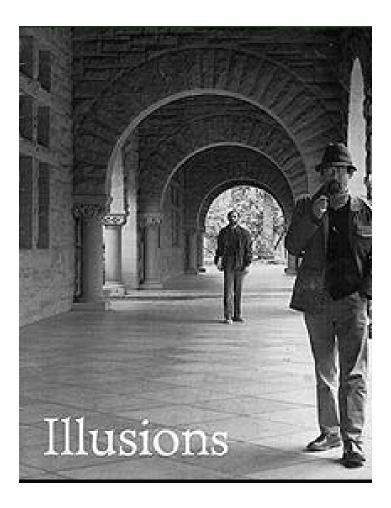
- 1) How to solve for intrinsic matrix? (assume K has three parameters)
 - The transpose of the rotation matrix is its inverse
 - Use the fact that the 3D directions are orthogonal
- 2) How to recover the rotation matrix that is aligned with the 3D axes defined by these points?
 - In homogeneous coordinates, 3d point at infinity is (X, Y, Z, 0)



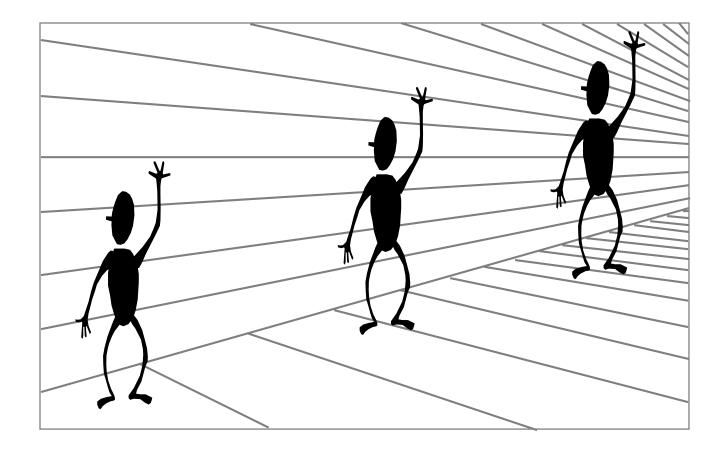


Photo from Garry Knight

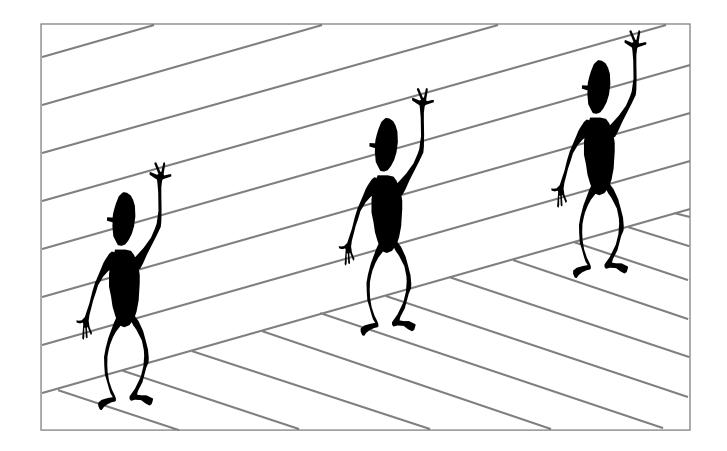
How can we measure the size of 3D objects from an image?



