



# Well-formed Dependency and Open-loop Safety

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Based on Slides by Professor Lui  
Sha



# Reminders and Announcements

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- Announcements:
  - CS 424 is now on Piazza:  
[piazza.com/illinois/fall2017/cs424/home](https://piazza.com/illinois/fall2017/cs424/home)
  - We must form 4-person groups for robot-based MPs (each group gets one robot)
    - If you already formed a group, please send me and Yiran Zhao (the TA) the names of your group partners (email to: [zhao97@illinois.edu](mailto:zhao97@illinois.edu), with CC: [zaher@Illinois.edu](mailto:zaher@Illinois.edu)).
    - Please use the subject: "CS424 GROUP" (in upper case).
    - All people who do not have a group by the end of next week will be assigned a group by us.



## Recap

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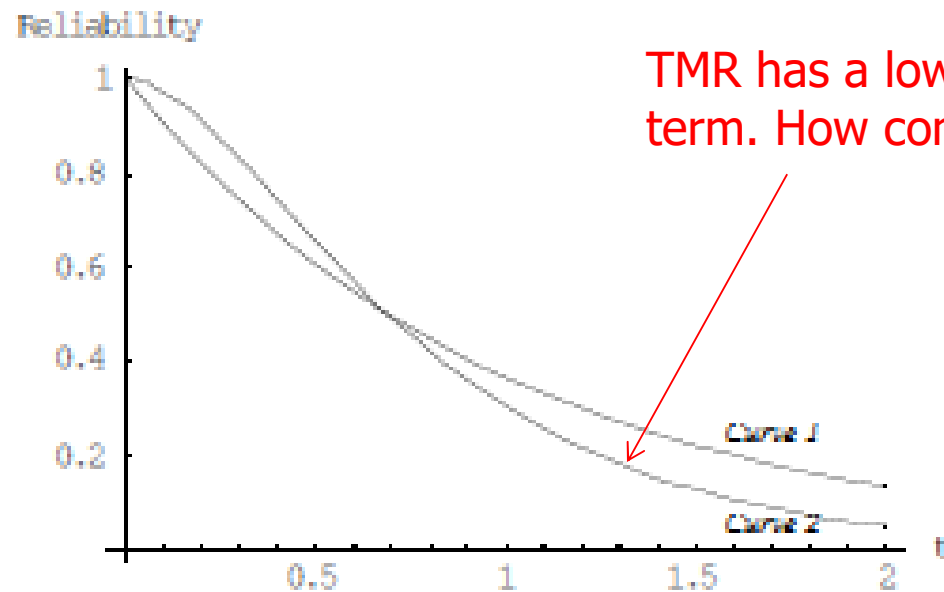
- Reliability for a given mission duration  $t$ ,  $R(t)$ , is the probability of the system working as specified (i.e., probability of no failures) for a duration that is at least as long as  $t$ .
- The most commonly used reliability function is the exponential reliability function:

$$R(t) = e^{-\lambda t}$$

where  $\lambda$  is the failure rate.

# Triple Modular Redundancy

- Which case is TMR?





# Implications of the Postulates

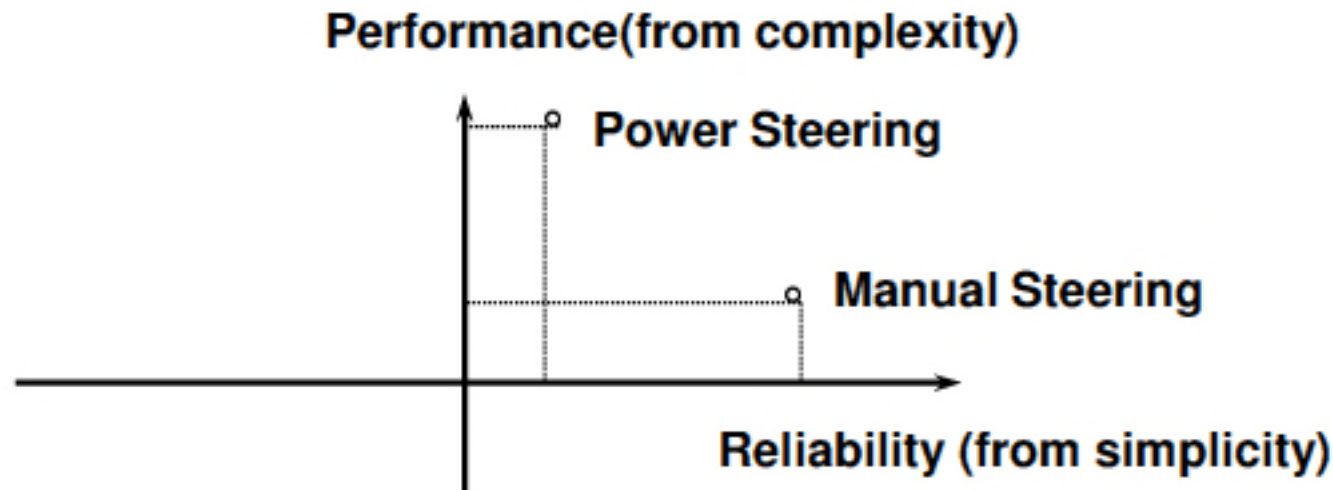
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$$R(\textit{Effort}, \textit{Complexity}, t) = e^{-kC t/E}$$

