

Computational Approaches to Cameras

11/12/15

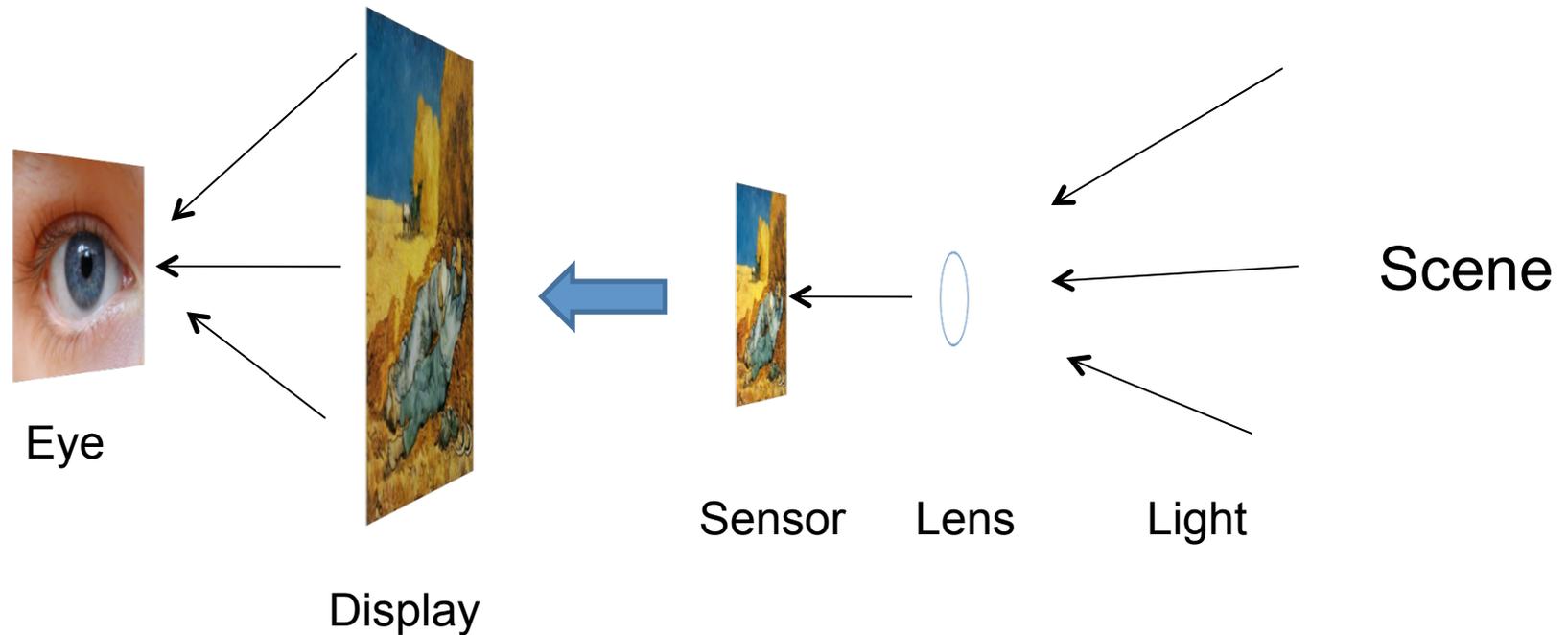


Magritte , *The False Mirror* (1935)

Computational Photography
Derek Hoiem, University of Illinois

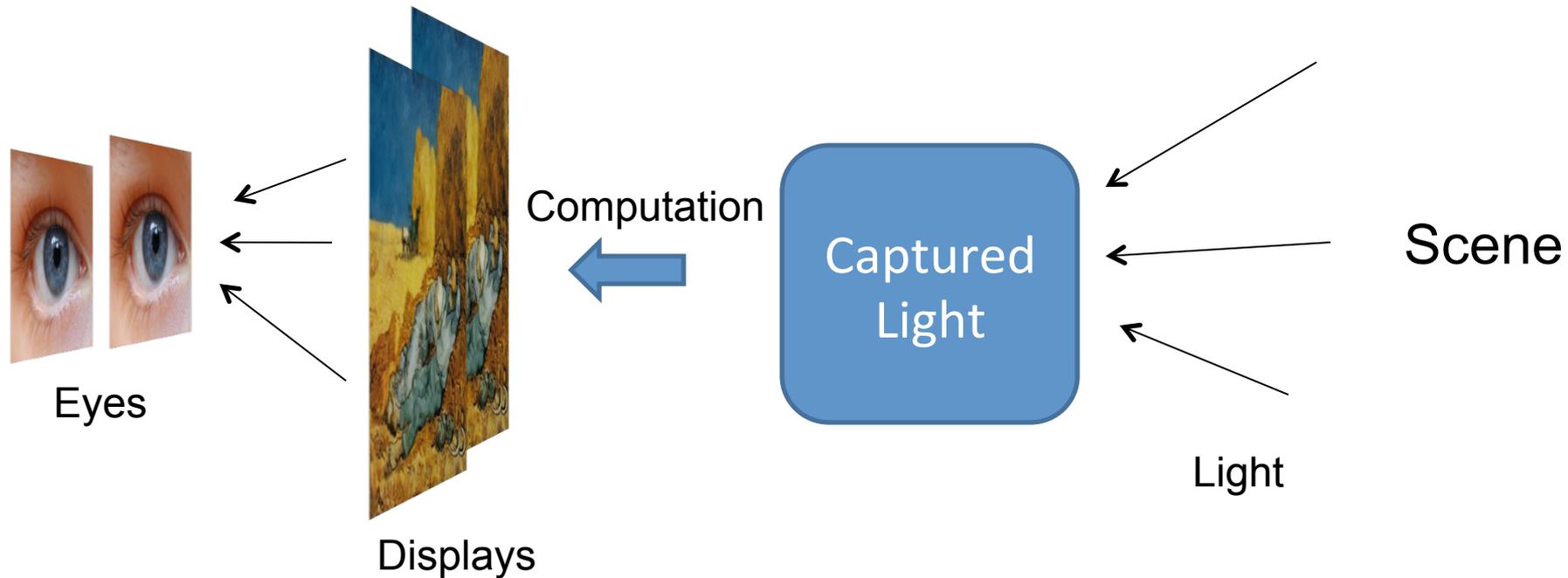
Conventional cameras

- Conventional cameras are designed to capture light in a medium that is directly viewable



Computational cameras

- With a computational approach, we can capture light and then figure out what to do with it



Questions for today

- How can we represent all of the information contained in light?
- What are the fundamental limitations of cameras?
- What sacrifices have we made in conventional cameras? For what benefits?
- How else can we design cameras for better focus, deblurring, multiple views, depth, etc.?

How can we represent all of the
information contained in light?

Representing Light: The Plenoptic Function



Figure by Leonard McMillan

Q: What is the set of all things that we can ever see?

A: The Plenoptic Function (Adelson & Bergen)

Let's start with a stationary person and try to parameterize everything that he can see...

Grayscale snapshot



$$P(\theta, \phi)$$

is intensity of light

- Seen from a single view point
- At a single time
- Averaged over the wavelengths of the visible spectrum

(can also do $P(x,y)$, but spherical coordinate are nicer)

Color snapshot



$$P(\theta, \phi, \lambda)$$

is intensity of light

- Seen from a single view point
- At a single time
- As a function of wavelength

A movie

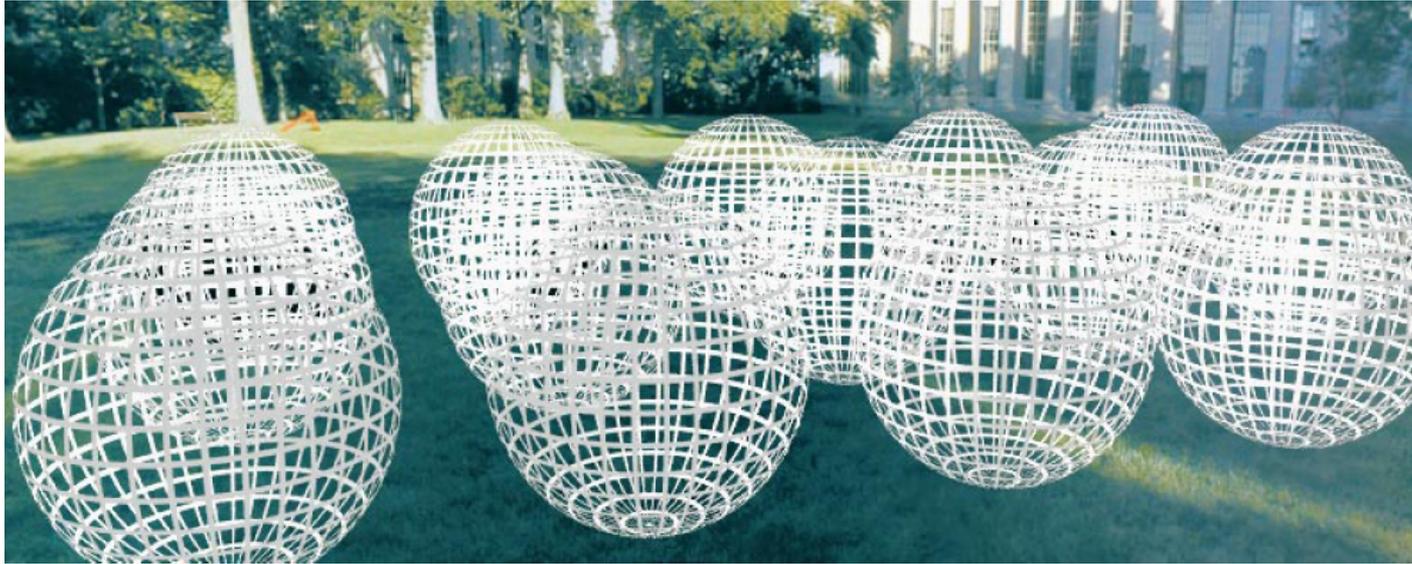


$$P(\theta, \phi, \lambda, t)$$

is intensity of light

- Seen from a single view point
- Over time
- As a function of wavelength

Holographic movie

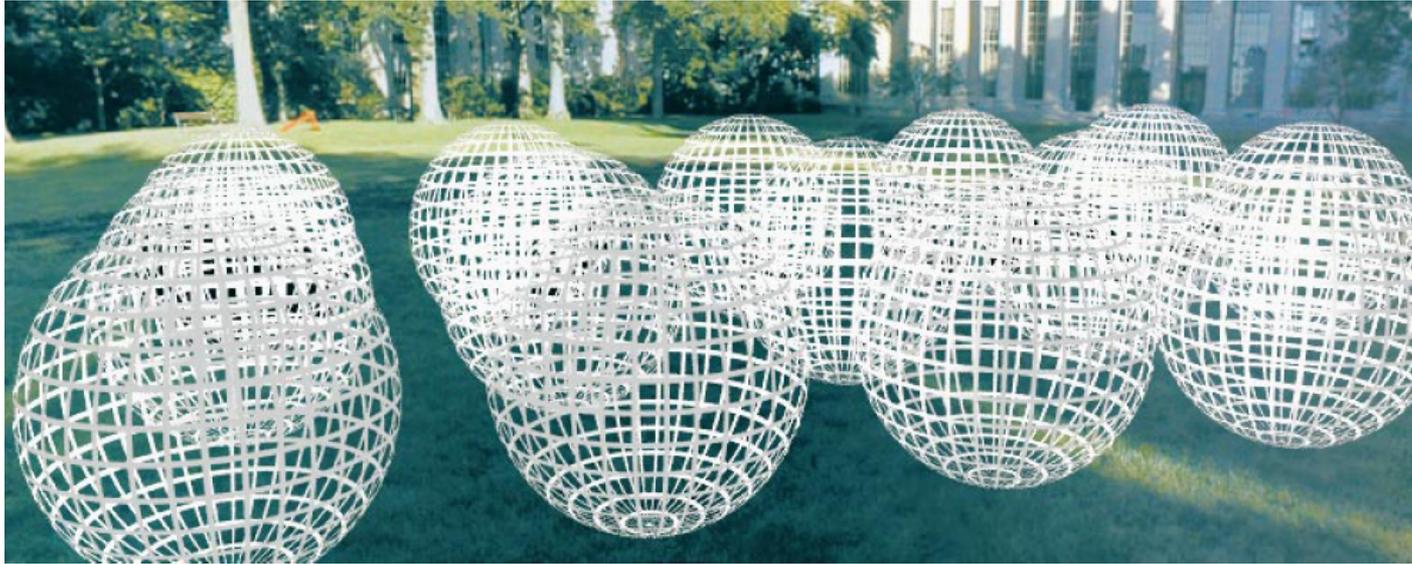


$$P(\theta, \phi, \lambda, t, V_x, V_y, V_z)$$

is intensity of light

- Seen from ANY viewpoint
- Over time
- As a function of wavelength

The Plenoptic Function



$$P(\theta, \phi, \lambda, t, V_x, V_y, V_z)$$

- Can reconstruct every possible view, at every moment, from every position, at every wavelength
- Contains every photograph, every movie, everything that anyone has ever seen!

Full Plenoptic Camera

Records position and orientation of each ray
at each time and wavelength

$$P(V_x, V_y, V_z, \theta, \phi, t, \lambda)$$

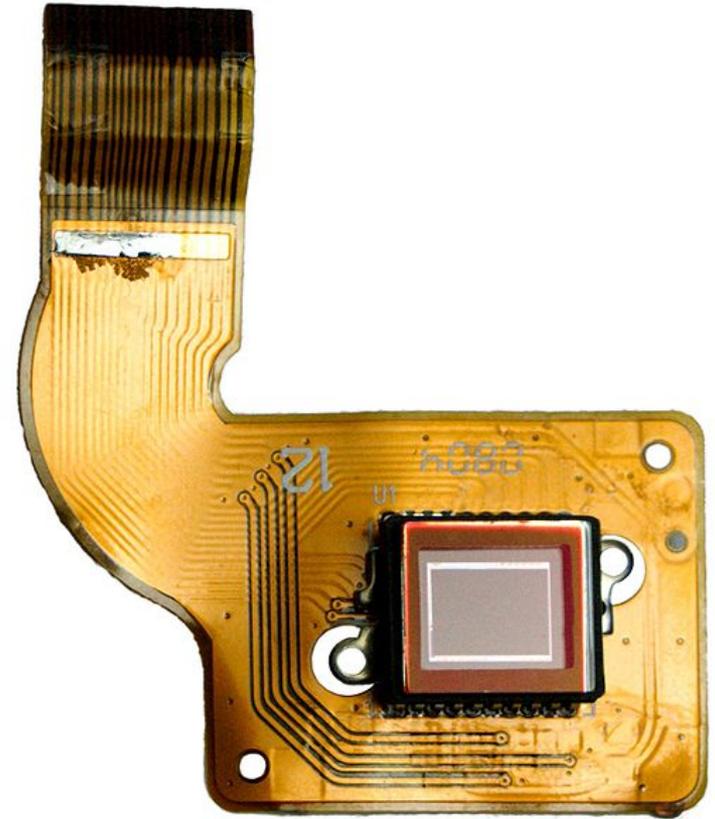
What fundamentally limits cameras?

Representing light

The atomic element of light: ~~a pixel~~ **a ray**

Fundamental limitations and trade-offs

- Only so much light in a given area to capture
- Basic sensor accumulates light at a set of positions from all orientations, over all time
- We want **intensity** of light at a **given time** at **one position** for a **set of orientations**
- Solutions:
 - funnel, constrain, redirect light
 - change the sensor



CCD inside camera

What sacrifices does the conventional camera make? For what gains?

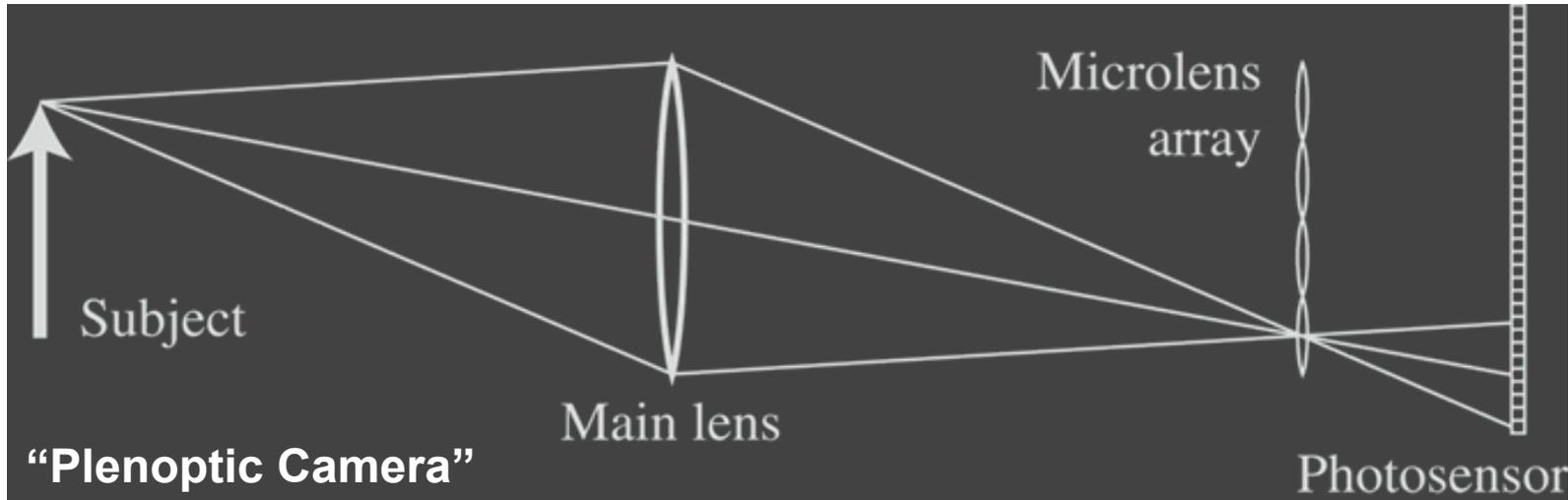
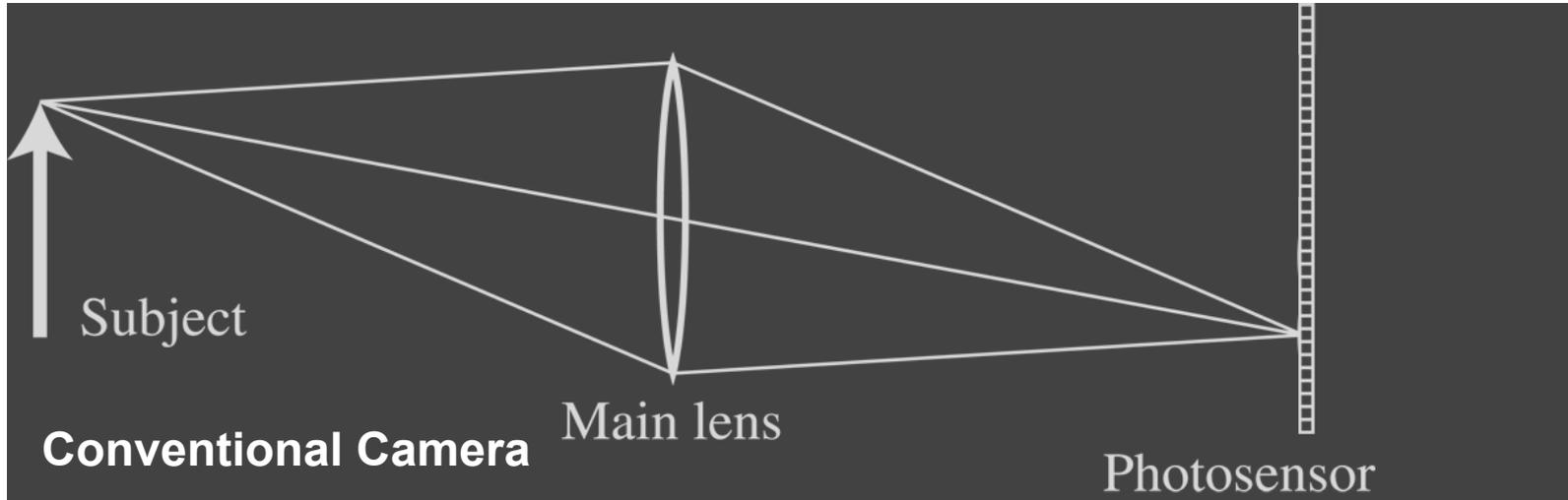
Trade-offs of conventional camera

- Add a pinhole
 - ✓ Pixels correspond to small range of orientations at the camera center, instead of all gathered light at one position
 - ✗ Much less light hits sensor
- Add a lens
 - ✓ More light hits sensor
 - ✗ Limited depth of field
 - ✗ Chromatic aberration
- Add a shutter
 - Capture average intensity at a particular range of times
- Increase sensor resolution
 - ✓ Each pixel represents a smaller range of orientations
 - ✗ Less light per pixel
- Controls: aperture size, focal length, shutter time

How else can we design cameras?

