Appendix C: Pipelining: Basic and Intermediate Concepts

Key ideas and simple pipeline (Section C.1)
Hazards (Sections C.2 and C.3)
  Structural hazards
  Data hazards
  Control hazards
Exceptions (Section C.4)
Multicycle operations (Section C.5)
Pipelining - Key Idea

Ideally,

\[ Time_{\text{pipeline}} = \frac{Time_{\text{sequential}}}{\text{Pipeline Depth}} \]

\[ \text{Speedup} = \frac{Time_{\text{sequential}}}{Time_{\text{pipeline}}} = \text{Pipeline Depth} \]
Consider an instruction that requires $n$ stages $s_1, s_2, \ldots, s_n$, taking time $t_1, t_2, \ldots, t_n$.

Let $T = \sum t_i$

Without pipelining

Throughput = 

Latency = 

Speedup

With an n-stage pipeline

Throughput = 

Latency =
Consider an instruction that requires \( n \) stages 
\( s_1, s_2, \ldots, s_n \), taking time \( t_1, t_2, \ldots, t_n \).

Let \( T = \sum t_i \)

Without pipelining

Throughput = \( \frac{1}{T} = \frac{1}{\sum t_i} \)

Latency =

Speedup

With an n-stage pipeline

Throughput = \( \frac{1}{\max t_i} \leq \frac{n}{T} \)

Latency =
Consider an instruction that requires \( n \) stages
\[ s_1, s_2, \ldots, s_n, \] taking time \( t_1, t_2, \ldots, t_n \).

Let \( T = \sum t_i \)

**Without pipelining**

Throughput = \( \frac{1}{T} = \frac{1}{\sum t_i} \)

Latency = \( T = \frac{1}{\text{Throughput}} \)

**With an n-stage pipeline**

Throughput = \( \frac{1}{\max t_i} \leq \frac{n}{T} \)

Latency = \( n \times \max t_i \geq T \)

Speedup
Consider an instruction that requires $n$ stages $s_1, s_2, \ldots, s_n$, taking time $t_1, t_2, \ldots, t_n$.

Let $T = \sum t_i$

Without pipelining

Throughput = \( \frac{1}{T} = \frac{1}{\sum t_i} \)

Latency = \( T = \frac{1}{\text{Throughput}} \)

Speedup \leq \frac{\sum t_i}{\text{max } t_i} \leq n$

With an $n$-stage pipeline

Throughput = \( \frac{1}{\text{max } t_i} \leq \frac{n}{T} \)

Latency = \( n \times \text{max } t_i \geq T \)
Practical Limit 2 - Overheads

Let $\Delta > 0$ be extra delay per stage
e.g., latches
$\Delta$ limits the useful depth of a pipeline.

With an $n$ stage pipeline

$$Throughput = \frac{1}{\Delta + \max t_i} < \frac{n}{T}$$

$$Latency = n \times (\Delta + \max t_i) \geq n\Delta + T$$

$$Speedup = \frac{\sum t_i}{\Delta + \max t_i} < n$$
Example

Let $t_{1,2,3} = 8, 12, 10 \text{ ns}$ and $\Delta = 2 \text{ ns}$

Throughput =

Latency =

Speedup =
Example

Let \( t_{1,2,3} = 8, 12, 10 \) ns and \( \Delta = 2 \) ns

Throughput = \( 1/(2 \text{ ns} + 12 \text{ ns}) = 1/(14 \text{ ns}) \)

Latency =

Speedup =
Example

Let $t_{1,2,3} = 8, 12, 10\, ns$ and $\Delta = 2\, ns$

Throughput $= 1/(2\, ns + 12\, ns) = 1/(14\, ns)$

Latency $= 3\, (2\, ns + 12\, ns) = 42\, ns$

Speedup =
Example

Let \( t_{1,2,3} = 8, 12, 10 \text{ ns} \) and \( \Delta = 2 \text{ ns} \)

Throughput = \( 1/(2 \text{ ns} + 12 \text{ ns}) = 1/(14 \text{ ns}) \)