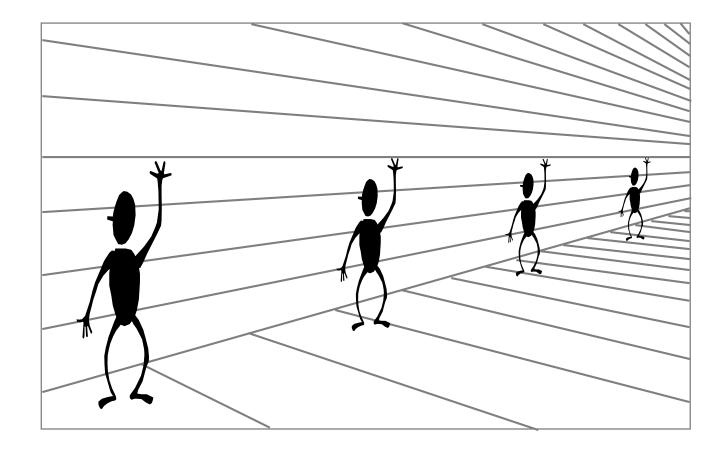
Perspective cues



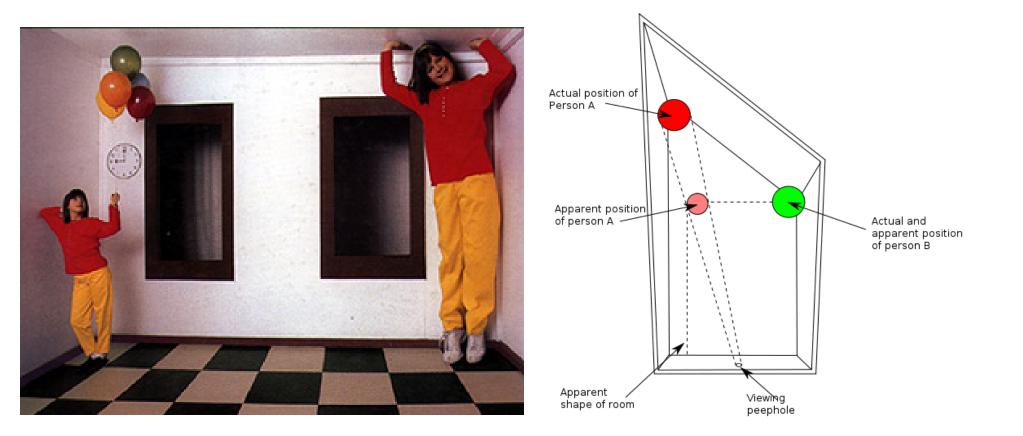
Perspective cues



Perspective cues

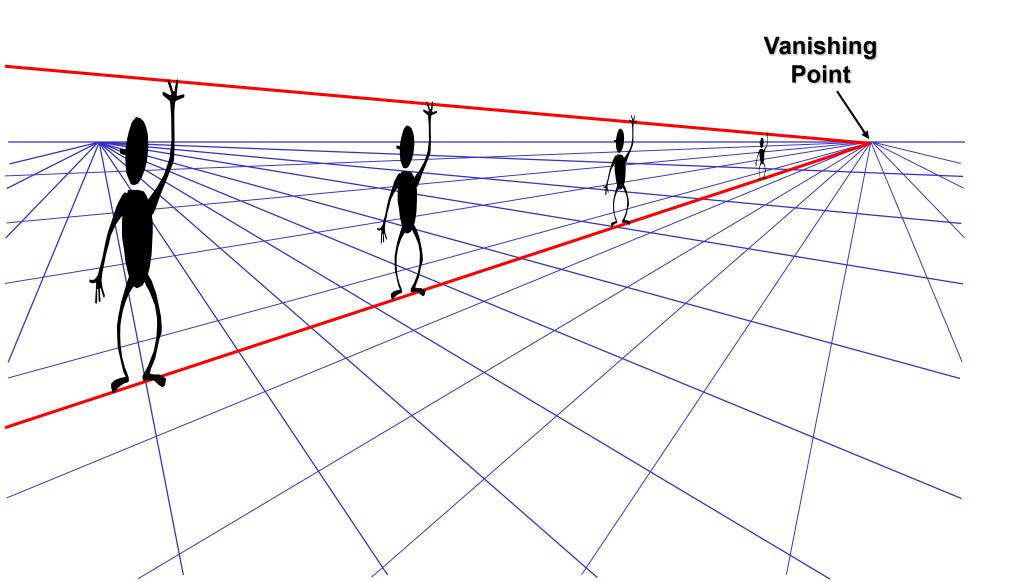


Ames Room



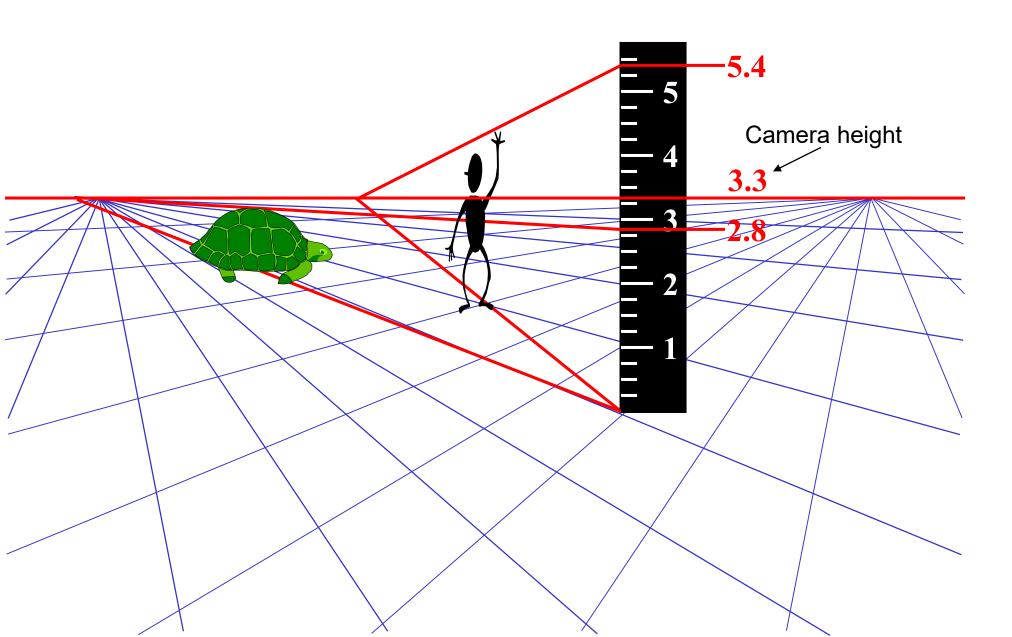
Slide by Steve Seitz

Comparing heights

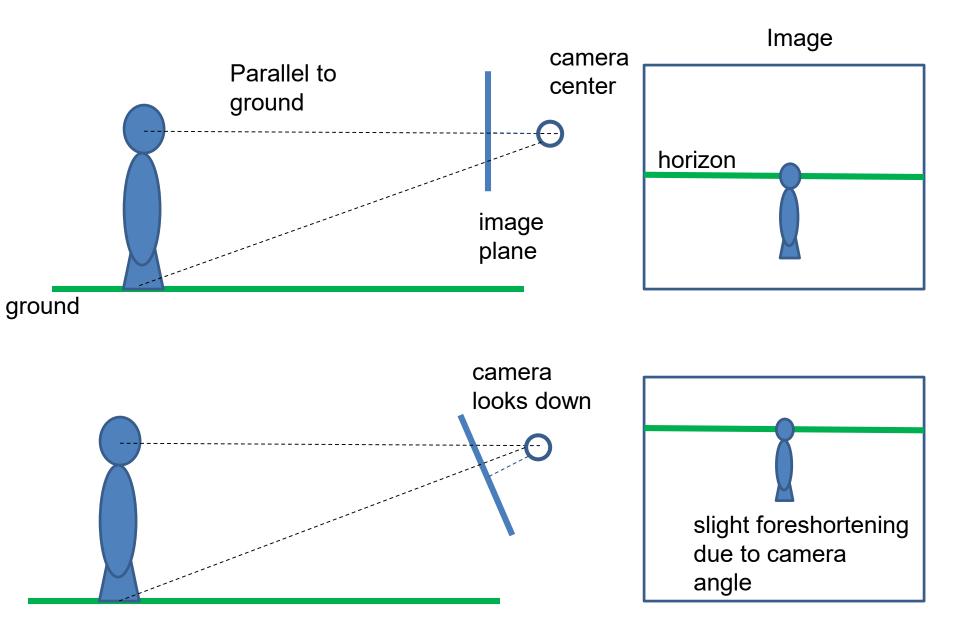


Slide by Steve Seitz

Measuring height