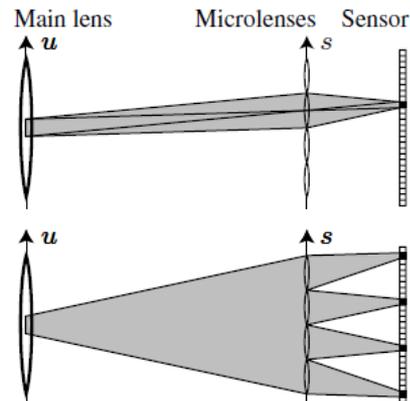
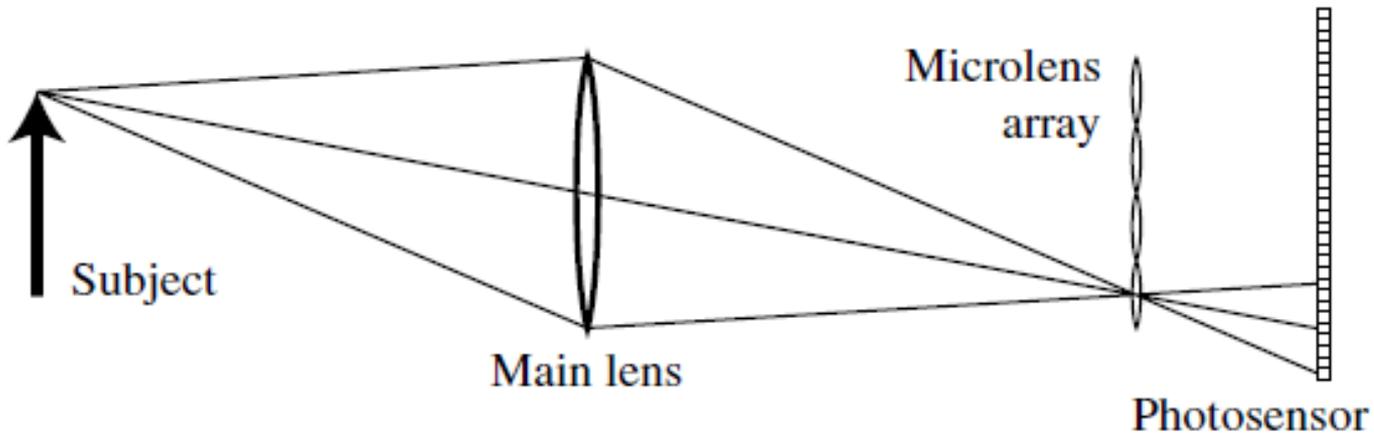
What do they sacrifice/gain?

1. Light Field Photography with “Plenoptic Camera”



Light field photography

- Like replacing the human retina with an insect compound eye
- Records where light ray hits the lens



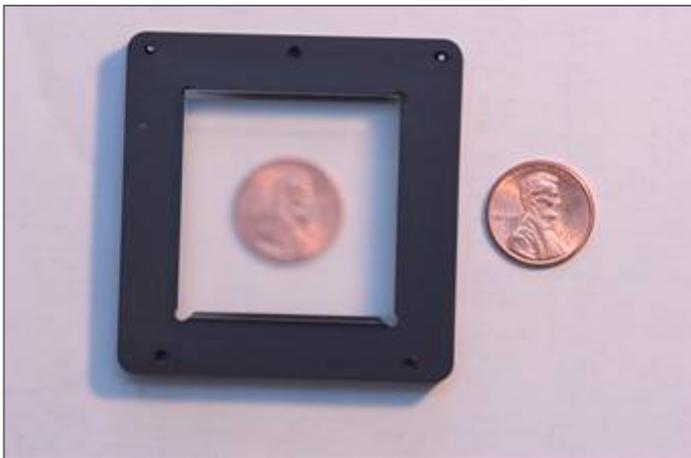
Stanford Plenoptic Camera [Ng et al 2005]



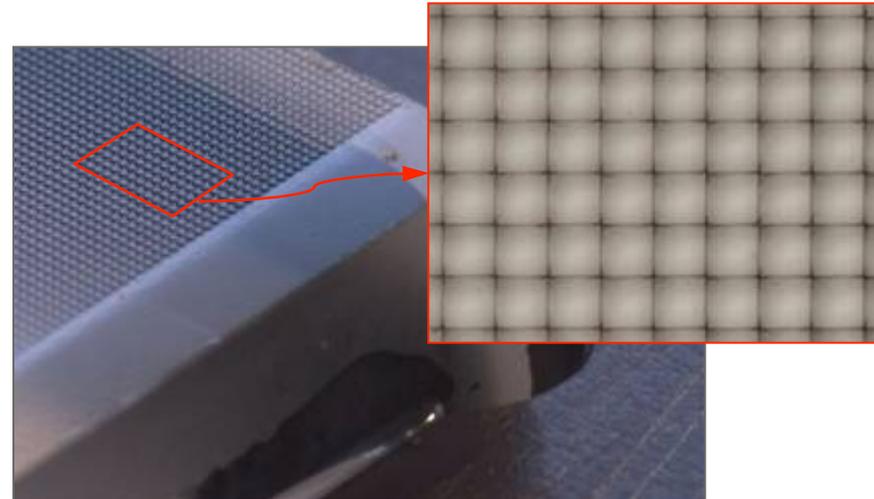
Contax medium format camera



Kodak 16-megapixel sensor



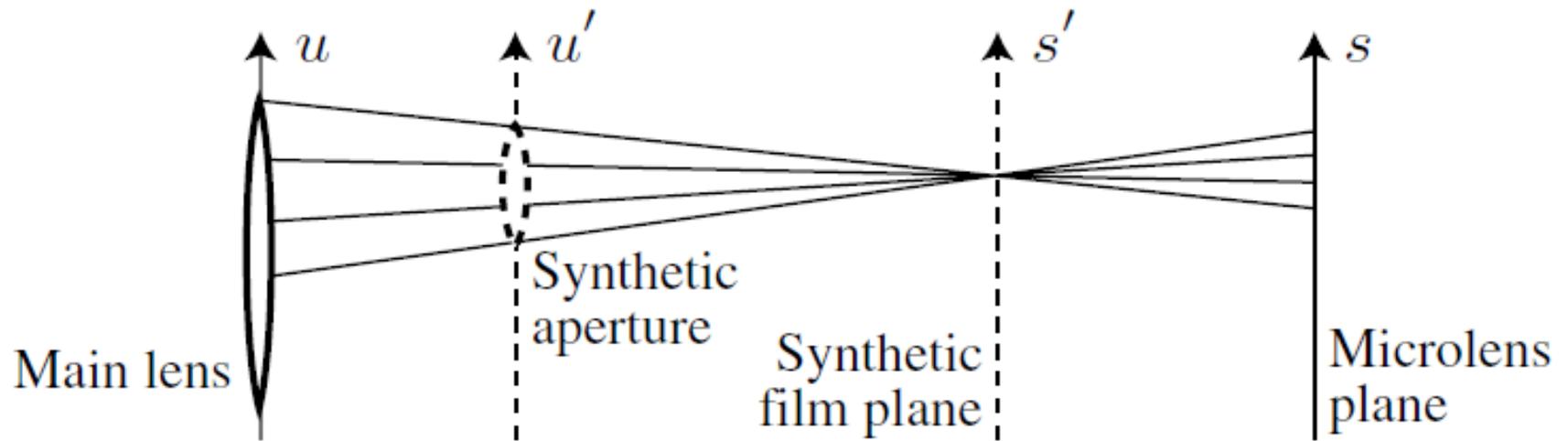
Adaptive Optics microlens array



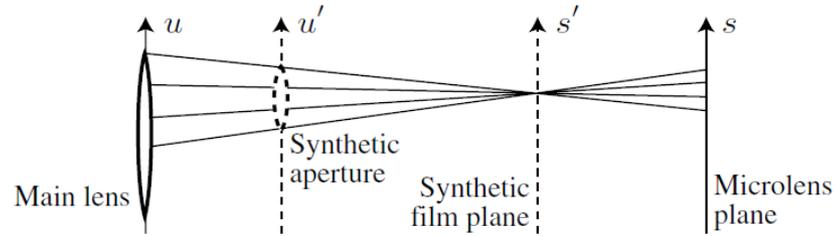
125μ square-sided microlenses

$$4000 \times 4000 \text{ pixels} \div 292 \times 292 \text{ lenses} = 14 \times 14 \text{ pixels per lens}$$

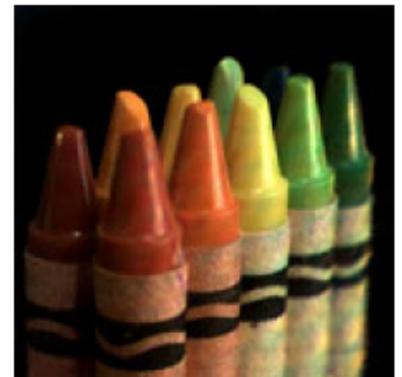
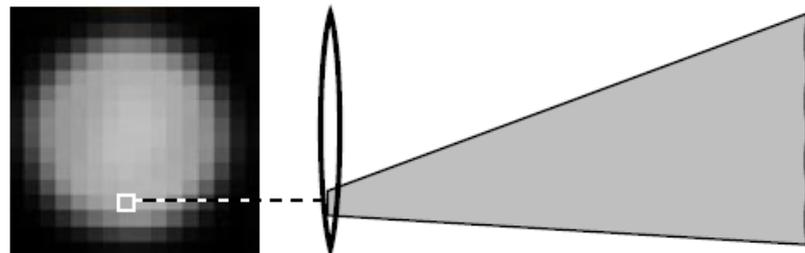
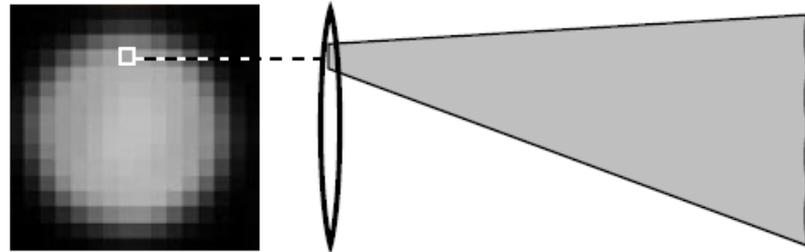
Light field photography: applications



Light field photography: applications



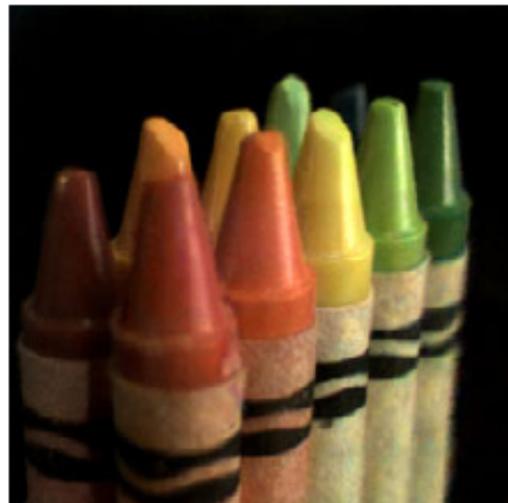
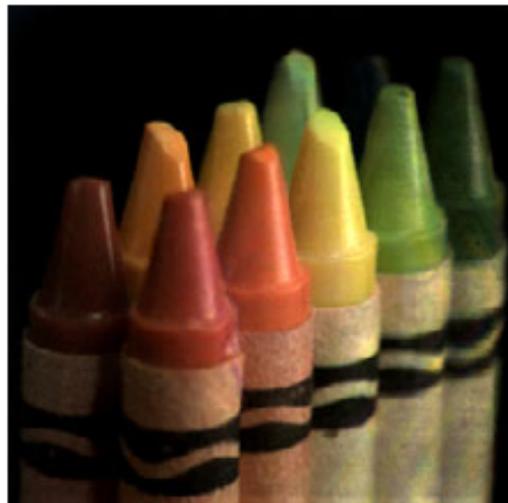
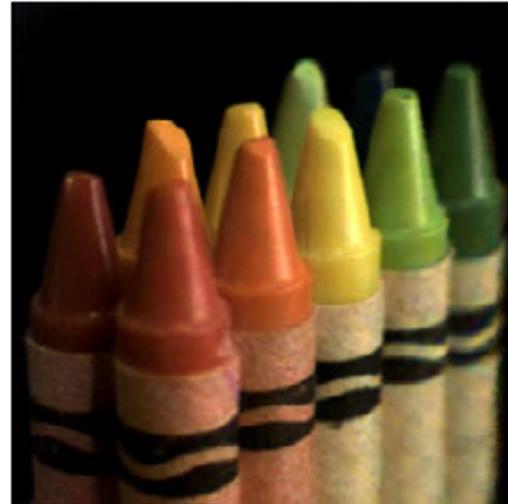
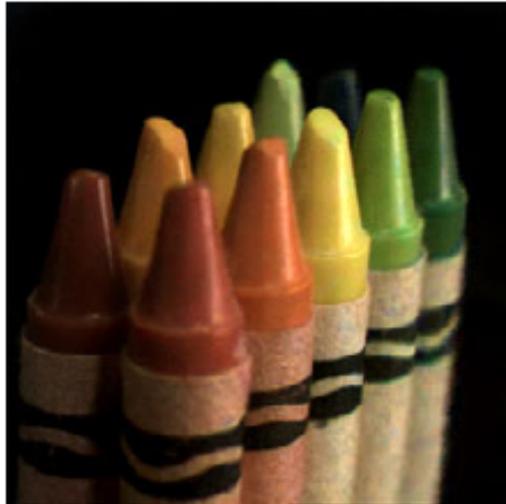
Change in
viewpoint



Light field photography: applications

Change in viewpoint

Lateral



Along Optical Axis

Digital Refocusing



Light field photography w/ microlenses

- We gain
 - Ability to refocus or increase depth of field
 - Ability for small viewpoint shifts
- What do we lose (vs. conventional camera)?

2. Coded apertures

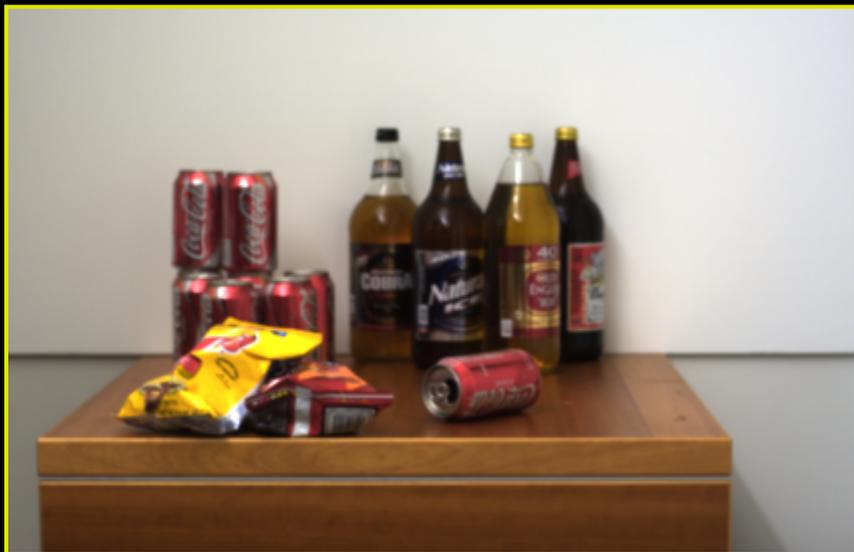
Image and Depth from a Conventional Camera with a Coded Aperture

**Anat Levin, Rob Fergus,
Frédo Durand, William Freeman**

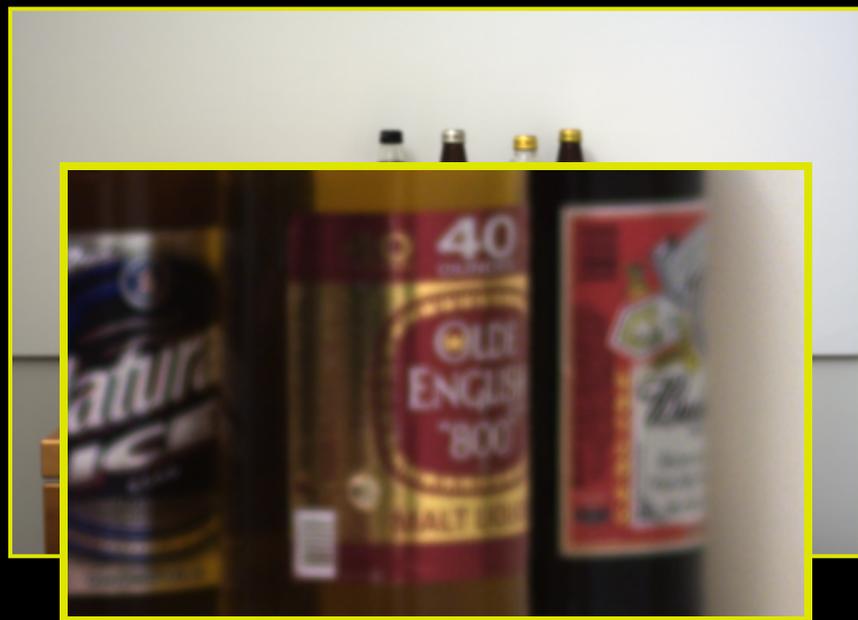
MIT CSAIL

Output #1: Depth map

Single input image:



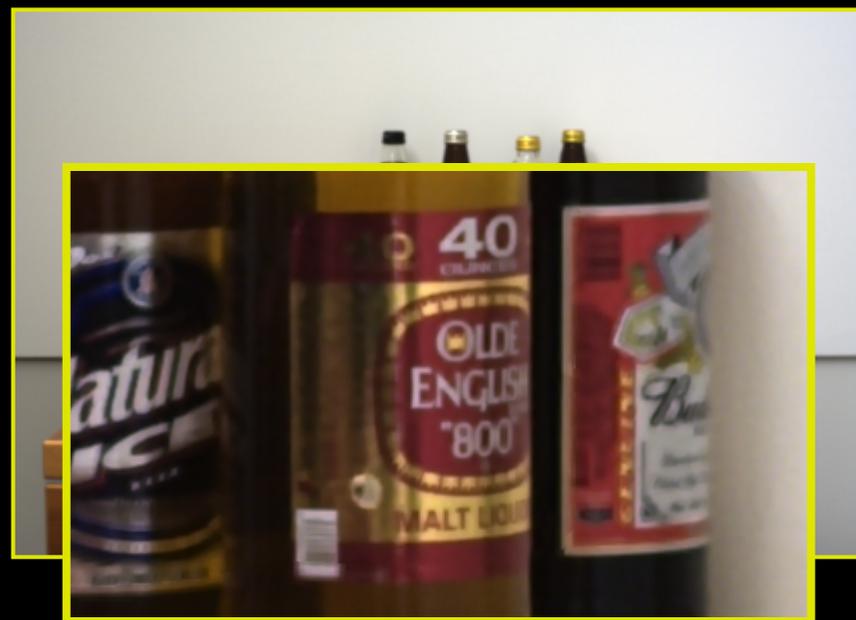
Single input image:



Output #1: Depth map



Output #2: All-focused image



Lens and defocus

Lens' aperture

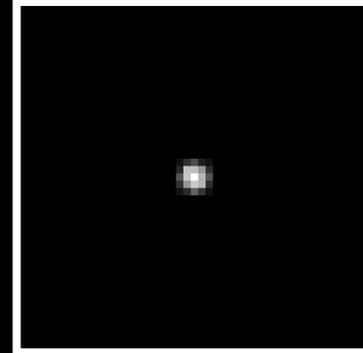
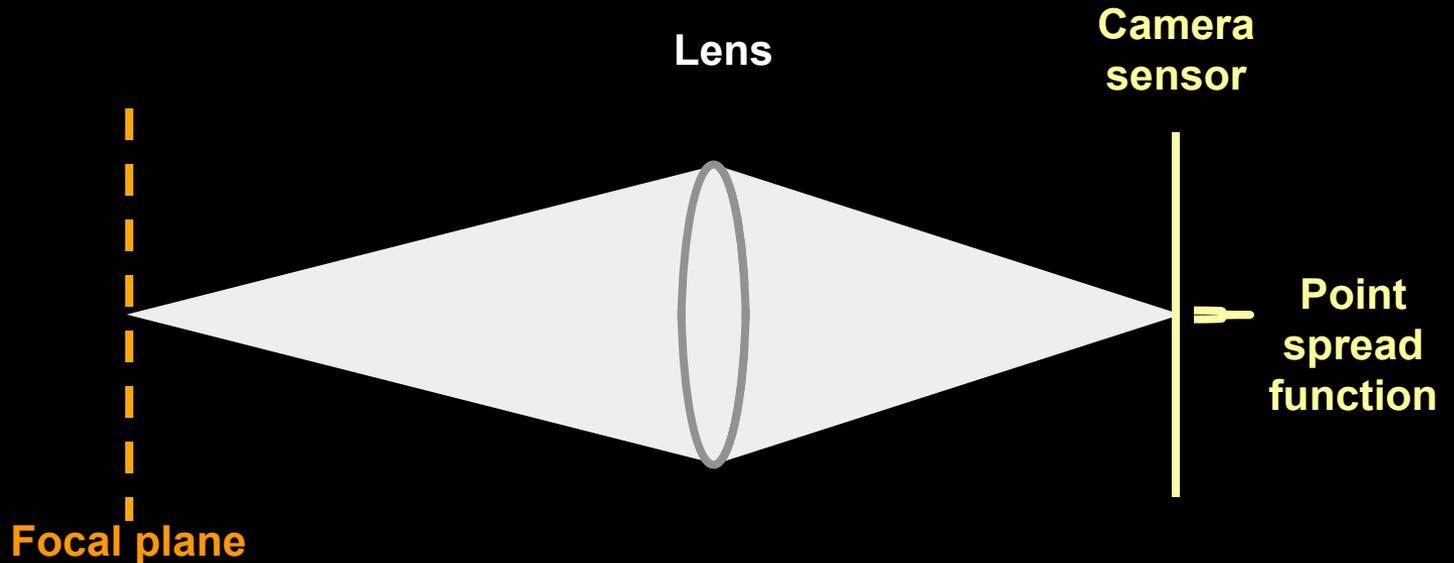


Image of a point light source



Lens and defocus

Lens' aperture

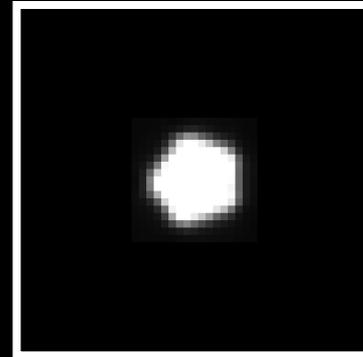
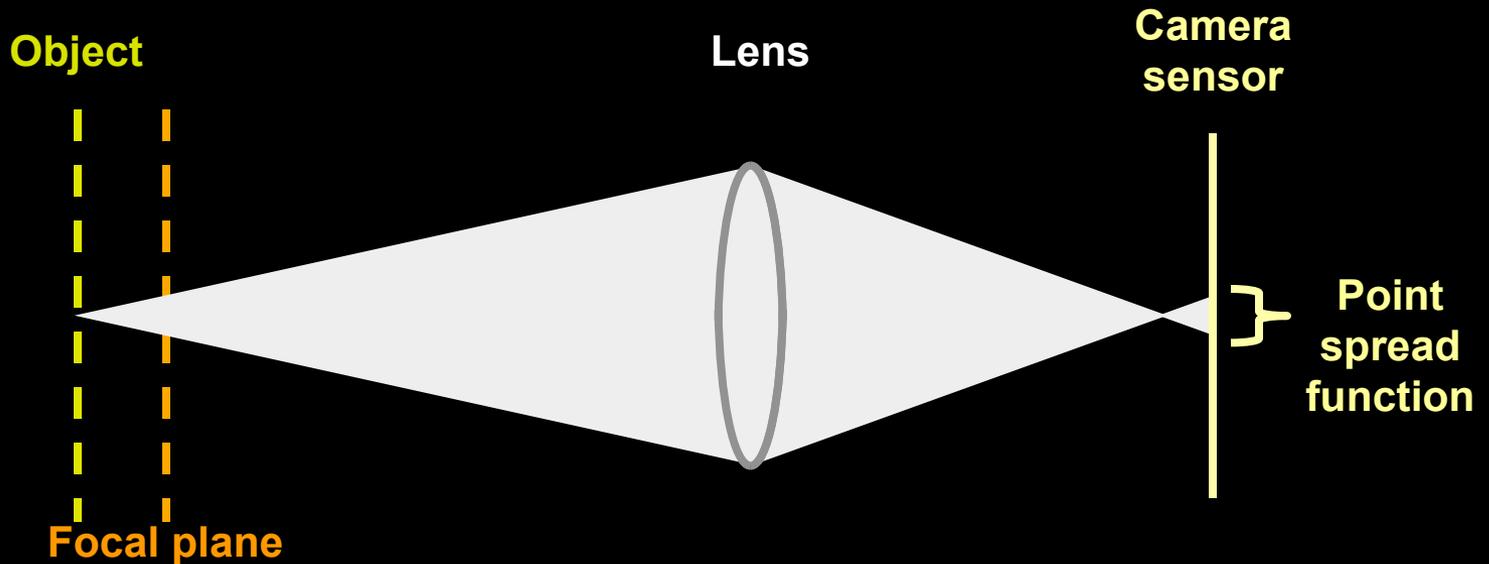


Image of a defocused point light source



Lens and defocus

Lens' aperture

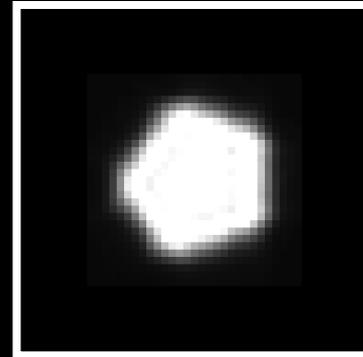
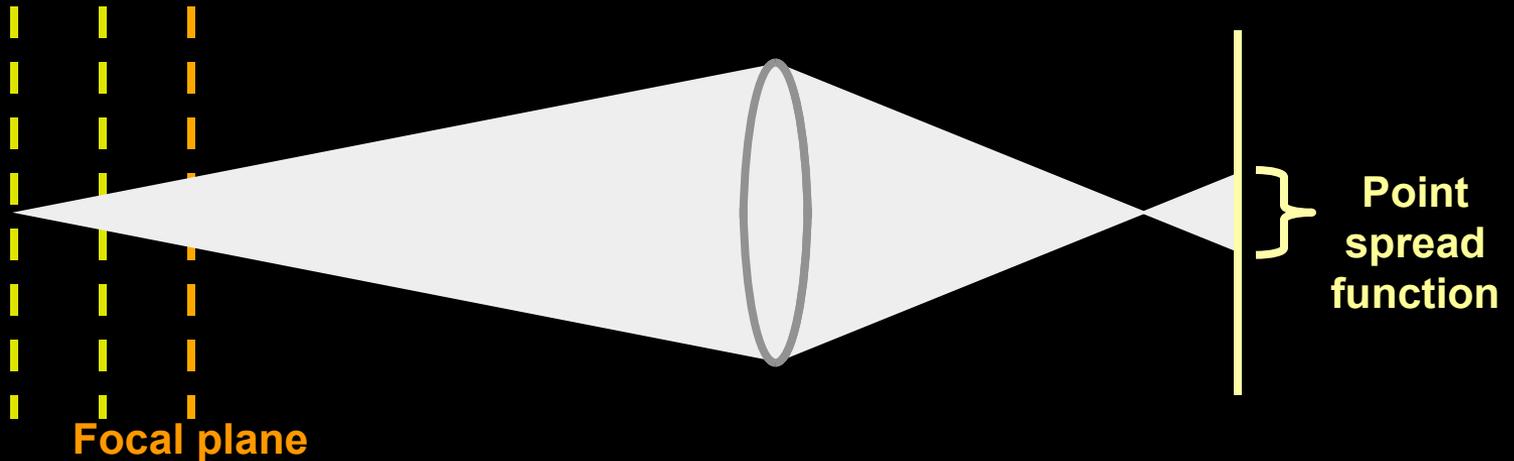


Image of a defocused point light source

Object

Lens

Camera sensor



Lens and defocus

Lens' aperture

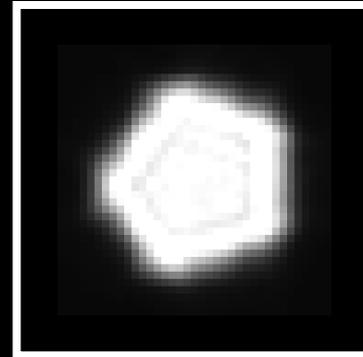
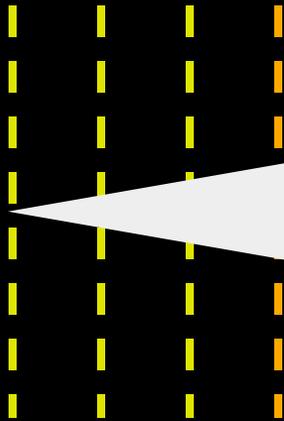


Image of a defocused point light source

Object



Focal plane

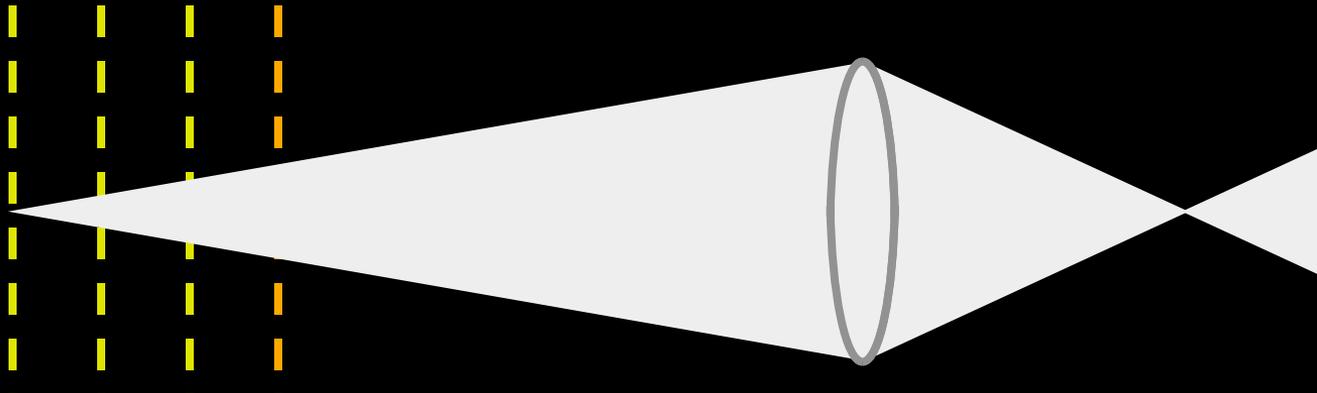
Lens



Camera sensor



Point spread function



Lens and defocus

Lens' aperture

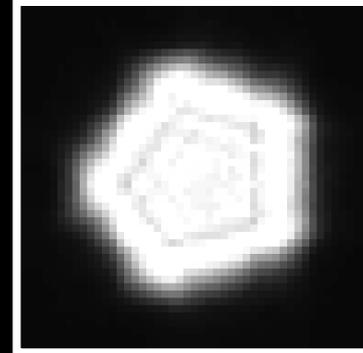
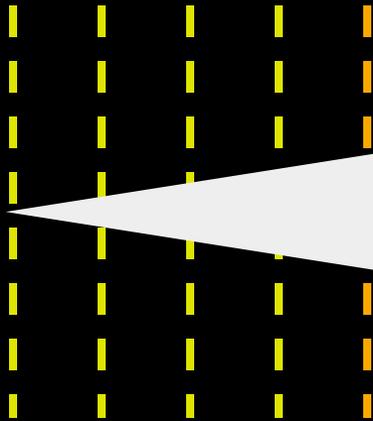


Image of a defocused point light source

Object



Focal plane

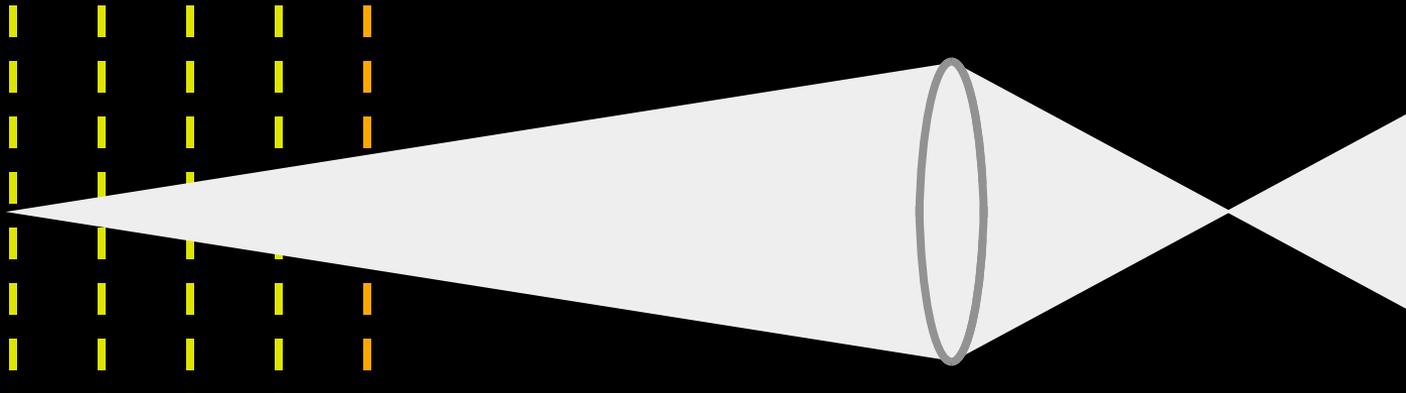
Lens



Camera sensor

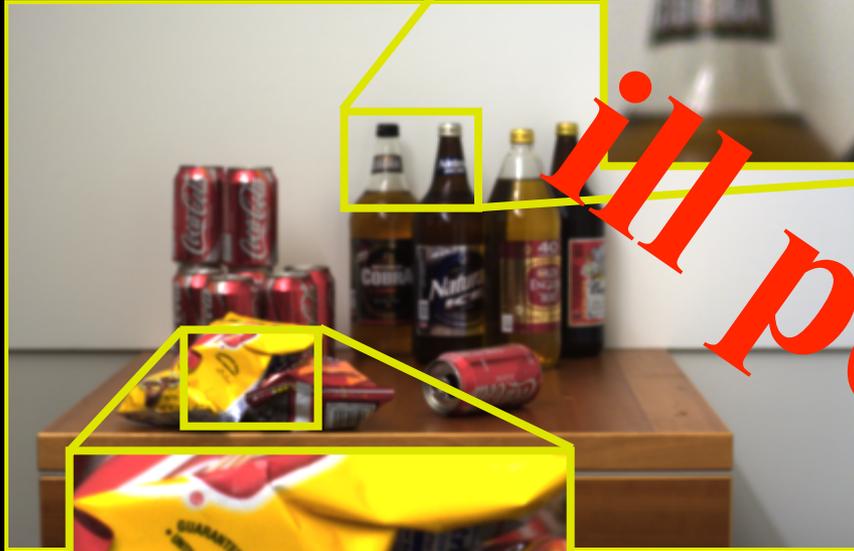


Point spread function



Depth and defocus

Out of focus



In focus



Depth from defocus:

Infer depth by analyzing local scale of defocus blur

ill posed

Challenges

- Hard to discriminate a smooth scene from defocus blur

?