Latency = \( 3 \times (2 \text{ ns} + 12 \text{ ns}) = 42 \text{ ns} \)

Speedup = \( (30 \text{ ns})/(2 \text{ ns} + 12 \text{ ns}) = 2.14 < 3 \)
Practical Limit 3 - Hazards

\[
\text{Pipeline Speedup} = \frac{\text{Time}_{\text{sequential}}}{\text{Time}_{\text{pipeline}}} = \frac{\text{CPI}_{\text{sequential}}}{\text{CPI}_{\text{pipeline}}} \times \frac{\text{Cycle Time}_{\text{sequential}}}{\text{Cycle Time}_{\text{pipeline}}}
\]

If we ignore cycle time differences:

\[
\text{CPI}_{\text{ideal-pipeline}} = \frac{\text{CPI}_{\text{sequential}}}{\text{Pipeline Depth}}
\]

\[
\text{Pipeline Speedup} = \frac{\text{CPI}_{\text{ideal-pipeline}} \times \text{Pipeline Depth}}{\text{CPI}_{\text{ideal-pipeline}} + \text{Pipeline stall cycles}}
\]
Pipelining a Basic RISC ISA

Assumptions:

Only loads and stores affect memory

Base register + immediate offset = effective address

ALU operations

Only access registers

Two sources – two registers, or register and immediate

Branches and jumps

Address = PC + offset

Comparison between a register and zero

The last assumption is different from the 6th edition of the text and results in a slightly different pipeline. We will discuss reasons and implications in class.
A Simple Five Stage RISC Pipeline

Pipeline Stages

IF – Instruction Fetch
ID – Instruction decode, register read, branch computation
EX – Execution and Effective Address
MEM – Memory Access
WB – Writeback

1 2 3 4 5 6 7 8 9

i  IF  ID  EX  MEM  WB
i+1 IF  ID  EX  MEM  WB
i+2 IF  ID  EX  MEM  WB
i+3 IF  ID  EX  MEM  WB
i+4 IF  ID  EX  MEM  WB

Pipelining really isn't this simple
Figure C.28 of 5th edition

Pipelining really isn't this simple
A Naive Pipeline Implementation**

Figure C.28 The stall from branch hazards can be reduced by moving the zero test and branch-target calculation into the ID phase of the pipeline. Notice that we have made two important changes, each of which removes 1 cycle from the 3-cycle stall for branches. The first change is to move both the branch-target address calculation and the branch condition decision to the ID cycle. The second change is to write the PC of the instruction in the IF phase, using either the branch-target address computed during ID or the incremented PC computed during IF. In comparison, Figure C.22 obtained the branch-target address from the EX/MEM register and wrote the result during the MEM clock cycle. As mentioned in Figure C.22, the PC can be thought of as a pipeline register (e.g., as part of ID/IF), which is written with the address of the next instruction at the end of each IF cycle.

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Hazards

Structural Hazards

Data Hazards

Control Hazards
Hazards

Conditions that prevent the next instruction from executing

Structural Hazards

Data Hazards

Control Hazards
Hazards

Conditions that prevent the next instruction from executing

Structural Hazards

When two different instructions want to use the same hardware resource in the same cycle (resource conflict)

Data Hazards

Control Hazards
Hazards

Hazards

Conditions that prevent the next instruction from executing

Structural Hazards

When two different instructions want to use the same hardware resource in the same cycle (resource conflict)

Data Hazards

When two different instructions use the same location, it must appear as if instructions execute one at a time and in the specified order

Control Hazards
Hazards

Conditions that prevent the next instruction from executing

Structural Hazards

When two different instructions want to use the same hardware resource in the same cycle (resource conflict)

Data Hazards

When two different instructions use the same location, it must appear as if instructions execute one at a time and in the specified order

Control Hazards

When an instruction affects which instructions are executed next – branches, jumps, calls
Handling Hazards

Pipeline interlock logic
  Detects hazard and takes appropriate action
Simplest solution: stall
  Increases CPI
  Decreases performance
Other solutions are harder, but have better performance
Structural Hazards

When two *different* instructions want to use the *same* hardware resource in the *same* cycle

Stall (cause bubble)
- Low cost, simple
  - Increases CPI
  - Use for rare events
  - E.g., ??