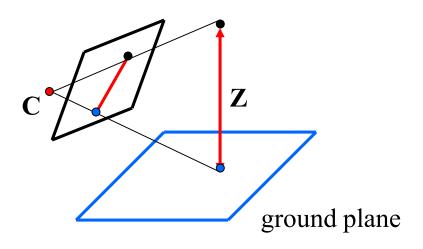
Two views of a scene



Which is higher – the camera or the parachute?



Measuring height without a giant ruler



Compute Z from image measurements

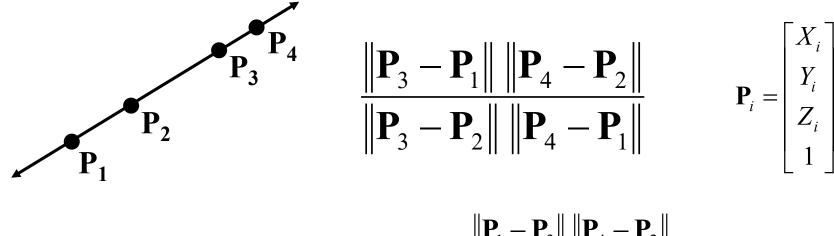
• Need a reference object

The cross ratio

A Projective Invariant

• Something that does not change under projective transformations (including perspective projection)