Out of focus



- Hard to undo defocus blur



Input



Ringing with conventional deblurring algorithm

Key ideas

- **Exploit prior on natural images**

- Improve deconvolution
- Improve depth discrimination



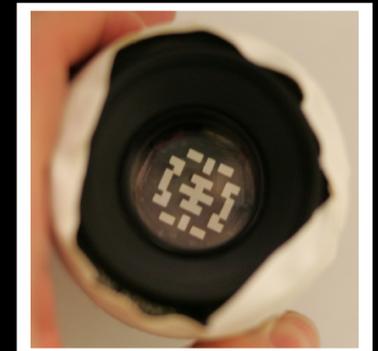
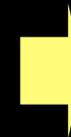
Natural



Unnatural

- **Coded aperture (mask inside lens)**

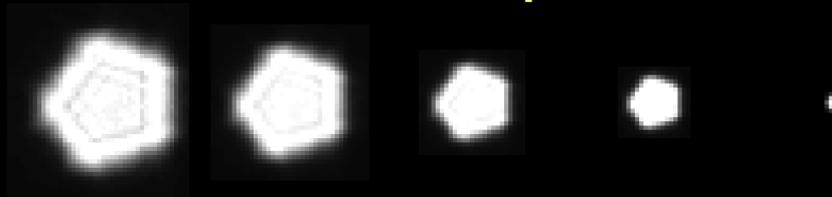
- make defocus patterns different from natural images and easier to discriminate



Defocus as local convolution



Calibrated blur kernels at different depths



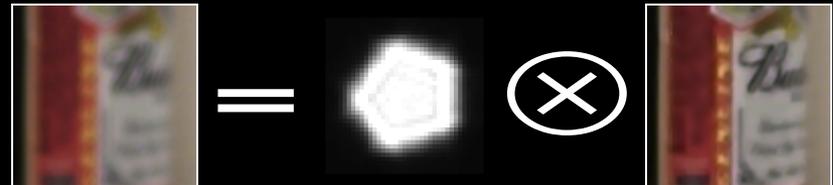
Defocus as local convolution



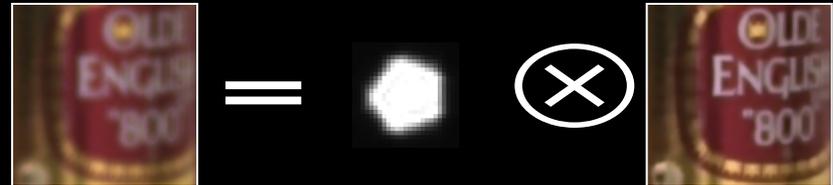
$$y = f_k \otimes x$$

Local sub-window Calibrated blur kernels at depth k Sharp sub-window

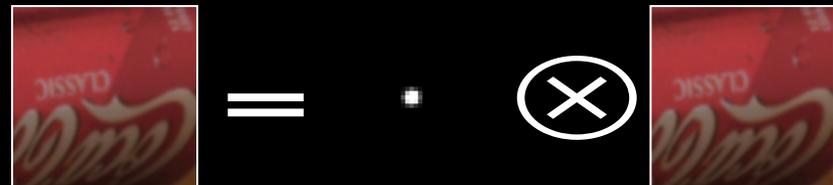
Depth $k=1$:



Depth $k=2$:

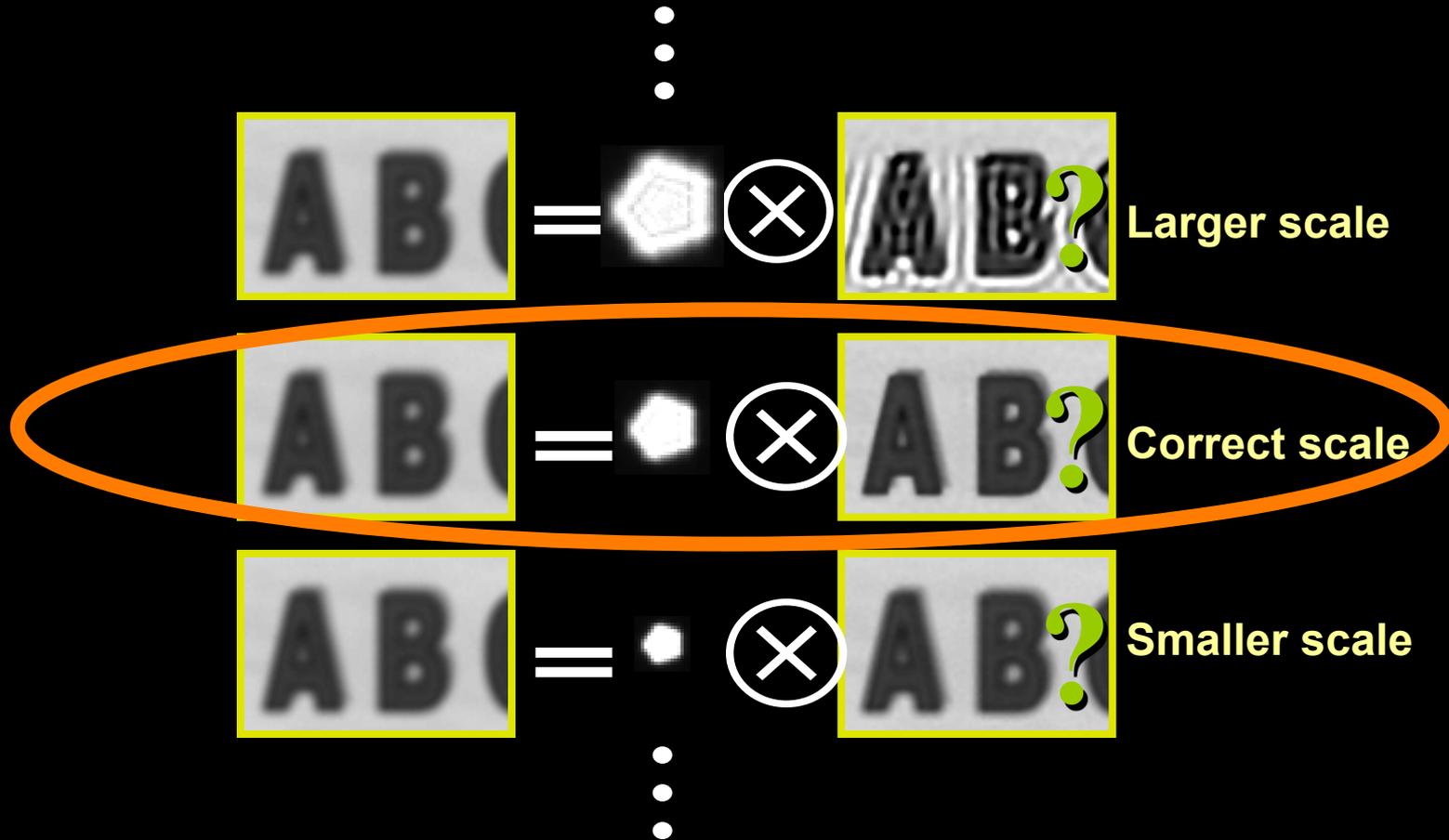


Depth $k=3$:



Overview

Try deconvolving local input windows with different scaled filters:



Somehow: select best scale.

Challenges

- Hard to deconvolve even when kernel is known



Input

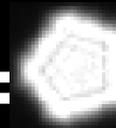


Ringing with the traditional Richardson-Lucy deconvolution algorithm

- Hard to identify correct scale:



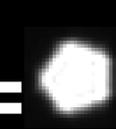
=



Larger scale



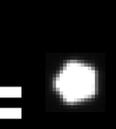
=



Correct scale



=

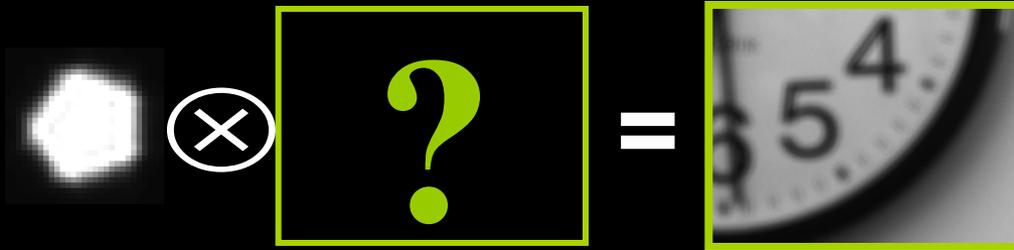


Smaller scale



Deconvolution is ill posed

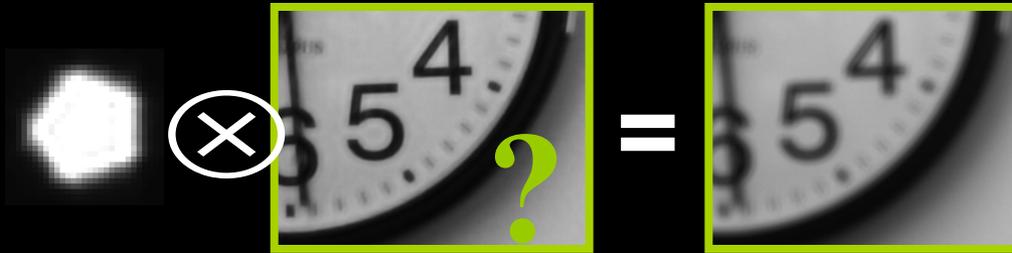
$$f \otimes x = y$$



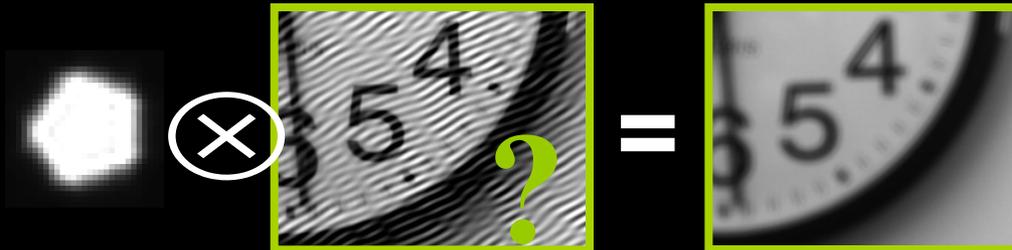
Deconvolution is ill posed

$$f \otimes x = y$$

Solution 1:

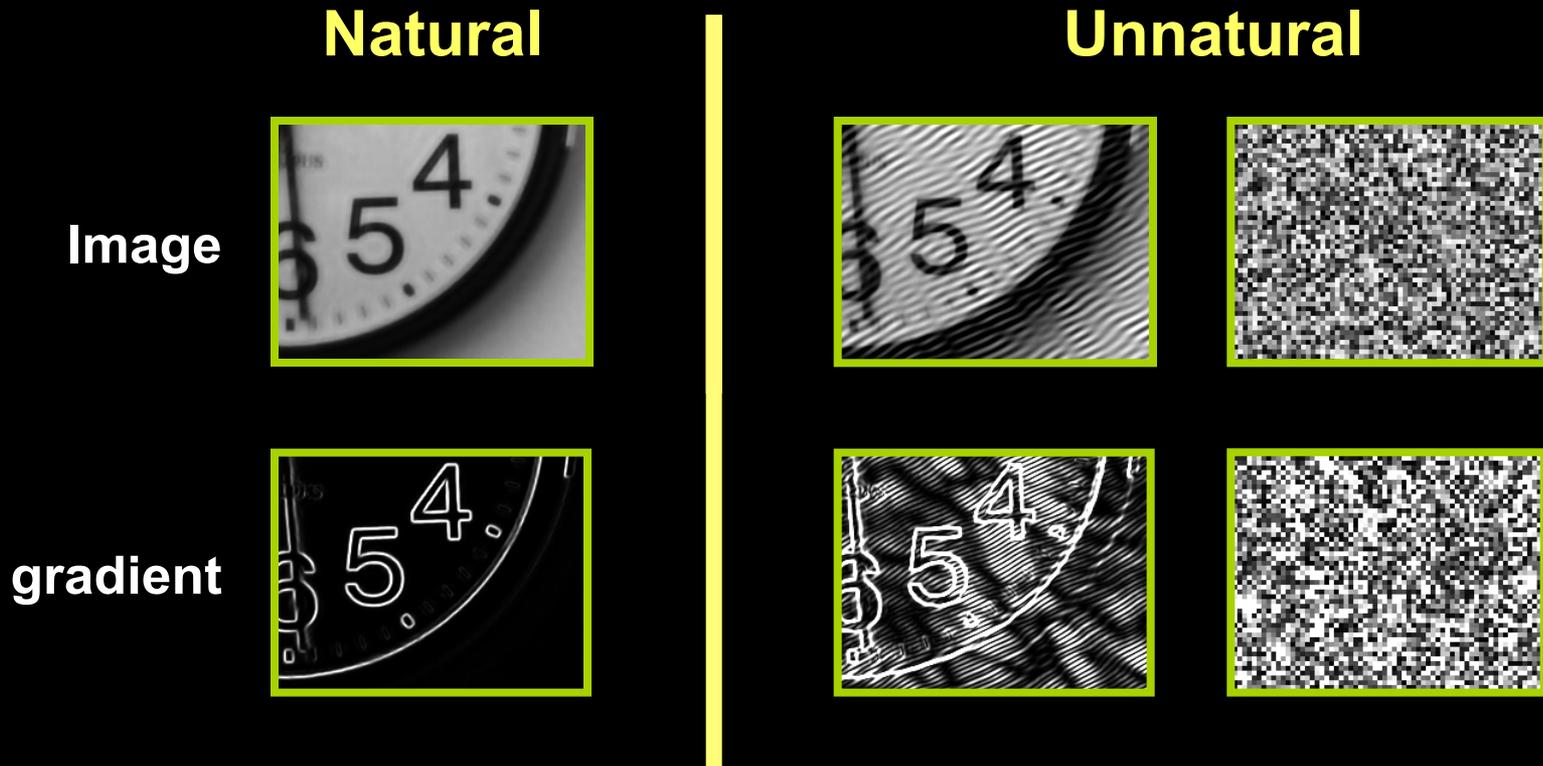


Solution 2:



Idea 1: Natural images prior

What makes images special?

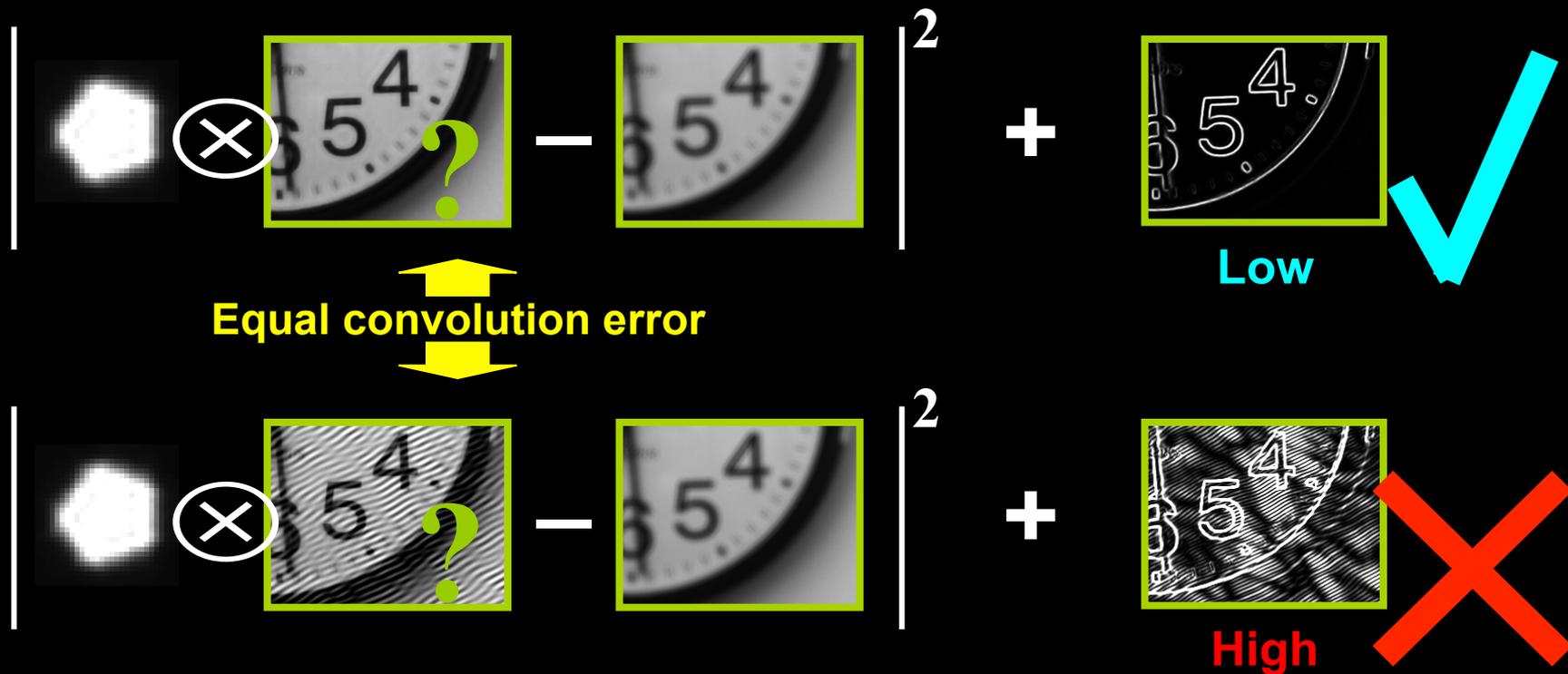


Natural images have sparse gradients

➡ put a penalty on gradients

Deconvolution with prior

$$x = \arg \min \underbrace{|f \otimes x - y|^2}_{\text{Convolution error}} + \lambda \underbrace{\sum_i \rho(\nabla x_i)}_{\text{Derivatives prior}}$$