Duplicate Resource
- Good performance
  - Increases cost (and maybe cycle time for interconnect)
  - Use for cheap resources
  - E.g., ALU and PC adder
Structural Hazards, cont.

Pipeline Resource
  - Good performance
    Often complex to do
    Use when simple to do
    E.g., write & read registers every cycle

Structural hazards are avoided if each instruction uses a resource
  At most once
  Always in the same pipeline stage
  For one cycle
  (⇒ no cycle where two instructions use the same resource)
**Structural Hazard Example**

Loads/stores (MEM) use same memory port as instrn fetches (IF)
30% of all instructions are loads and stores

Assume $CPI_{old}$ is 1.5

<table>
<thead>
<tr>
<th>i</th>
<th>IF</th>
<th>ID</th>
<th>EX</th>
<th>MEM</th>
<th>WB</th>
</tr>
</thead>
<tbody>
<tr>
<td>i+1</td>
<td>IF</td>
<td>ID</td>
<td>EX</td>
<td>MEM</td>
<td>WB</td>
</tr>
<tr>
<td>i+2</td>
<td>IF</td>
<td>ID</td>
<td>EX</td>
<td>MEM</td>
<td>WB</td>
</tr>
<tr>
<td>i+3</td>
<td>**</td>
<td>IF</td>
<td>ID</td>
<td>EX</td>
<td>MEM</td>
</tr>
<tr>
<td>i+4</td>
<td></td>
<td>IF</td>
<td>ID</td>
<td>EX</td>
<td>MEM</td>
</tr>
</tbody>
</table>

How much faster could a new machine with two memory ports be?
Structural Hazard Example

Loads/stores (MEM) use same memory port as instrn fetches (IF)
30% of all instructions are loads and stores

Assume $CPI_{old}$ is 1.5

1 2 3 4 5 6 7 8 9
i IF ID EX MEM WB ← a load
i+1 IF ID EX MEM WB
i+2 IF ID EX MEM WB
i+3 ** IF ID EX MEM WB
i+4 IF ID EX MEM WB

How much faster could a new machine with two memory ports be?

$$CPI_{new} = 1.5 - 1 \times 30\% = 1.2$$

$$Speedup = \frac{CPI_{old}}{CPI_{new}} = \left(\frac{1.5}{1.2}\right) = 1.25$$
Data Hazards

When two different instructions use the same location, it must appear as if instructions execute one at a time and in the specified order:

i    ADD r1,r2,
i+1  SUB r2,,r1
i+2  OR  r1,--,

Read-After-Write (RAW, data-dependence)
A true dependence

MOST IMPORTANT
Write-After-Read (WAR, anti-dependence)
Write-After-Write (WAW, output-dependence)
NOT: Read-After-Read (RAR)
Example Read-After-Write Hazards

ADD r1,_,_  IF  ID  EX  MEM  WB

SUB __, r1,___  IF  ID  EX  MEM  WB

LW r1,_,_  IF  ID  EX  MEM  WB

SW r1,100(r0)  IF  ID  EX  MEM  WB

LW r2,100(r0)  IF  ID  EX  MEM  WB

r1 written

r1 read

NOT OK!

r1 written

r1 read

NOT OK!

memory written

CORRECT!

memory read

(Unless LW instrn is at address 100(r0))
RAW Solutions

Solutions must first detect RAW, and then ...