The cross-ratio of 4 collinear points



$$\frac{\|\mathbf{P}_1 - \mathbf{P}_3\| \|\mathbf{P}_4 - \mathbf{P}_2\|}{\|\mathbf{P}_1 - \mathbf{P}_2\| \|\mathbf{P}_4 - \mathbf{P}_3\|}$$

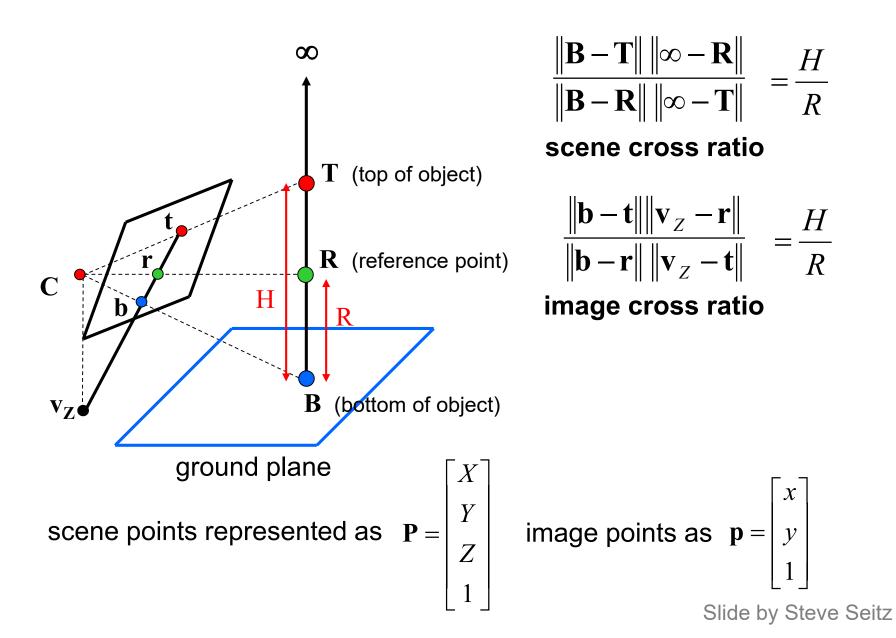
Can permute the point ordering

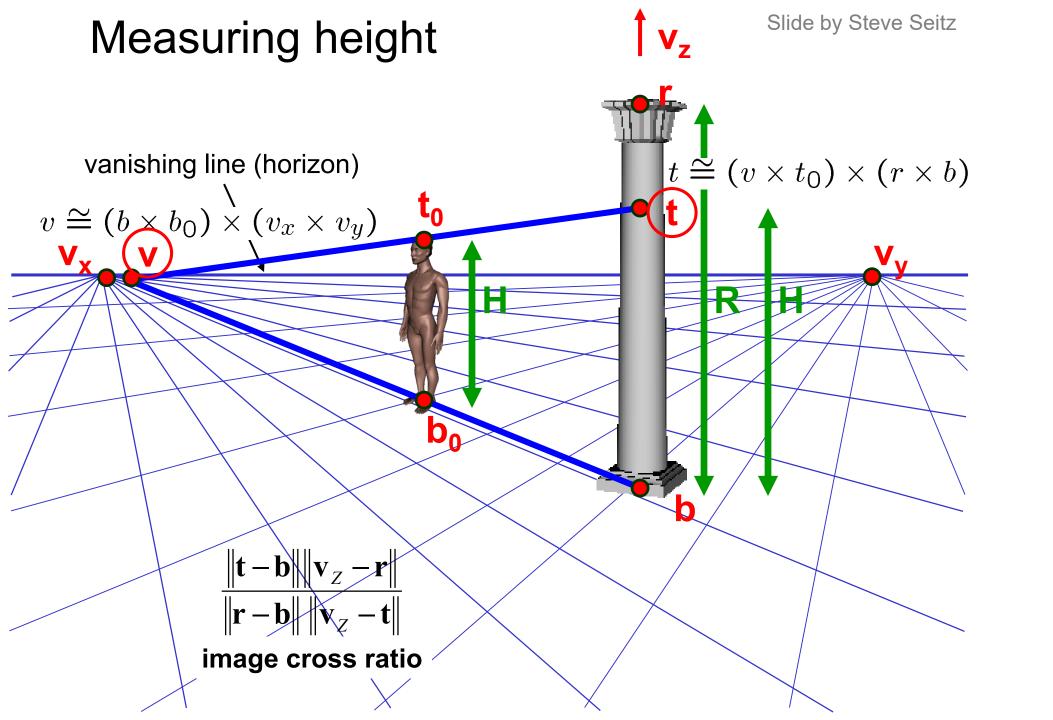
• 4! = 24 different orders (but only 6 distinct values)