Comparing deconvolution algorithms



Input

(Non blind) deconvolution code available online: <http://groups.csail.mit.edu/graphics/CodedAperture/>

$$\rho(\nabla x) = \|\nabla x\|^2$$

“spread” gradients

$$\rho(\nabla x) = \|\nabla x\|^{0.8}$$

“localizes” gradients



Richardson-Lucy



Gaussian prior



Sparse prior

Comparing deconvolution algorithms



Input

(Non blind) deconvolution code available online: <http://groups.csail.mit.edu/graphics/CodedAperture/>

$$\rho(\nabla x) = \|\nabla x\|^2$$

“spread” gradients

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“localizes” gradients



Richardson-Lucy



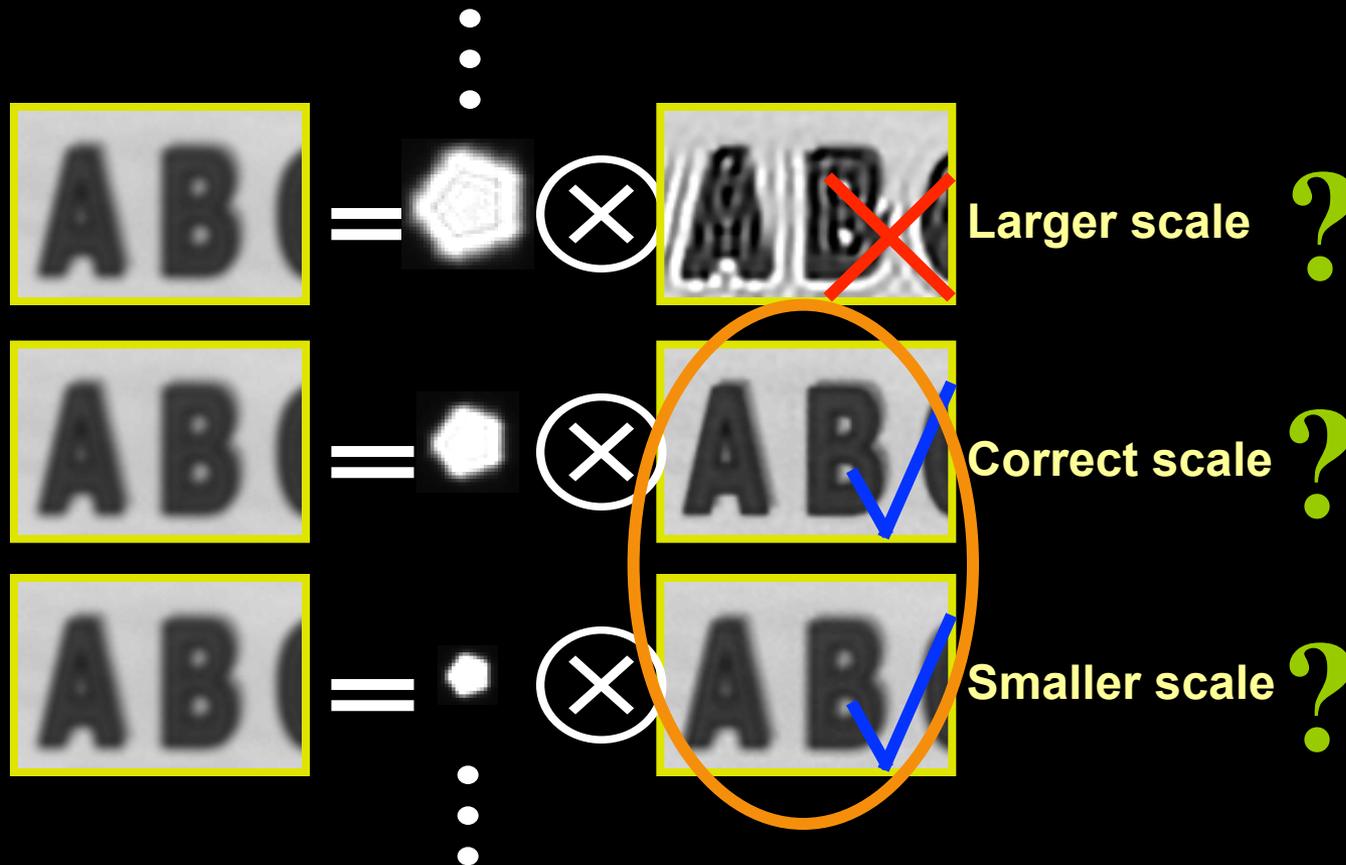
Gaussian prior



Sparse prior

Recall: Overview

Try deconvolving local input windows with different scaled filters:



Somehow: select best scale.

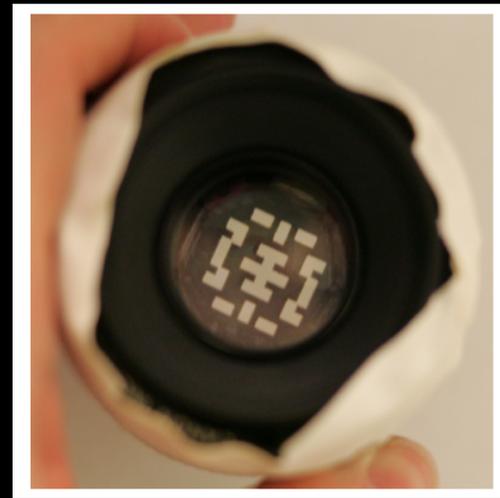
Challenge: smaller scale not so different than correct

Idea 2: Coded Aperture

- **Mask (code) in aperture plane**
 - make defocus patterns different from natural images and easier to discriminate



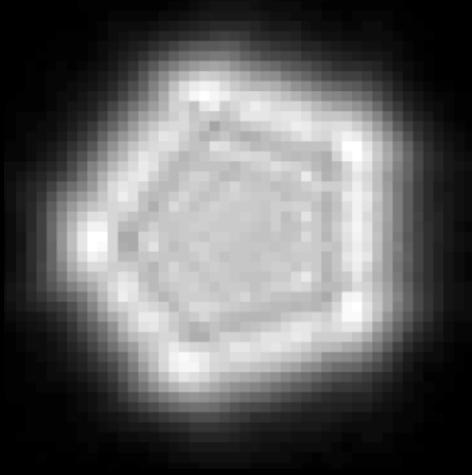
**Conventional
aperture**



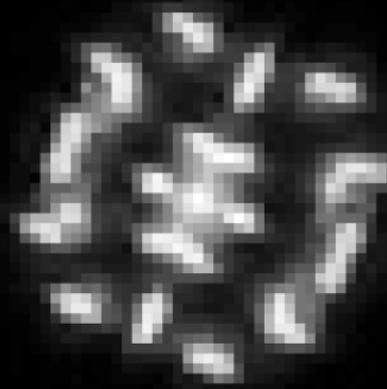
**Our coded
aperture**

Idea 2: Coded Aperture

- **Mask (code) in aperture plane**
 - make defocus patterns different from natural images and easier to discriminate



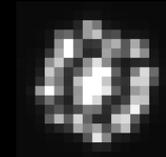
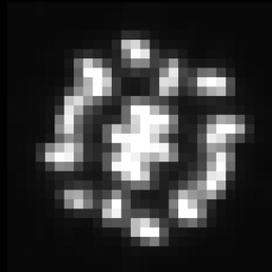
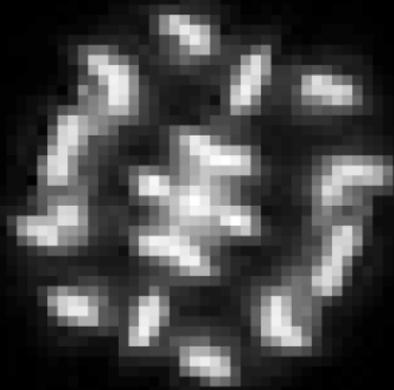
**Conventional
aperture**



**Coded
aperture**

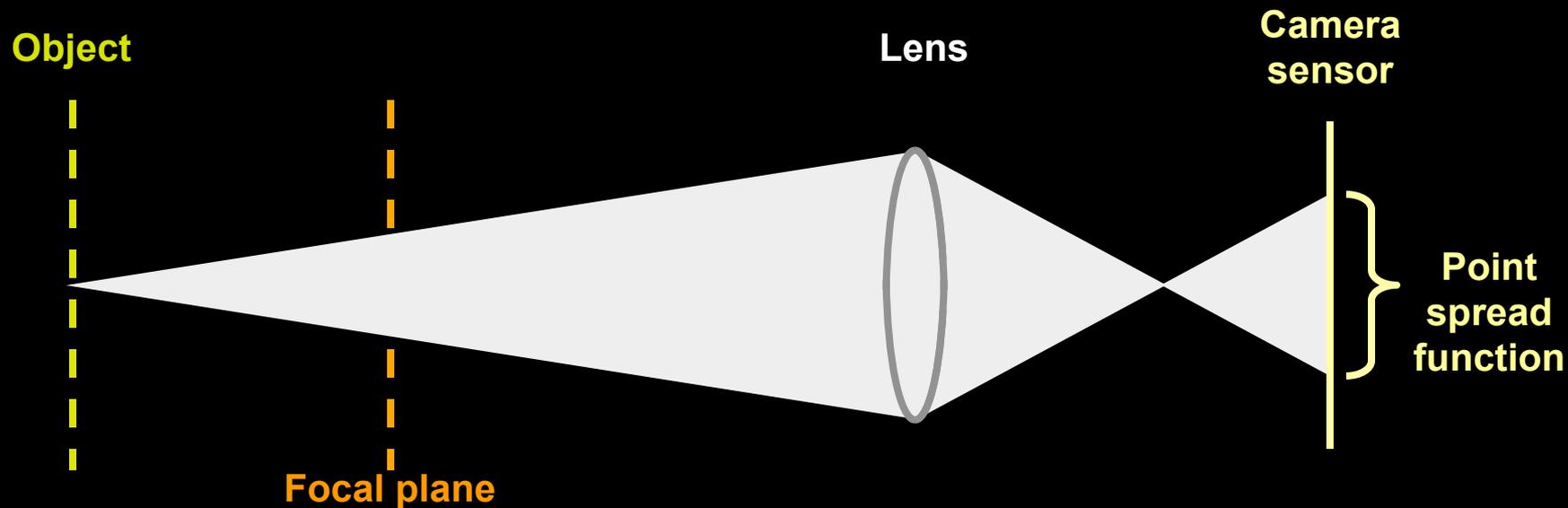
Idea 2: Coded Aperture

- **Mask (code) in aperture plane**
 - make defocus patterns different from natural images and easier to discriminate



**Coded
aperture**

Solution: lens with occluder



Solution: lens with occluder

Aperture pattern

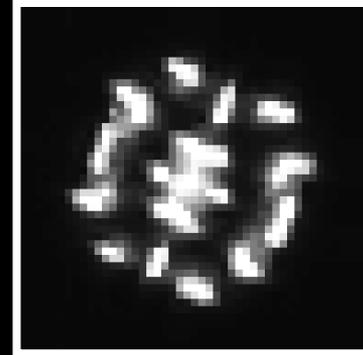
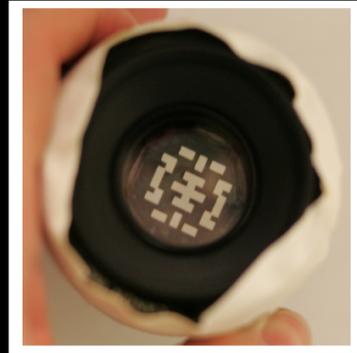
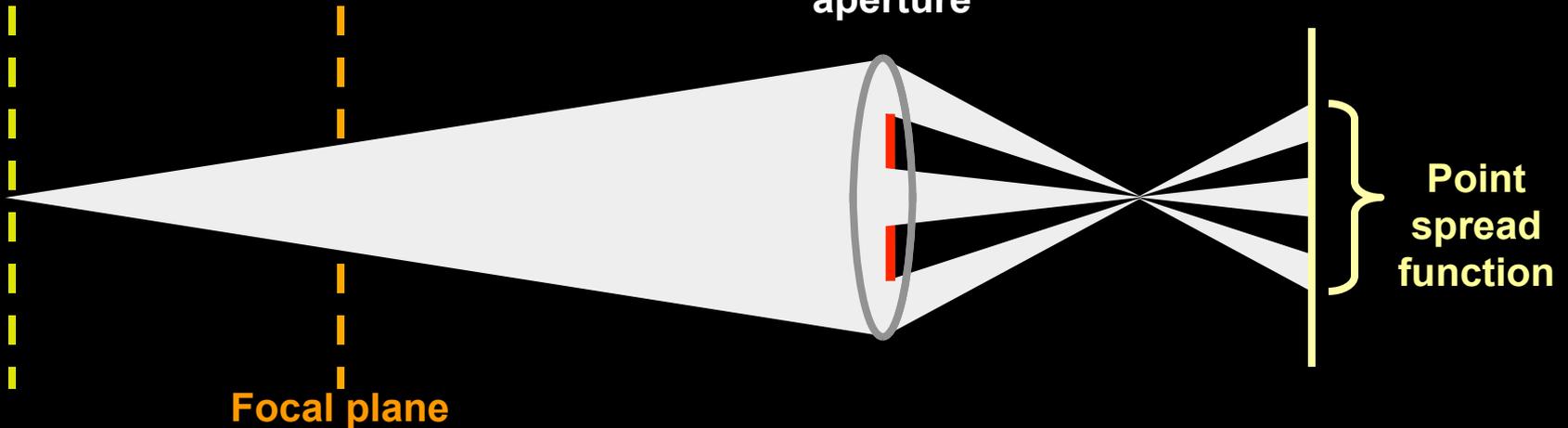


Image of a defocused point light source

Object

Lens with coded aperture

Camera sensor



Solution: lens with occluder

Aperture pattern

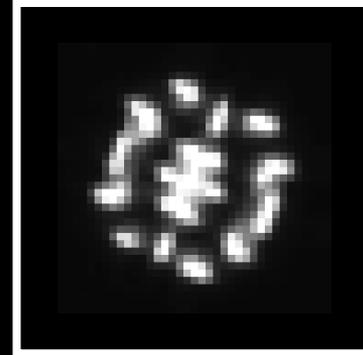
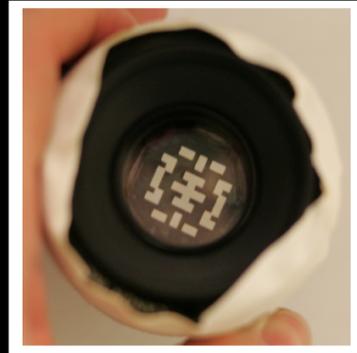
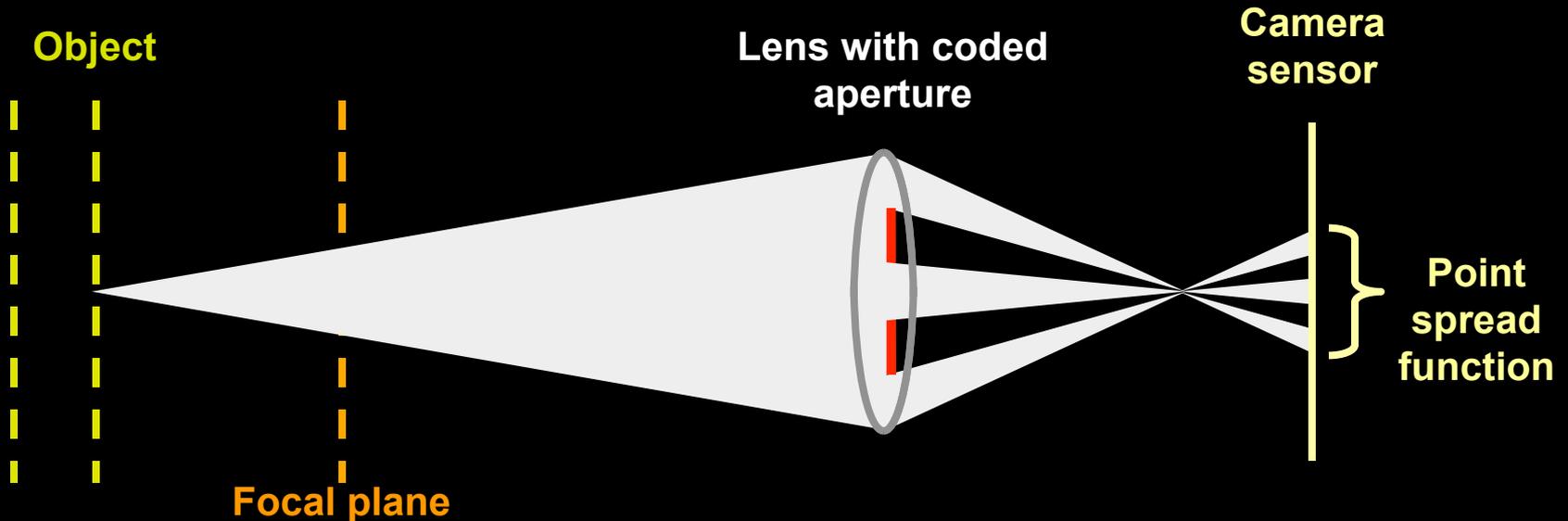


Image of a defocused point light source



Solution: lens with occluder

Aperture pattern

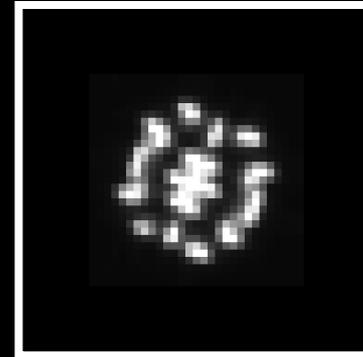
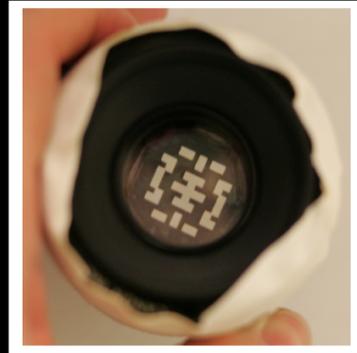
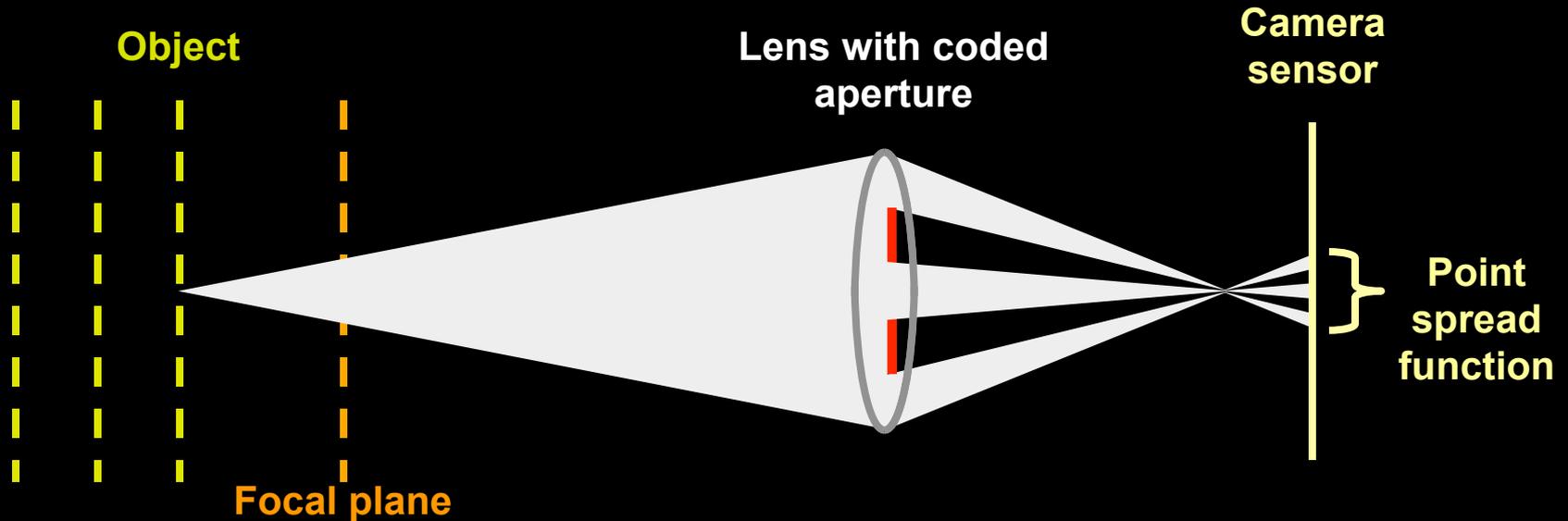