Stall

ADD r1,_,_  IF  ID  EX  MEM  WB

SUB _, r1,_,  IF  ID  stall  stall  EX  MEM  WB

r1 written

r1 read

(Assumes registers written then read each cycle)

+ Low cost, simple

Increases CPI (plus 2 per stall in 5 stage pipeline)

Use for rare events
Bypass/Forward/ShortCircuit

Use data before it is in register

+ Reduces (avoids) stalls

More complex

Critical for common RAW hazards
Additional hardware

Muxes supply correct result to ALU

Additional control

Interlock logic must control muxes
Figure C.27 Forwarding of results to the ALU requires the addition of three extra inputs on each ALU multiplexer and the addition of three paths to the new inputs. The paths correspond to a bypass of: (1) the ALU output at the end of the EX, (2) the ALU output at the end of the MEM stage, and (3) the memory output at the end of the MEM stage.
Hybrid solution sometimes required:

One cycle bubble if result of load used by next instruction

Pipeline scheduling at compile time

Moves instructions to eliminate stalls
Pipeline Scheduling Example

Before:

\[
a = b + c;
\]

\[
LW \ Rb,b
\]

\[
LW \ Rc,c
\]

\[
\text{<- stall}
\]

\[
ADD \ Ra,Rb,Rc
\]

\[
SW \ a, \ Ra
\]

\[
d = e - f;
\]

\[
LW \ Re,e
\]

\[
LW \ Rf,f
\]

\[
\text{<- stall}
\]

\[
SUB \ Rd,Re,Rf
\]

\[
SW \ d, \ Rd
\]

After:

\[
a = b + c;
\]

\[
LW \ Rb,b
\]

\[
LW \ Rc,c
\]

\[
\text{<- stall}
\]

\[
ADD \ Ra,Rb,Rc
\]

\[
SW \ a, \ Ra
\]

\[
d = e - f;
\]

\[
LW \ Rf,f
\]

\[
\text{<- stall}
\]

\[
SUB \ Rd,Re,Rf
\]

\[
SW \ d, \ Rd
\]
Other Data Hazards

Write-After-Read (WAR, anti-dependence)

\[
\begin{align*}
i & \quad \text{ADD } r_1, r_2, \\
i + 1 & \quad \text{SUB } r_2, , r_1 \\
i + 2 & \quad \text{OR } r_1, , \\
\end{align*}
\]

Write-After-Write (WAW, output-dependence)

\[
\begin{align*}
i & \quad \text{MULT }, (r_2), r_1 /* RX mult */ \\
i + 1 & \quad \text{LW }, (r_1)+ /* autoincrement */ \\
i & \quad \text{DIVF fr}_1, , /* slow */ \\
i + 1 & \quad /* fast */ \\
i + 2 & \quad \text{ADDF fr}_1, , /* fast */
\end{align*}
\]
Other Data Hazards

i    ADD r1, r2,
i+1  SUB r2,, r1
i+2  OR  r1,,

Write-After-Read (WAR, anti-dependence)
Not in basic pipeline: read early / write late
Consider late read then early write:

i    MULT , (r2), r1    /* RX mult */
i+1  LW   , (r1)+      /* autoincrement */

Write-After-Write (WAW, output-dependence)

i    DIVF fr1, ,     /* slow */
i+1
i+2  ADDF fr1, ,     /* fast */
**Other Data Hazards**

```
i    ADD  r1, r2,
i+1   SUB  r2, , r1
i+2   OR   r1, ,
```

**Write-After-Read (WAR, anti-dependence)**

Not in basic pipeline: read early / write late

Consider late read then early write:

```
i    MULT  , (r2), r1  /* RX mult */
i+1   LW     , (r1)+   /* autoincrement */
```

**Write-After-Write (WAW, output-dependence)**

Not in basic pipeline: writes are in order

Consider: slow then fast operation

```
i    DIVF  fr1, ,     /* slow */
i+1
i+2   ADDF  fr1, ,     /* fast */
```

Occur easily with out-of-order execution
Control Hazards

When an instruction affects which instructions are executed next -- branches, jumps, calls

```
i  BEQZ r1,#8
i+1  SUB ,, 
     ... 
i+8  OR ,,  
i+9  ADD ,,  
```

```
1  2  3  4  5  6  7  8  9  
i  IF  ID  EX  MEM  WB  
i+1  IF (aborted)  
i+8  IF  ID  EX  MEM  WB  
i+9  IF  ID  EX  MEM  
```

Handling control hazards is very important
Handling Control Hazards

Branch Prediction
- Guess the direction of the branch
- Minimize penalty when right
- May increase penalty when wrong

Techniques
- Static – At compile time
- Dynamic – At run time

Static Techniques
- Predict Not Taken
- Predict Taken
- Delayed Branches

Dynamic techniques and more powerful static techniques later…
Handling Control Hazards, cont.