- Note: splitting the effort greatly reduces reliability.

# Analytic Redundancy and Complexity Reduction

- Partial redundancy via simple backup that meets only safety-critical requirements





# Example: A Sorting Exercise

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- Sorting:
  - Bubble sort: easy to write but slower,  $O(n^2)$
  - Quick sort: faster,  $O(n \log(n))$ , but more complicated to write
- Joe remembers how to do bubble sort, but is not perfectly sure of quick sort (has a 50% chance of getting it right).
- Joe is asked to write a sorting routine:
  - Correct and fast: A
  - Correct but slow: B
  - Incorrect: F

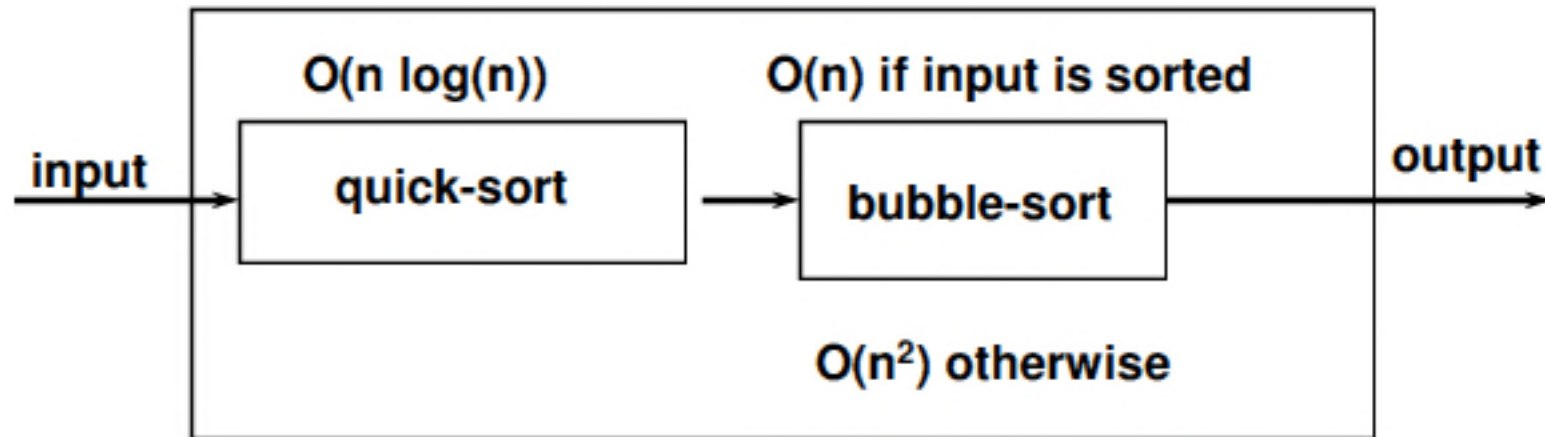
*What is Joe's optimal strategy?*

Critical requirement:  
Must pass!