Image of a defocused point light source



Solution: lens with occluder

Aperture pattern

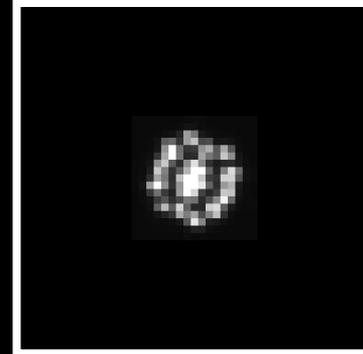
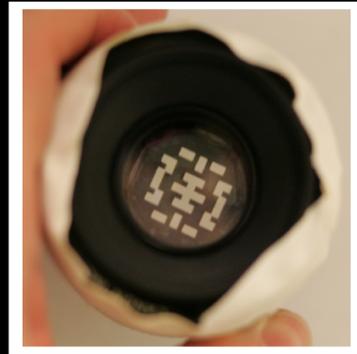
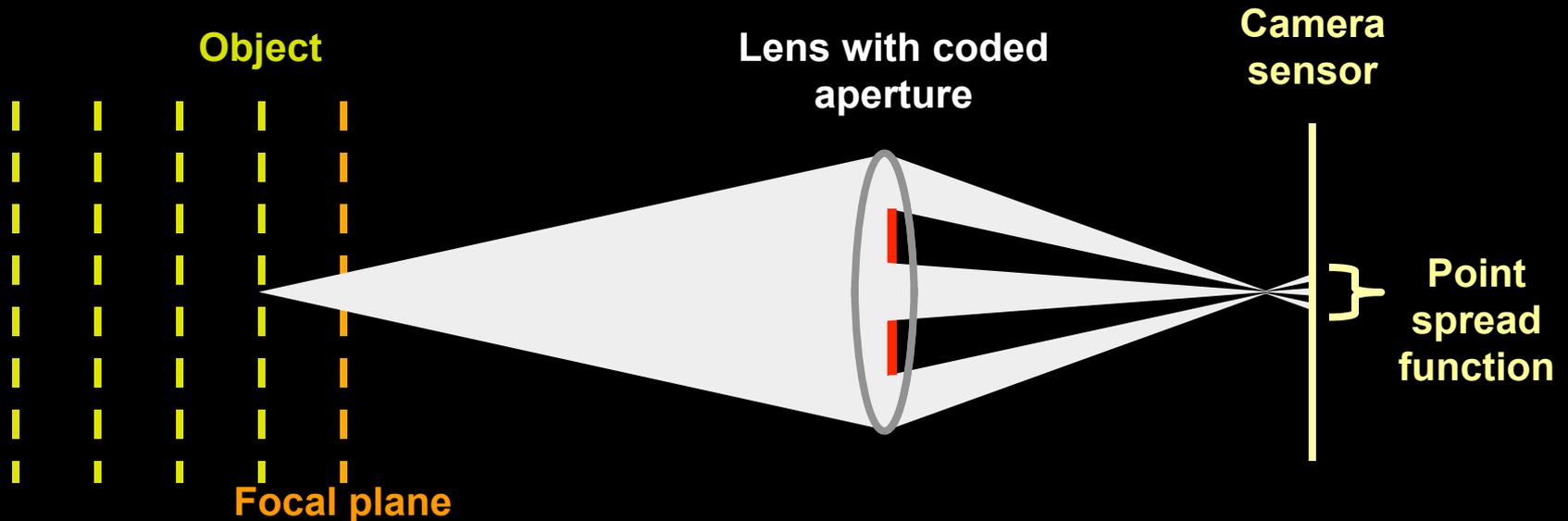


Image of a defocused point light source



Solution: lens with occluder

Aperture pattern

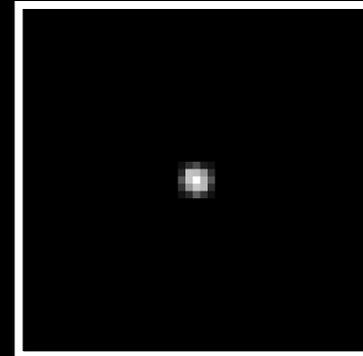
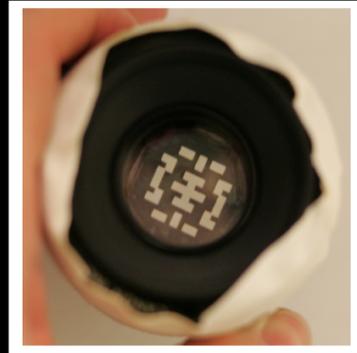
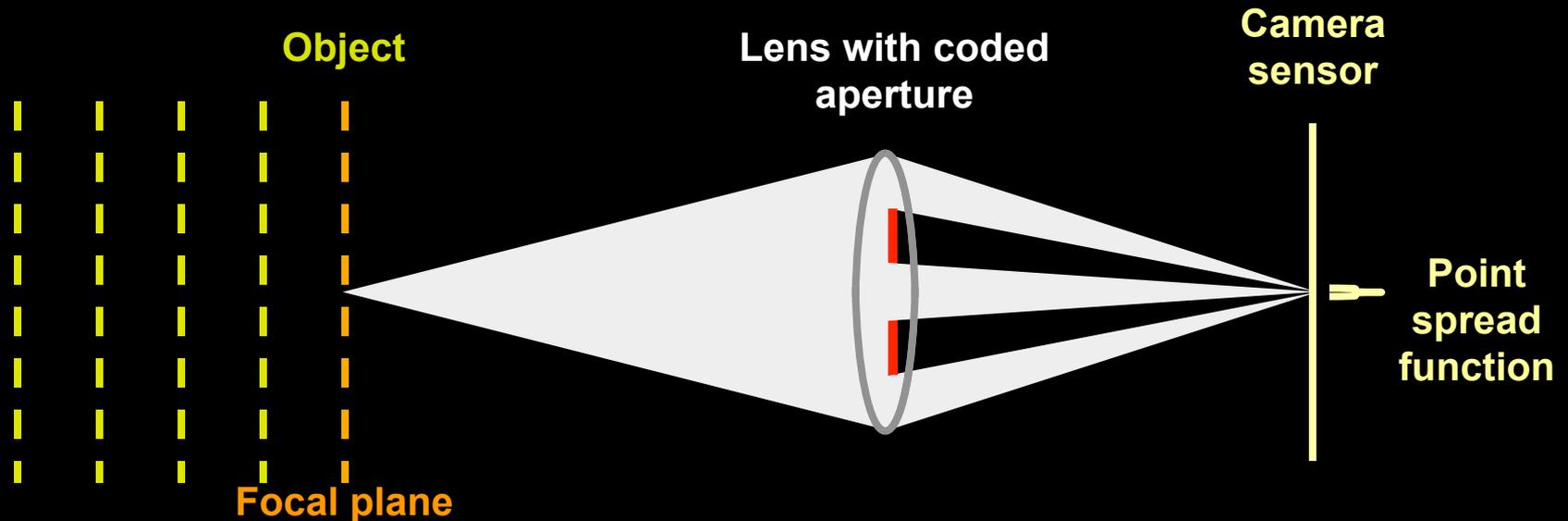


Image of a defocused point light source

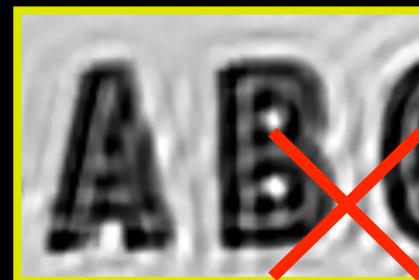
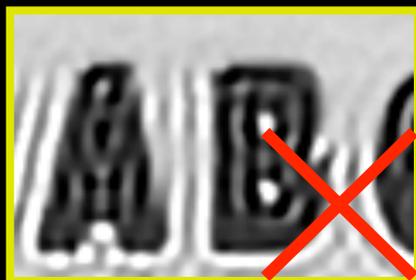
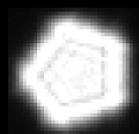


Coded aperture reduces uncertainty in scale identification

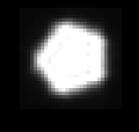
Conventional

Coded

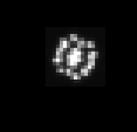
Larger scale



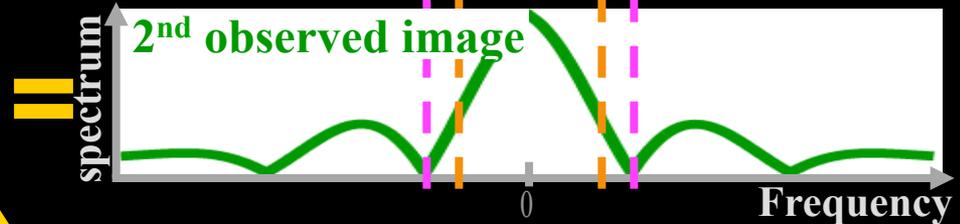
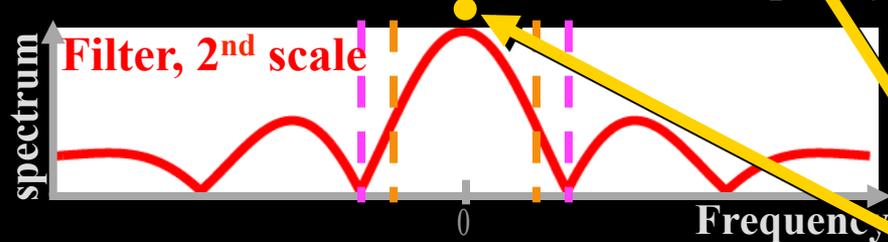
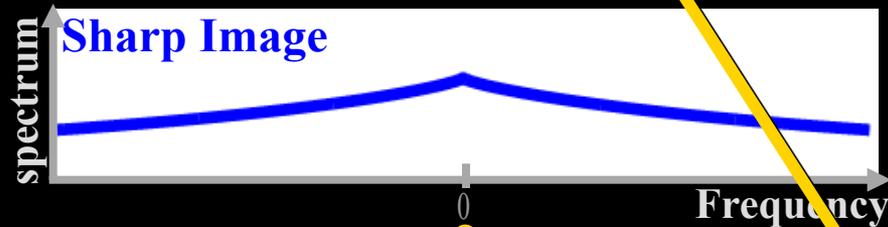
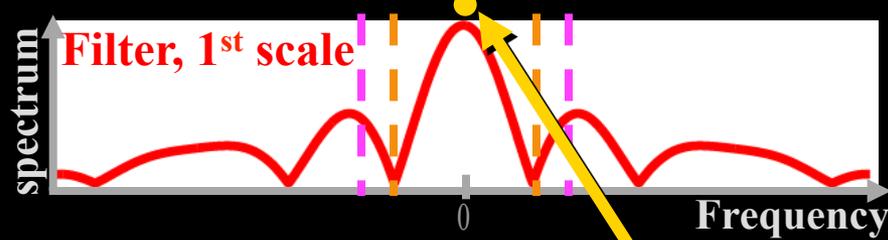
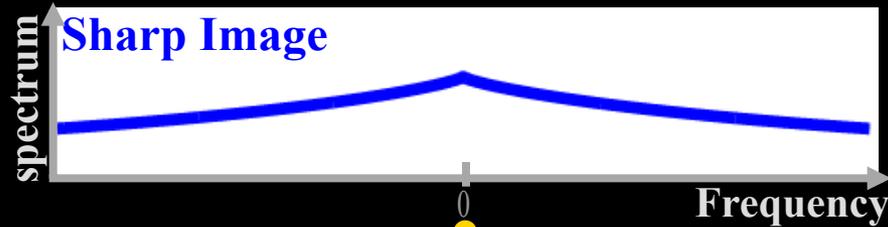
Correct scale



Smaller scale



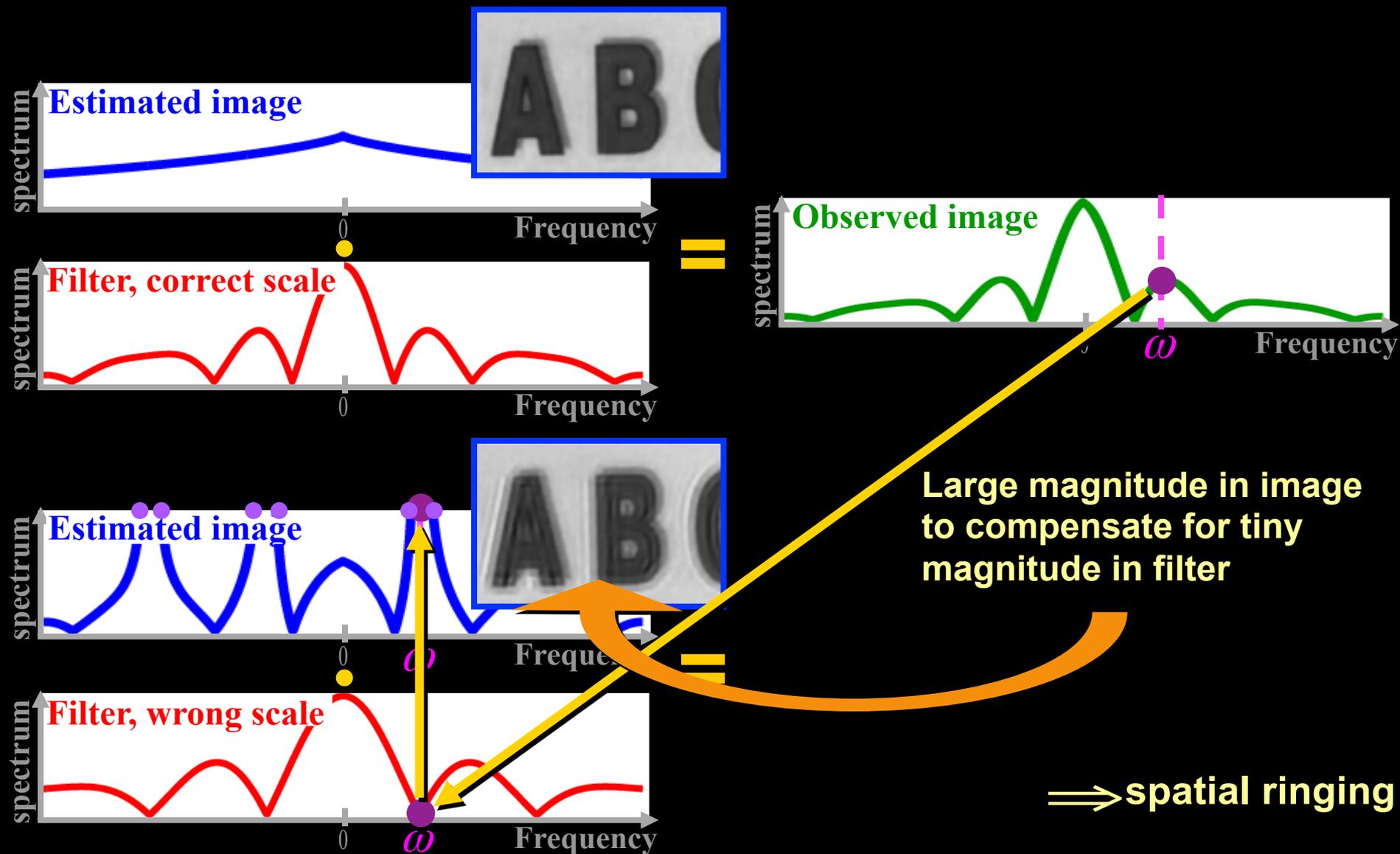
Convolution- frequency domain representation



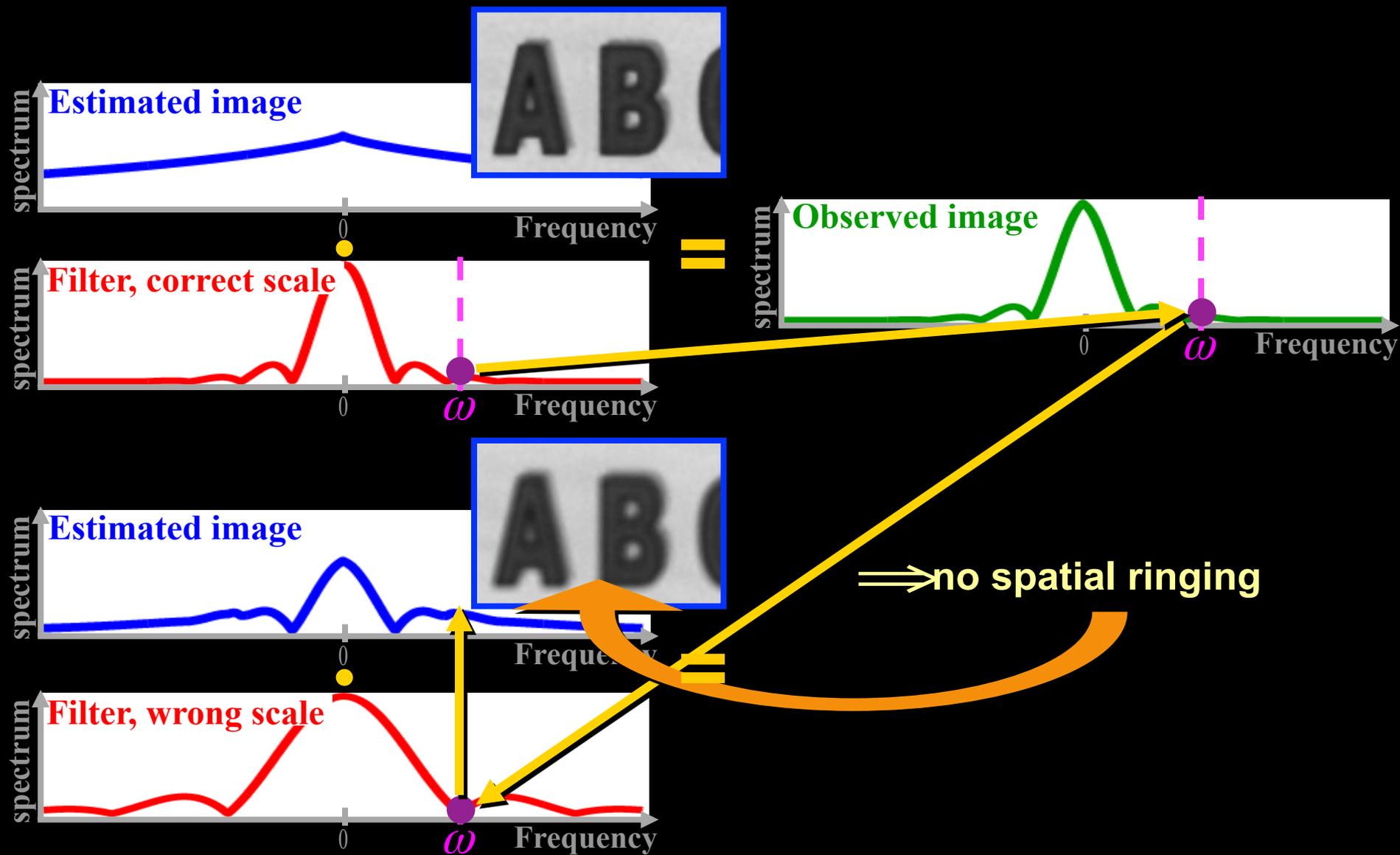
Spatial convolution \iff frequency multiplication