Predict NOT-TAKEN Always

NotTaken:

\[
\begin{array}{cccccccc}
1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\
i & \text{IF} & \text{ID} & \text{EX} & \text{MEM} & \text{WB} \\
i+1 & \text{IF} & \text{ID} & \text{EX} & \text{MEM} & \text{WB} \\
i+2 & \text{IF} & \text{ID} & \text{EX} & \text{MEM} & \text{WB} \\
i+3 & \text{IF} & \text{ID} & \text{EX} & \text{MEM} & \text{WB} \\
\end{array}
\]

Taken:

\[
\begin{array}{cccccccc}
1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\
i & \text{IF} & \text{ID} & \text{EX} & \text{MEM} & \text{WB} \\
i+1 & \text{IF} & \text{ID} & \text{EX} & \text{MEM} & \text{WB} \\
i+8 & \text{IF} & \text{ID} & \text{EX} & \text{MEM} & \text{WB} \\
i+9 & \text{IF} & \text{ID} & \text{EX} & \text{MEM} & \text{WB} \\
\end{array}
\]

Don't change machine state until branch outcome is known

Basic pipeline: State always changes late (WB)
Handling Control Hazards, cont.

Predict TAKEN Always

```
1  2  3  4  5  6  7  8  
 i  IF  ID  EX  MEM  WB

i+8  ‘IF’ ID  EX  MEM  WB

i+9  IF  ID  EX  MEM  WB

i+10  IF  ID  EX  MEM  WB
```

Must know what address to fetch at BEFORE branch is decoded

Not practical for our basic pipeline
Delayed branch

Execute next instruction regardless (of whether branch is taken)

What do we execute in the DELAY SLOT?
Delay Slots

Fill from before branch
  When:
  Helps:

Fill from target
  When:
  Helps:

Fill from fall through
  When:
  Helps:
Delay Slots**

Fill from before branch
  When: Branch independent of instruction
  Helps: Always

Fill from target
  When:

  Helps:

Fill from fall through
  When:
  Helps:
Delay Slots**

Fill from before branch
  When: Branch independent of instruction
  Helps: Always

Fill from target
  When: OK to execute target
    May have to duplicate code
  Helps: On taken branch
    May increase code size

Fill from fall through
  When:
  Helps:
**Delay Slots**

Fill from before branch
- When: Branch independent of instruction
- Helps: Always

Fill from target
- When: OK to execute target
  - May have to duplicate code
- Helps: On taken branch
  - May increase code size

Fill from fall through
- When: OK to execute instruction
- Helps: when not taken
Cancelling or nullifying branch

Instruction includes direction of prediction

Delay instruction squashed if wrong prediction

Allows second and third case of previous slide to be more aggressive
Comparison of Branch Schemes

Suppose 14% of all instructions are branches
Suppose 65% of all branches are taken
Suppose 50% of delay slots usefully filled

\[ \text{CPI penalty} = \% \text{ branches} \times \]
\[ (\% \text{ Taken} \times \text{Taken-Penalty} + \% \text{ Not-Taken} \times \text{Not-Taken penalty}) \]

<table>
<thead>
<tr>
<th>Branch Scheme</th>
<th>Taken Penalty</th>
<th>Not-Taken Penalty</th>
<th>CPI Penalty</th>
</tr>
</thead>
<tbody>
<tr>
<td>Basic Branch</td>
<td>1</td>
<td>1</td>
<td>.14</td>
</tr>
<tr>
<td>Not-Taken</td>
<td>1</td>
<td>0</td>
<td>.09</td>
</tr>
<tr>
<td>Taken0</td>
<td>0</td>
<td>1</td>
<td>.05</td>
</tr>
<tr>
<td>Taken1</td>
<td>1</td>
<td>1</td>
<td>.14</td>
</tr>
<tr>
<td>Delayed Branch</td>
<td>.5</td>
<td>.5</td>
<td>.07</td>
</tr>
</tbody>
</table>
Real Processors