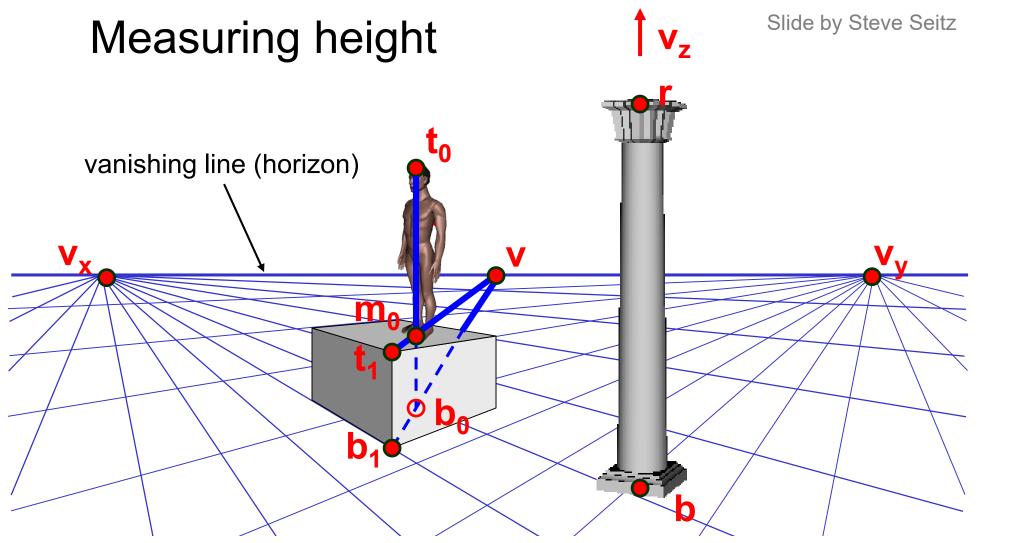
This is the fundamental invariant of projective geometry

Slide by Steve Seitz

Measuring height







What if the point on the ground plane \mathbf{b}_0 is not known?

- Here the guy is standing on the box, height of box is known
- Use one side of the box to help find \mathbf{b}_0 as shown above

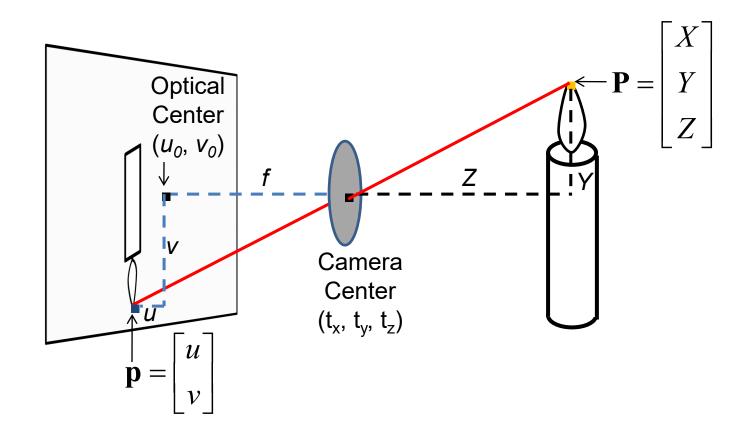
Take-home question

Assume that the man is 6 ft tall

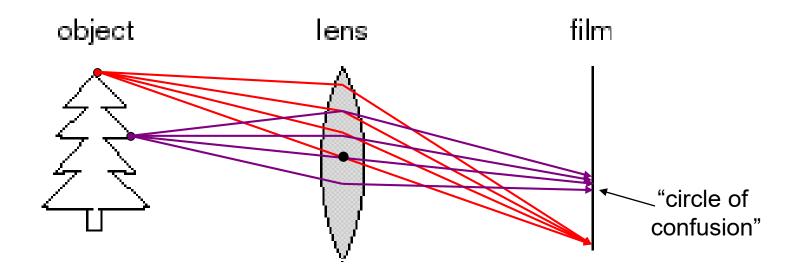
- What is the height of the front of the building?
- What is the height of the camera?



Beyond the pinhole: What about focus, aperture, DOF, FOV, etc?