Output spectrum has zeros where filter spectrum has zeros

Coded aperture: Scale estimation and division by zero



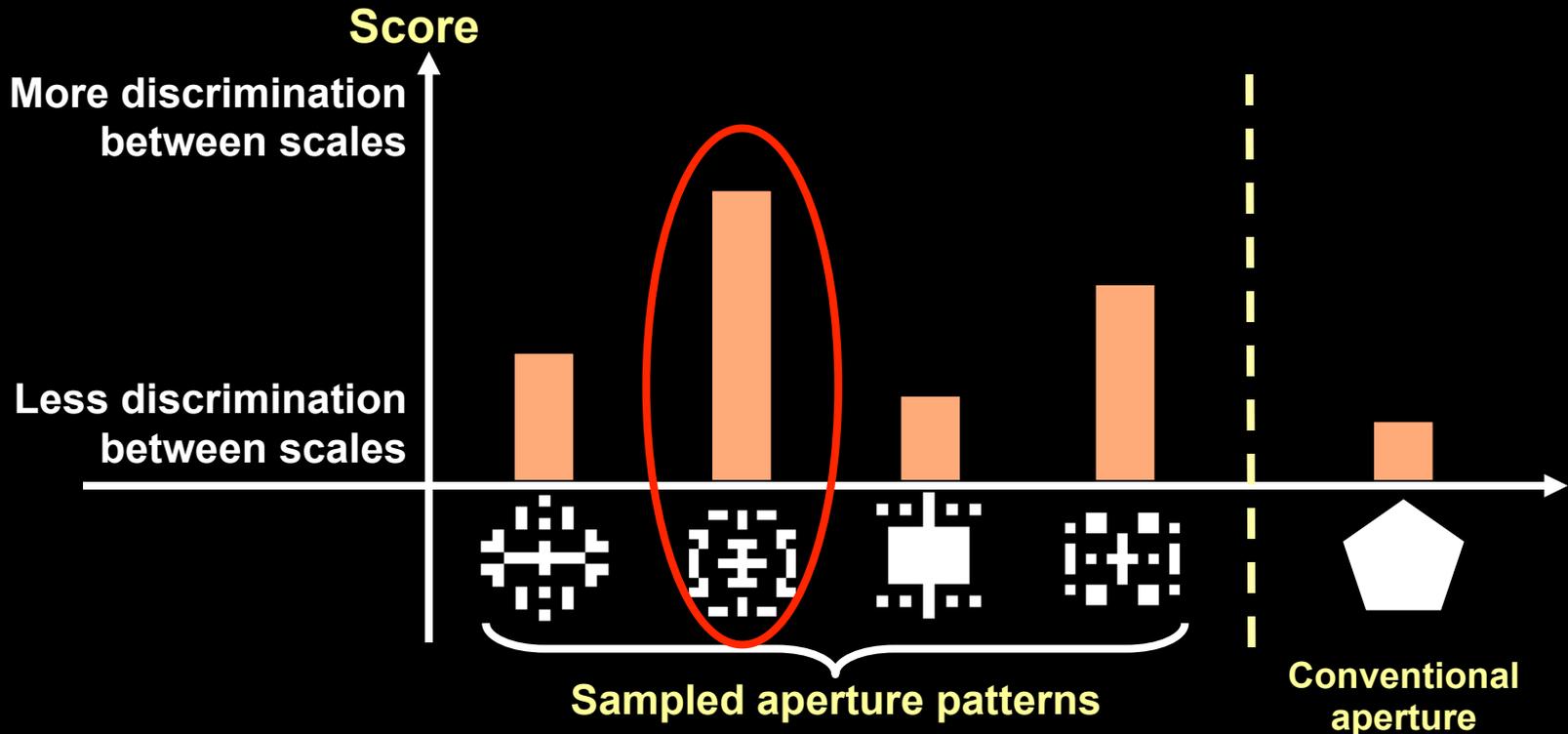
Division by zero with a conventional aperture?



Filter Design

Analytically search for a pattern maximizing discrimination between images at different defocus scales (*KL-divergence*)

Account for image prior and physical constraints



Depth results

Regularizing depth estimation

Try deblurring with 10 different aperture scales

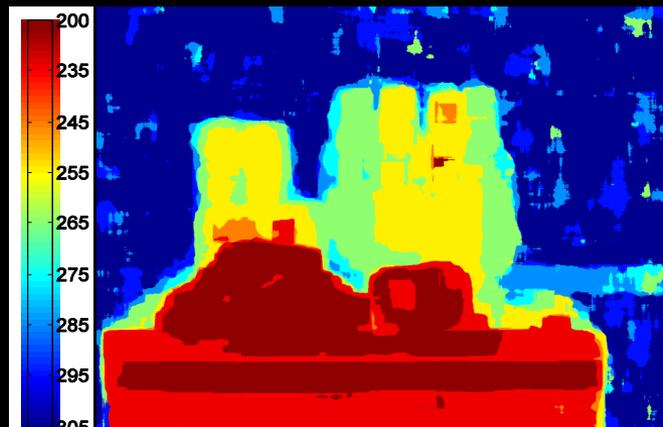
$$x = \arg \min \underbrace{|f \otimes x - y|^2}_{\text{Convolution error}} + \lambda \underbrace{\sum_i \rho(\nabla x_i)}_{\text{Derivatives prior}}$$

The diagram illustrates the components of the optimization equation. On the left, a blurred image of a clock face is convolved with a kernel (represented by a circle with an 'x') to produce a sharper image. This is labeled as the convolution error. On the right, a sharp image of a clock face is shown with a green border, representing the derivatives prior term.

Keep minimal error scale in each local window + regularization



Input



Local depth estimation

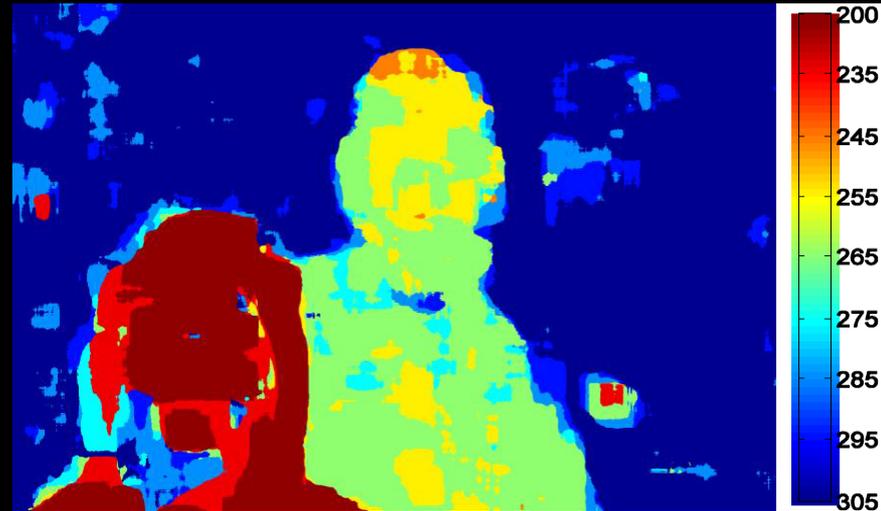


Regularized depth

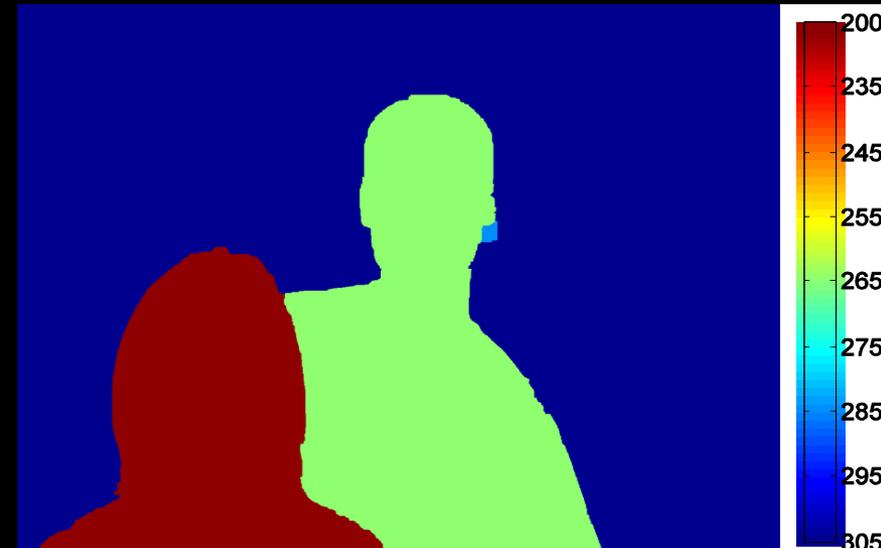
Regularizing depth estimation



Input



Local depth estimation



Regularized depth

All focused results

Input



All-focused (deconvolved)



Close-up

Original image



All-focus image



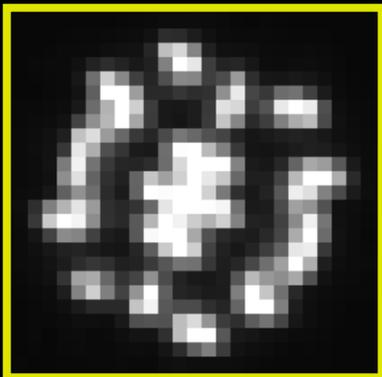
Comparison- conventional aperture result