MIPS R4000: 3 cycle branch penalty

First cycle: cancelling delayed branch (cancel if not taken)

Next two cycles: Predict not taken

Recent architectures:

Because of deeper pipelines, delayed branches not very useful

Processors rely more on hardware prediction (will see later) or may include both delayed and nondelayed branches
Branch Prediction Accuracy**

Figure 4. As processors use more complex algorithms, branch-prediction accuracy increases. (Number of history-table entries in parentheses.) *also uses return-address stack.
Interrupts

Interrupts (a.k.a. faults, exceptions, traps) often require

- Surprise jump
- Linking of return address
- Saving of PSW (including CCs)
- State change (e.g., to kernel mode)

Some examples

- Arithmetic overflow
- I/O device request
- O.S. call
- Page fault

Make pipelining hard
One Classification of Interrupts

1a. Synchronous
   function of program and memory state
   (e.g., arithmetic overflow, page fault)

1b. Asynchronous
   external device or hardware malfunction
   (printer ready, bus error)
Handling Interrupts

Precise Interrupts (Sequential Semantics)

- Complete instrns before offending one
- Squash (effects of) instrns after
- Save PC
- Force trap instrn into IF

Must handle simultaneous interrupts

- IF –
- ID –
- EX –
- MEM –
- WB –

Which interrupt should be handled first?
Handling Interrupts**

Precise Interrupts (Sequential Semantics)
- Complete instrns before offending one
- Squash (effects of) instrns after
- Save PC (& nextPC w/ delayed branches)
- Force trap instrn into IF

Must handle simultaneous interrupts
- IF – memory problems (pagefault, misaligned reference, protection violation)
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- ID – illegal or privileged instrn
- EX – arithmetic exception
- MEM –
- WB –

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- Save PC (& nextPC w/ delayed branches)
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- ID – illegal or privileged instrn
- EX – arithmetic exception
- MEM – memory problems
- WB –

Which interrupt should be handled first?
Handling Interrupts

Precise Interrupts (Sequential Semantics)
- Complete instrns before offending one
- Squash (effects of) instrns after
- Save PC (& nextPC w/ delayed branches)
- Force trap instrn into IF

Must handle simultaneous interrupts
- IF – memory problems (pagefault, misaligned reference, protection violation)
- ID – illegal or privileged instrn
- EX – arithmetic exception
- MEM – memory problems
- WB – none

Which interrupt should be handled first?
Example: Data Page Fault

1  2  3  4  5  6  7  8
i   IF  ID  EX  MEM  WB
i+1 IF  ID  EX  MEM  WB <- page fault (MEM)
i+2 IF  ID  EX  MEM  WB <- squash
i+3 IF  ID  EX  MEM  WB <- squash
i+4 IF  ID  EX  MEM  WB <- squash
i+5 trap -> IF  ID  EX  MEM  WB
i+6 trap handler -> IF  ID  EX  MEM  WB

Preceding instruction already complete
Squash succeeding instructions
    Prevent from modifying state
‘Trap’ instruction jumps to trap handler
Hardware saves PC in IAR
Trap handler must save IAR
Example: Arithmetic Exception

1  2  3  4  5  6  7  8
i    IF  ID  EX  MEM  WB
i+1     IF  ID  EX  MEM  WB
i+2          IF  ID  EX  MEM  WB  ← Exception (EX)
i+3              IF  ID  EX  MEM  WB  ← squash
i+4                  IF  ID  EX  MEM  WB  ← squash
i+5              trap  → IF  ID  EX  MEM  WB
i+6          trap handler  → IF  ID  EX  MEM  WB

Let preceding instructions complete
Squash succeeding instruction
Interrupts, cont.