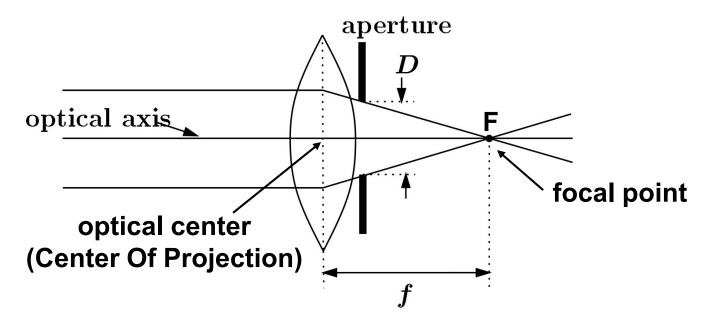


Adding a lens



- A lens focuses light onto the film
 - There is a specific distance at which objects are "in focus"
 - other points project to a "circle of confusion" in the image
 - Changing the shape of the lens changes this distance

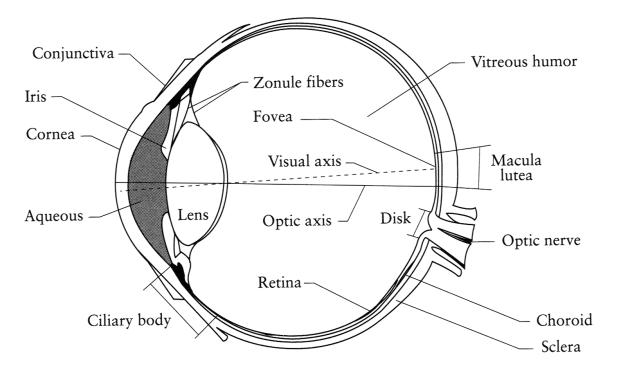
Focal length, aperture, depth of field



A lens focuses parallel rays onto a single focal point

- focal point at a distance *f* beyond the plane of the lens
- Aperture of diameter D restricts the range of rays

The eye

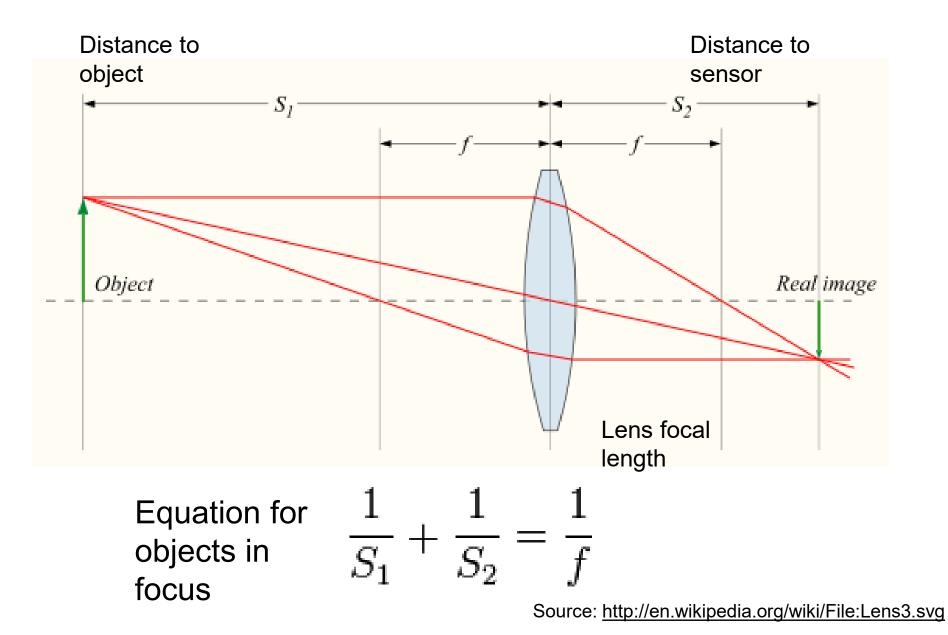


The human eye is a camera

- Iris colored annulus with radial muscles
- **Pupil** the hole (aperture) whose size is controlled by the iris

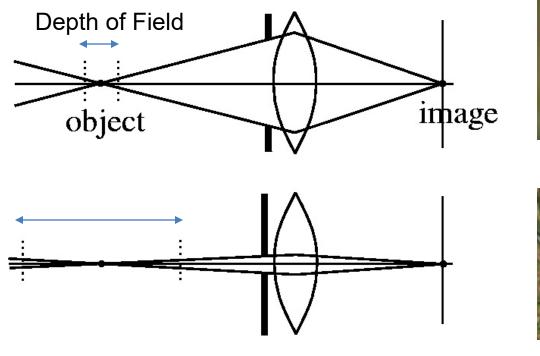
Figure: Fig. 1.1, Principles of Digital Image Synthesis, Volume 1. Andrew Glassner