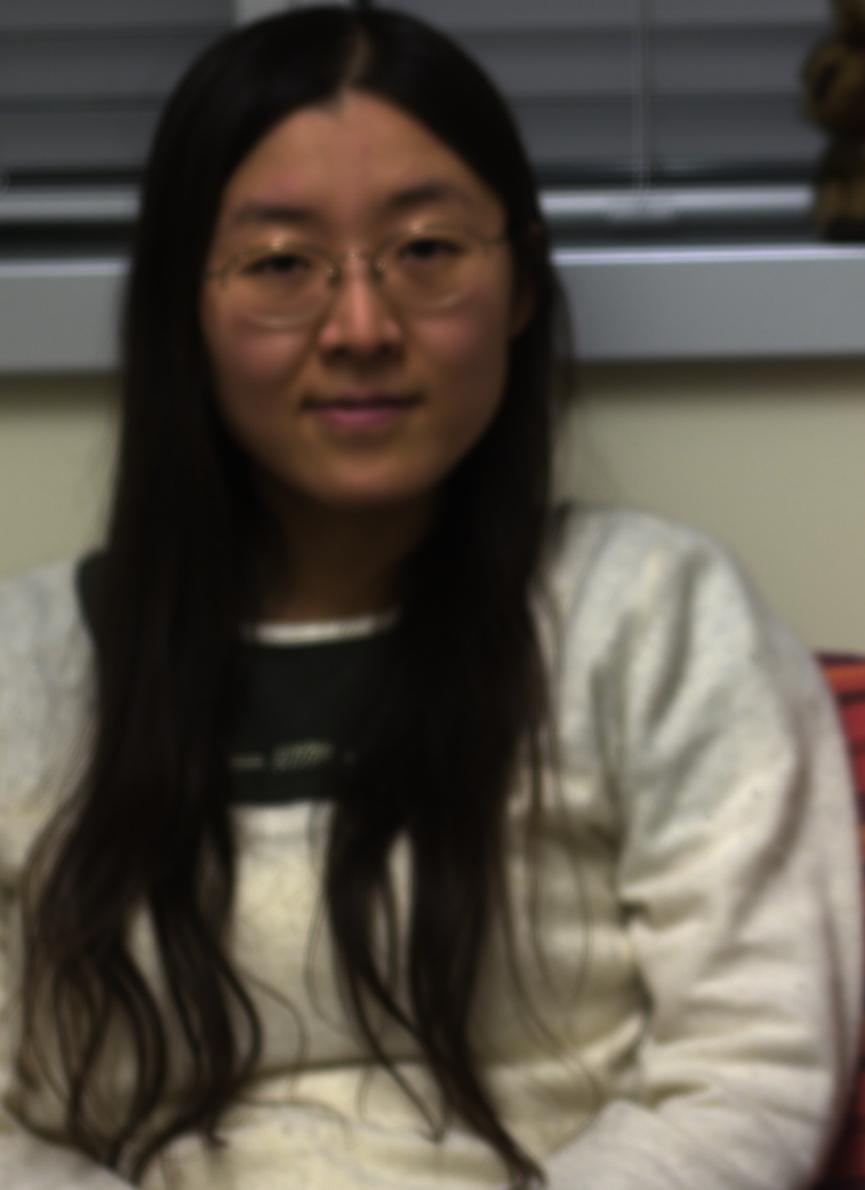
Ringing due to wrong scale estimation



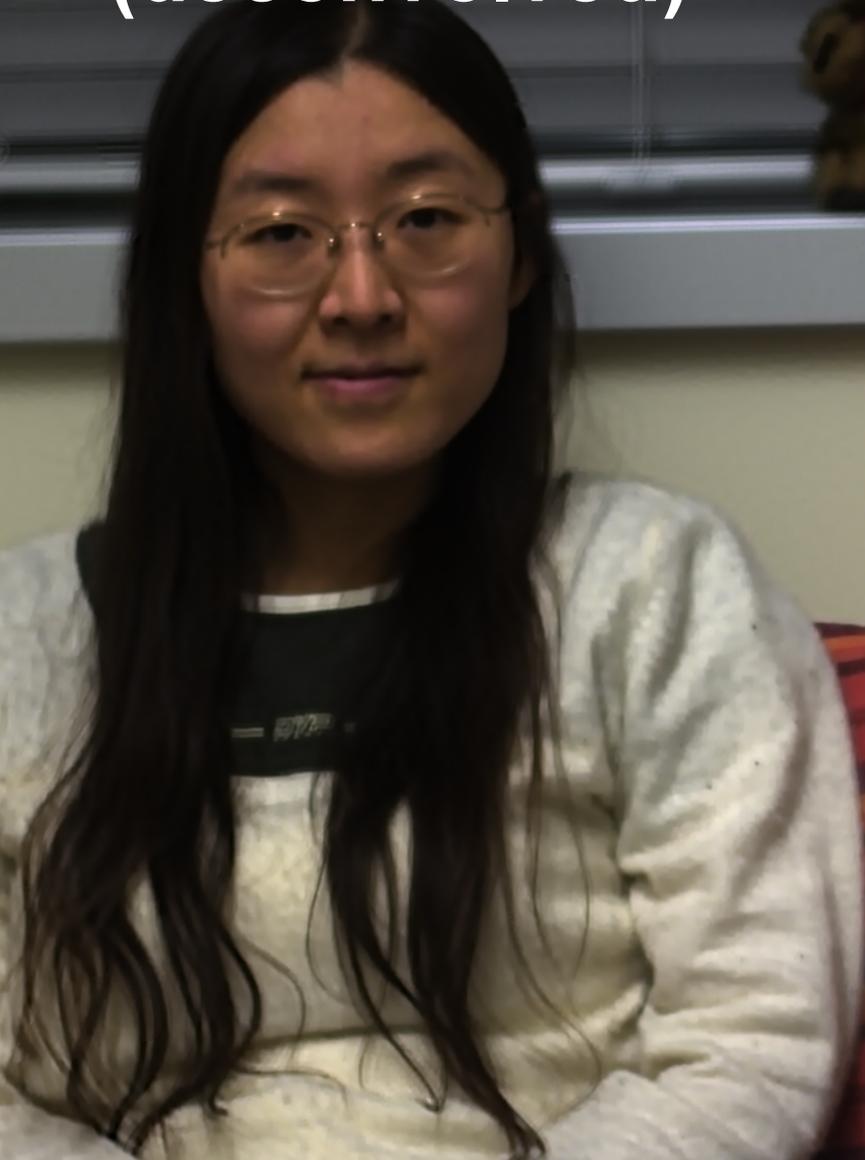
Comparison- coded aperture result



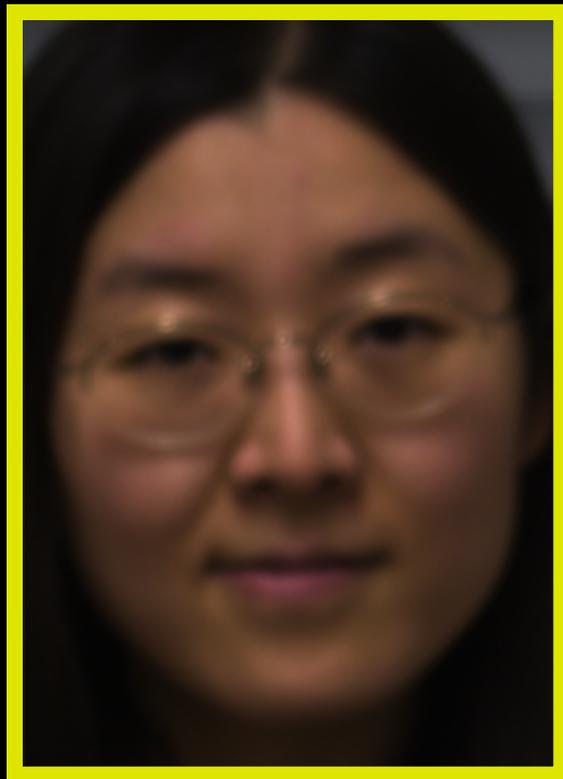
Input



**All-focused
(deconvolved)**



Close-up



Original image



All-focus image

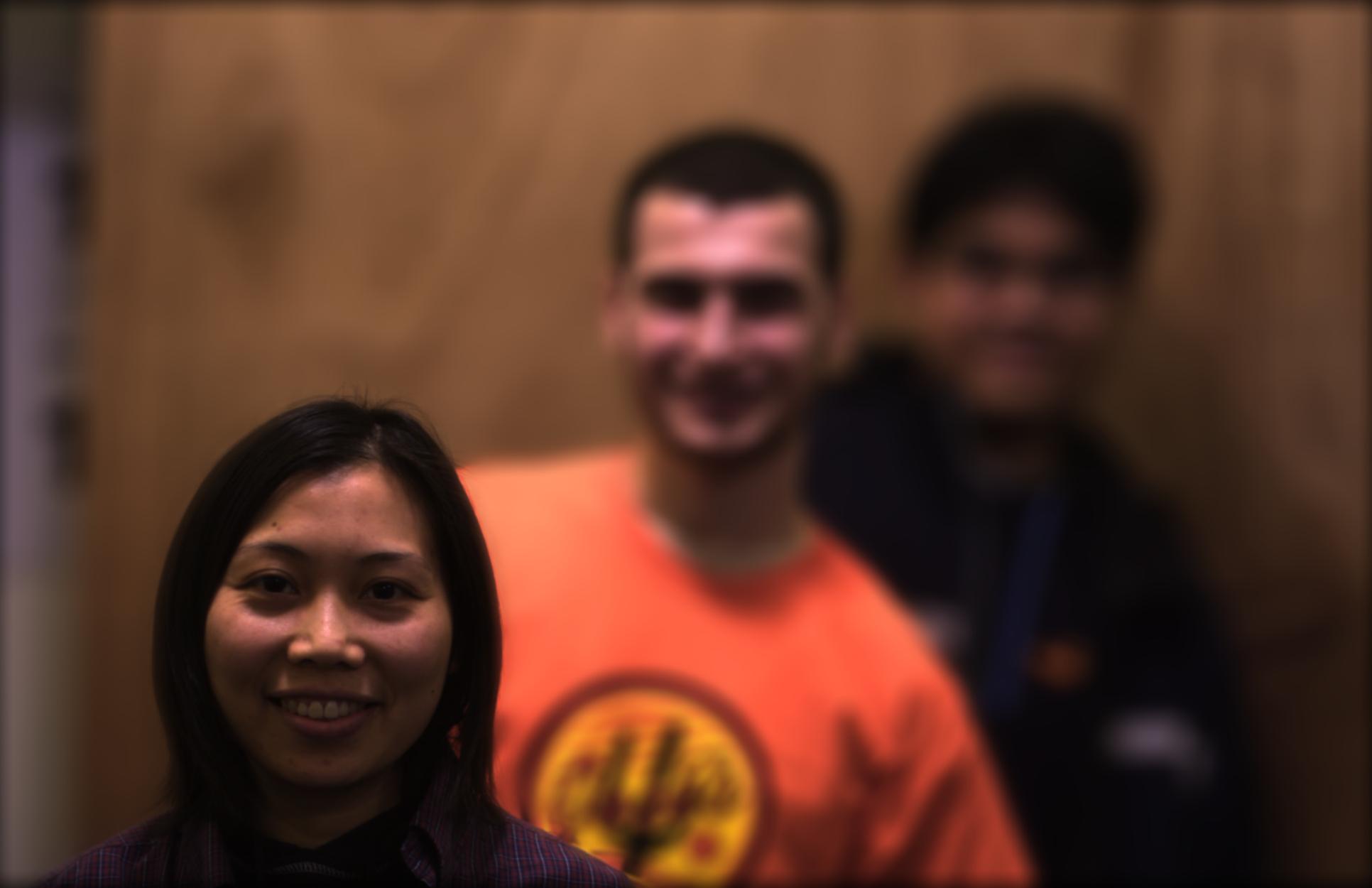


Naïve sharpening

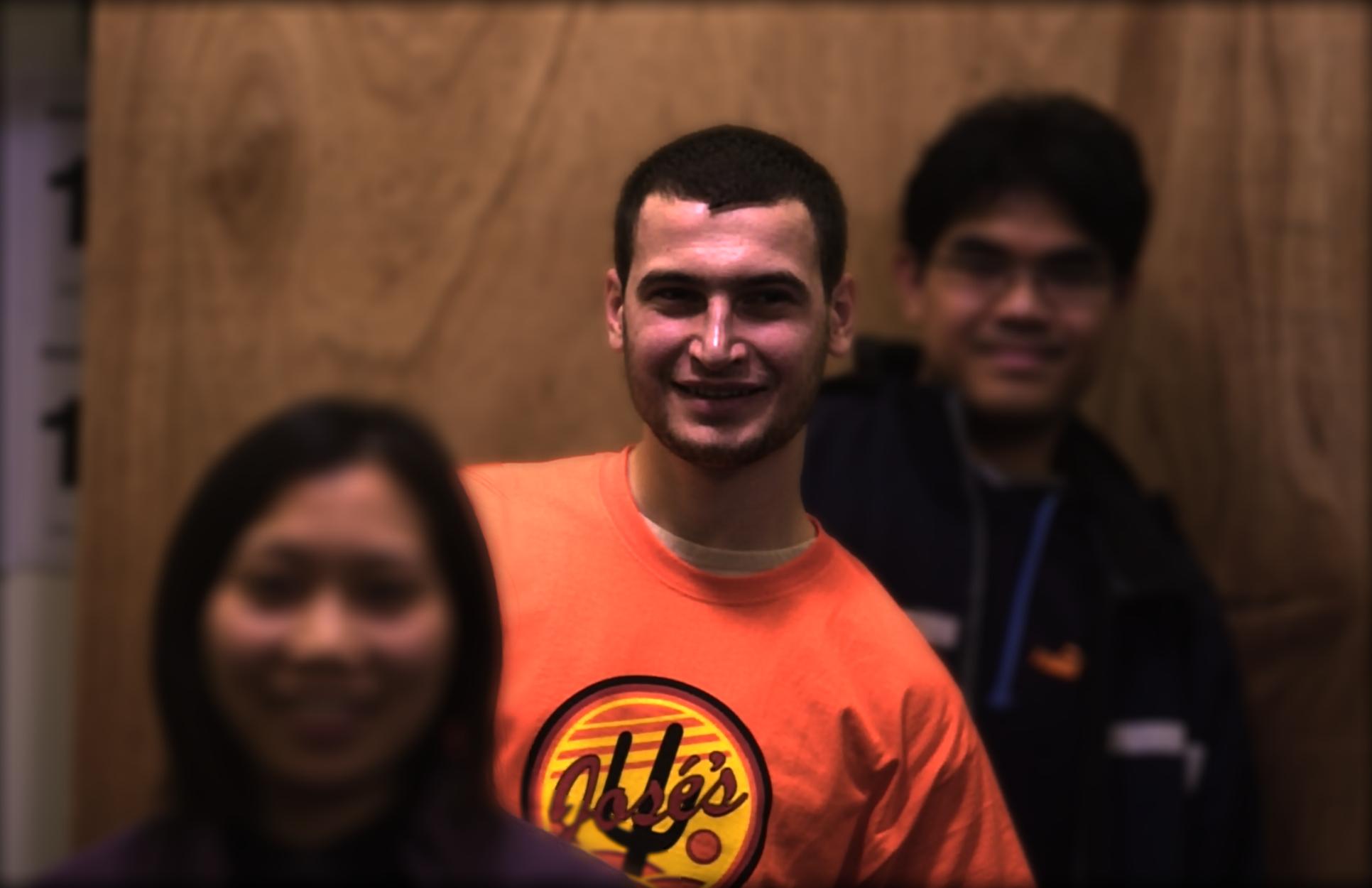
Application: Digital refocusing from a single image



Application: Digital refocusing from a single image



Application: Digital refocusing from a single image



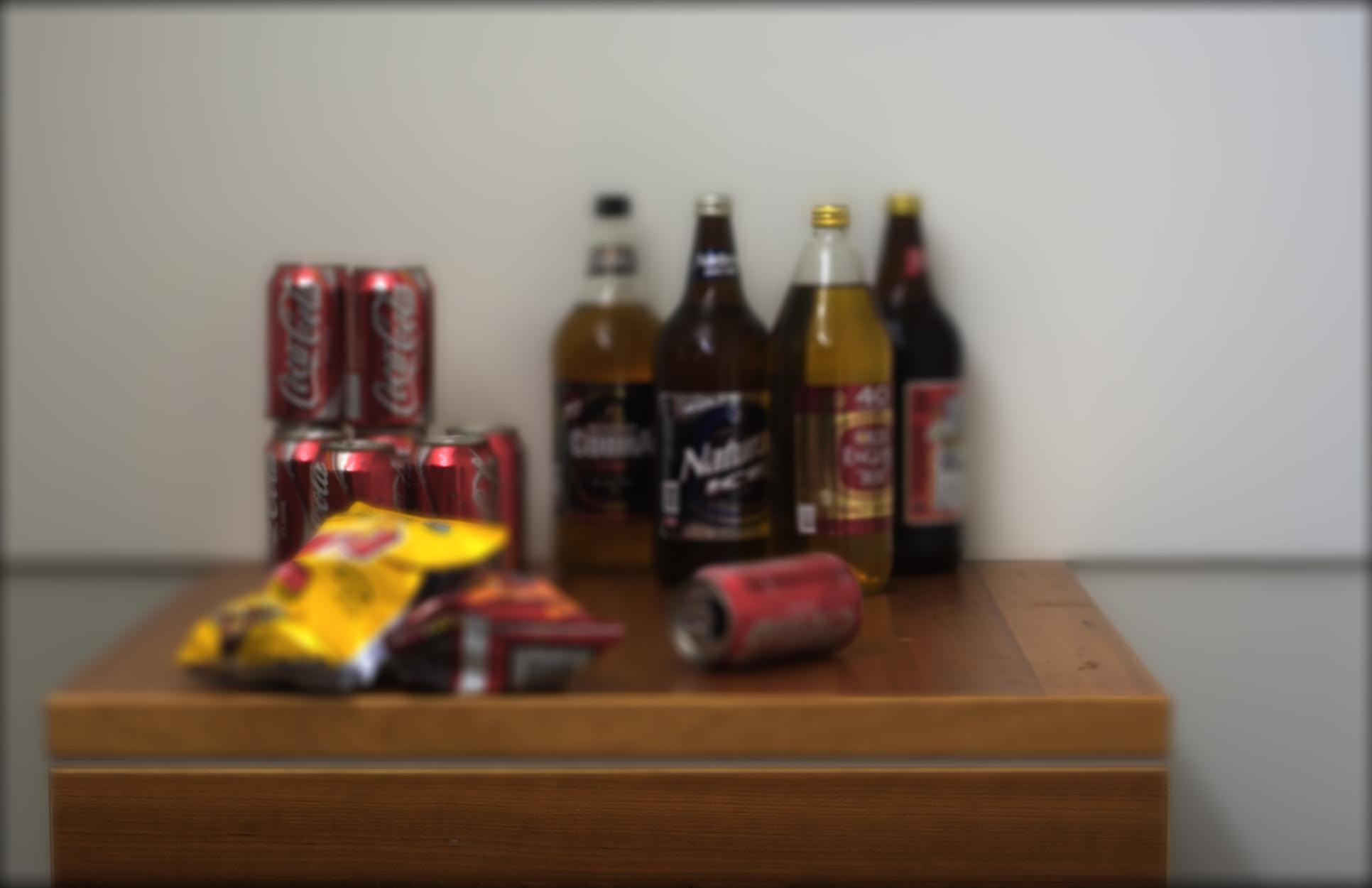
Application: Digital refocusing from a single image



Application: Digital refocusing from a single image



Application: Digital refocusing from a single image

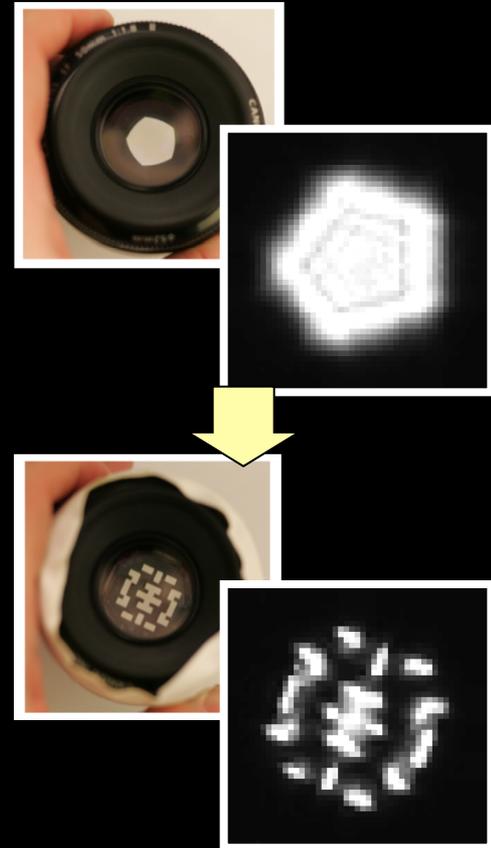


Application: Digital refocusing from a single image



Coded aperture: pros and cons

- + Image AND depth at a single shot
- + No loss of image resolution
- + Simple modification to lens
- Depth is coarse
 - unable to get depth at untextured areas, might need manual corrections.
- + But depth is a pure bonus
- Lose some light
- + But deconvolution increases depth of field





50mm f/1.8: \$79.95

Cardboard: \$1

Tape: \$1

Depth acquisition: priceless



Some more quick examples

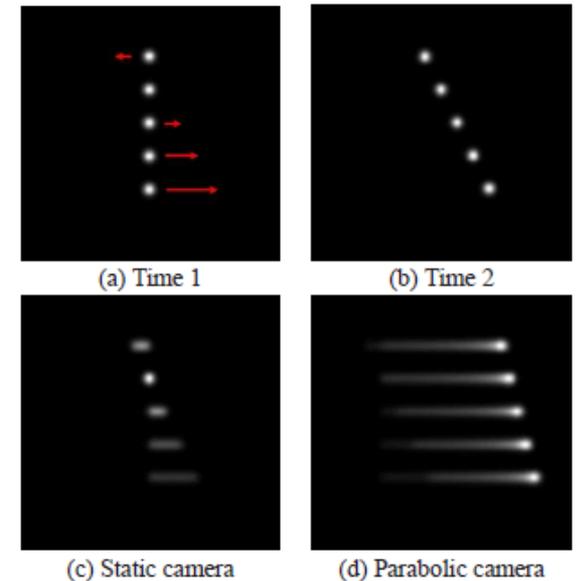
Motion-Invariant Photography

Anat Levin Peter Sand Taeg Sang Cho Frédo Durand William T. Freeman

Massachusetts Institute of Technology, Computer Science and Artificial Intelligence Laboratory



- Quickly move camera in a parabola when taking a picture
- A motion at any speed in the direction of the parabola will give the same blur kernel

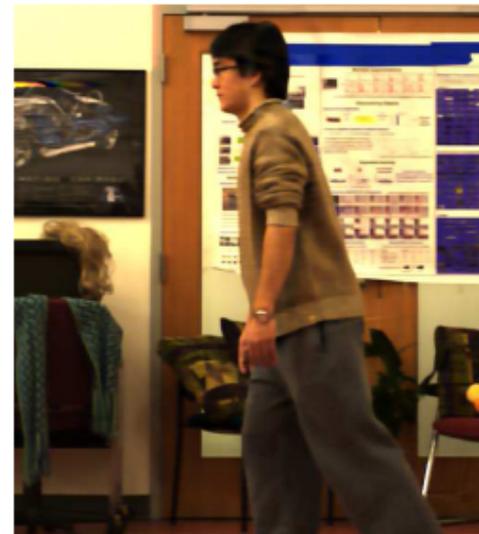


Results

Static
Camera



Parabolic
Camera



Results

Static Camera



Parabolic Camera



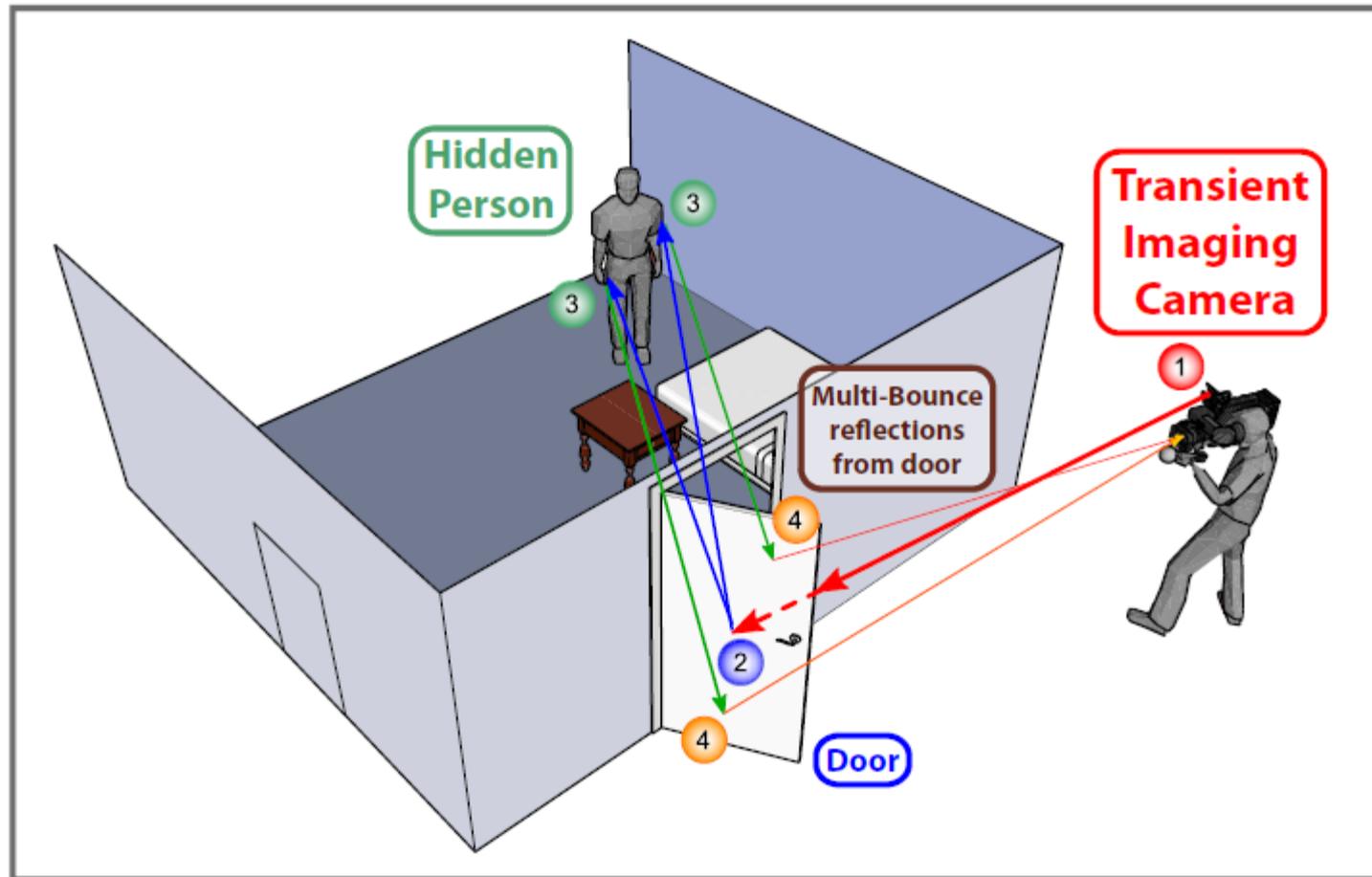
Motion in
wrong
direction

Looking Around the Corner using Transient Imaging

Ahmed Kirmani ^{*1}, Tyler Hutchison¹, James Davis ^{†2}, and Ramesh Raskar^{‡1}

¹MIT Media Laboratory

² UC Santa Cruz



Recap of questions

- How can we represent all of the information contained in light?
- What are the fundamental limitations of cameras?
- What sacrifices have we made in conventional cameras? For what benefits?
- How else can we design cameras for better focus, deblurring, multiple views, depth, etc.?

Next class

- Exam review