Example: Illegal Opcode

1 2 3 4 5 6 7 8
i IF ID EX MEM WB
i+1 IF ID EX MEM WB
i+2 IF ID EX MEM WB
i+3 IF ID EX MEM WB ← ill. op (ID)
i+4 IF ID EX MEM WB ← squash
i+5 trap → IF ID EX MEM WB
i+6 trap handler → IF ID EX MEM WB

Let preceding instructions complete
Squash succeeding instruction
Example: Out-of-order Interrupts

<table>
<thead>
<tr>
<th>i</th>
<th>IF</th>
<th>ID</th>
<th>EX</th>
<th>MEM</th>
<th>WB</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>2</td>
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<tr>
<td>3</td>
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<tr>
<td>4</td>
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<tr>
<td>5</td>
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<tr>
<td>6</td>
<td></td>
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Which page fault should we take?

For precise interrupts – Post interrupts on a status vector associated with instruction, disable later writes in pipeline

- Check interrupt bit on entering WB
- Longer latency

For imprecise interrupts – Handle immediately

- Interrupts may occur in different order than on a sequential machine
- May cause implementation headaches
Interrupts, cont.

Other complications

- Odd bits of state (e.g., CCs)
- Early writes (e.g., autoincrement)
- Out of order execution

Interrupts come at random times

- The frequent case isn't everything
- The rare case MUST work correctly
Multicycle Operations

Not all operations complete in one cycle

Floating point arithmetic is inherently slower than integer arithmetic

2 to 4 cycles for multiply or add

20 to 50 cycles for divide

Extend basic 5-stage pipeline

EX stage may repeat multiple times

Multiple function units

Not pipelined for now
Handling Multicycle Operations

Four Functional Units
- EX: Integer unit
- $E^*$: FP/integer multiplier
- $E_+$: FP adder
- $E/_+$: FP/integer divider

Assume
- EX takes one cycle & all FP units take 4 cycles
- Separate integer and FP registers
- All FP arithmetic from FP registers

Worry about
- Structural hazards
- RAW hazards & forwarding
- WAR & WAW between integer & FP ops
**Simple Multicycle Example**

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**Notes**

(1) WAW possible only if?
(2) Stall forced by?
(3) Stall forced by?
(4) Stall forced by?
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**Notes**

1. WAW possible only if int is a load
2. Stall forced by
3. Stall forced by
4. Stall forced by
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**Notes**

1. WAW possible only if int is a load
2. Stall forced by MEM / WB conflict
3. Stall forced by
4. Stall forced by
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**Notes**

(1) WAW possible only if int is a load
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(3) Stall forced by structural conflict
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Notes

(1) WAW possible only if int is a load
(2) Stall forced by MEM / WB conflict
(3) Stall forced by structural conflict
(4) Stall forced by inorder issue
FP Instruction Issue

Check for RAW data hazard (in ID)

Wait until source registers are not used as destinations by instructions in EX that will not be available when needed

Check for forwarding

Bypass data from other stages, if necessary

Check for structural hazard in function unit

Wait until function unit is free (in ID)

Check for structural hazard in MEM / WB

Instructions stall in ID

Instructions stall before MEM

Static priority (e.g., FU with longest latency)
FP Instruction Issue (Cont.)

Check for WAW hazards

\[
\text{DIVF } F0, F2, F4 \\
\text{SUBF } F0, F8, F10
\]

SUBF completes first

1. Stall SUBF
2. Abort DIVF's WB

WAR hazards?
FP Instruction Issue (Cont.)

Check for WAW hazards

DIVF F0, F2, F4
SUBF F0, F8, F10

SUBF completes first
(1) Stall SUBF
(2) Abort DIVF's WB

WAR hazards
Read early, write late
More Multicycle Operations

Problems with Interrupts

DIVF F0, F2, F4
ADDF F2, F8, F10
SUBF F6, F4, F10

ADDF and SUBF complete before DIVF

Out-of-order completion

Possible imprecise interrupt

What happens if DIVF generates an exception after ADDF and SUBF complete??

We'll discuss solutions later