Focus with lenses



Slide source: Seitz

The aperture and depth of field





f/5.6



f/32

- Changing the aperture size or focusing distance affects depth of field f-number (f/#) =focal_length / aperture_diameter (e.g., f/16 means that the focal length is 16 times the diameter)
 - When you change the f-number, you are changing the aperture
- Depth of Field = range around focused distance that leads to smaller than threshold circle of confusion

Flower images from Wikipedia <u>http://en.wikipedia.org/wiki/Depth_of_field</u>

Varying the aperture



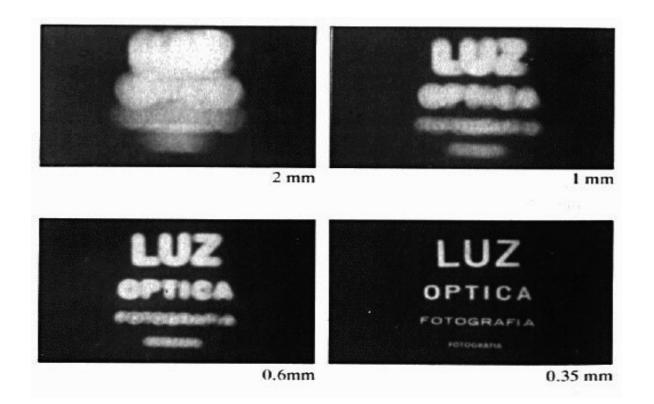


Photo credit: Philip Greenspun

Small aperture = large DOF

Large aperture = small DOF

Shrinking the aperture



Why not make the aperture as small as possible?

- Less light gets through
- Diffraction effects

Shrinking the aperture

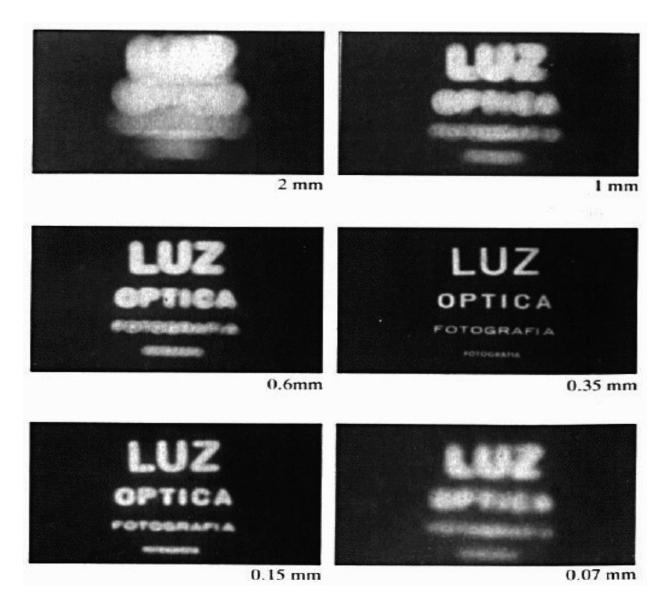
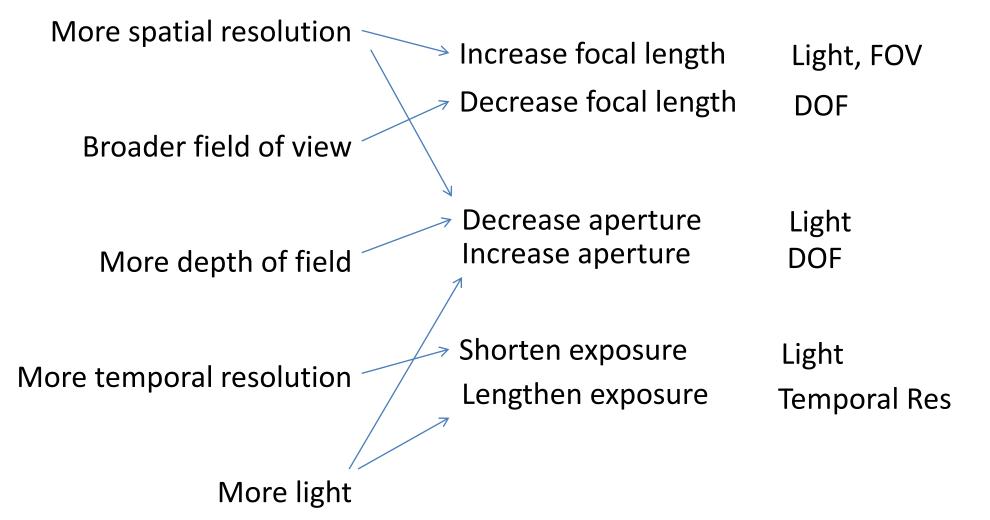


Figure: Optics. Eugene Hecht

The Photographer's Great Compromise

What we want How we get it Cost



End lecture here next time

Difficulty in macro (close-up) photography

- For close objects, we have a small relative DOF
- Can only shrink aperture so far

How to get both bugs in focus?



Solution: Focus stacking

1. Take pictures with varying focal length



Example from http://www.wonderfulphotos.com/articles/macro/focus_stacking/

Solution: Focus stacking

- 1. Take pictures with varying focal length
- 2. Combine



Focus stacking



http://www.wonderfulphotos.com/articles/macro/focus_stacking/

Focus stacking

How to combine?

Web answer: With software (Photoshop, CombineZM)

How to do it automatically?

Focus stacking

How to combine?

- 1. Align images (e.g., using corresponding points)
- 2. Two ideas
 - a) Mask regions by hand and combine with pyramid blend
 - b) Gradient domain fusion (mixed gradient) without masking

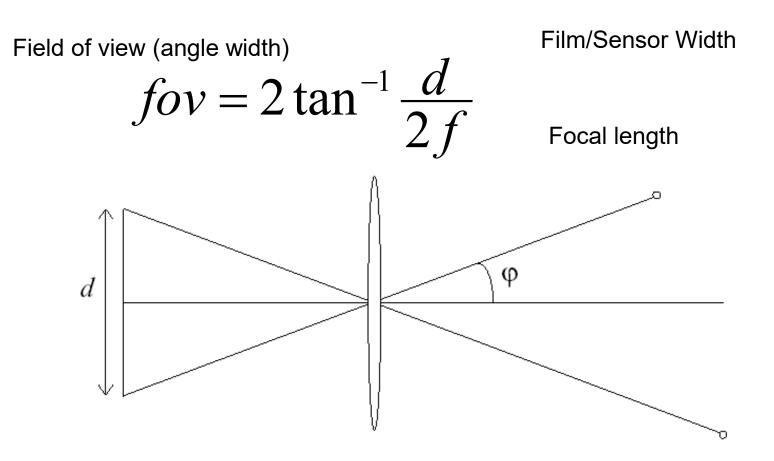
Automatic solution would make an interesting final project

Recommended Reading:

http://www.digital-photographyschool.com/an-introduction-to-focusstacking

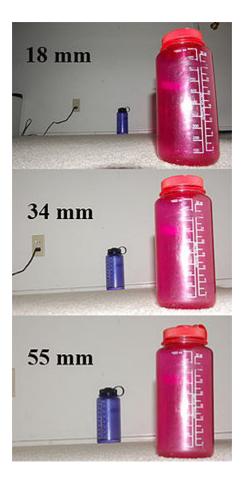
http://www.zen20934.zen.co.uk/photograph y/Workflow.htm#Focus%20Stacking

Relation between field of view and focal length



Dolly Zoom or "Vertigo Effect"

http://www.youtube.com/watch?v=NB4bikrNzMk

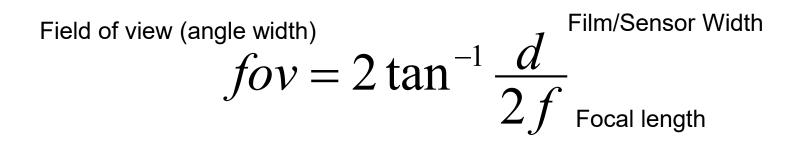


How is this done?

Zoom in while moving away

http://en.wikipedia.org/wiki/Focal_length

Dolly zoom (or "Vertigo effect")



width of object

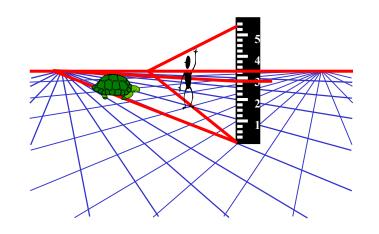
$$2\tan\frac{fov}{2} = \frac{width}{distance}$$

Distance between object and camera

Things to remember

 Can calibrate using grid or VP

 Can measure relative sizes using VP



• Effects of focal length, aperture + tricks



Next class

- Go over take-home questions from today
- Single-view 3D Reconstruction