# Solution

- Simplicity to “control” complexity

**Joe will get at least a “B”.**

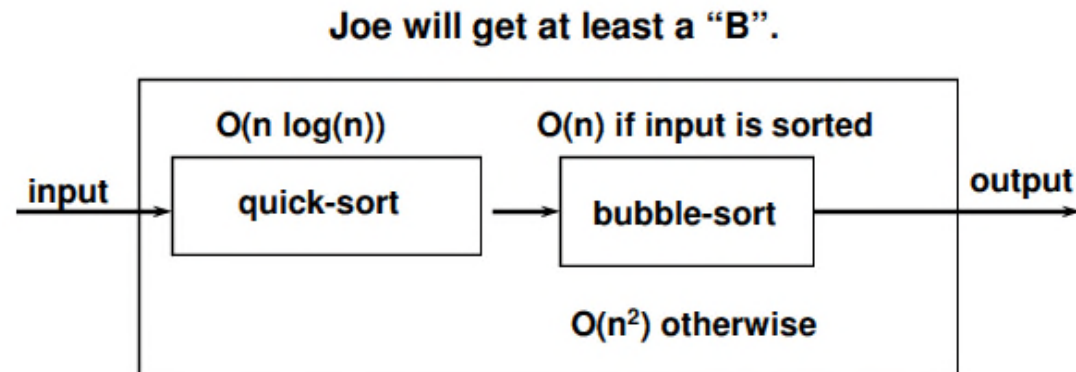




# Solution

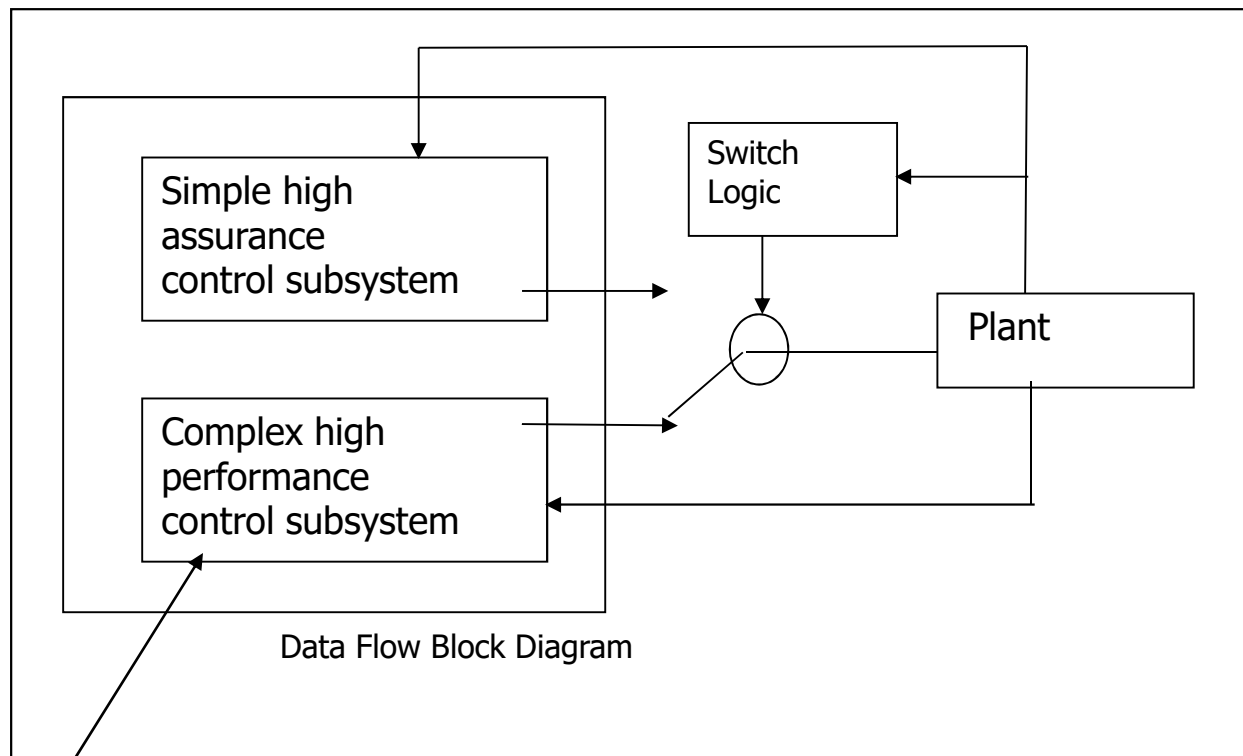
- Key property

- Use complex but efficient solution in the common case
- If the complex solution fails, catch the failure and switch to the simple (less efficient) but safe option



# Simplex Architectural Pattern

A simple verifiable core; diversity in the form of 2 alternatives; feedback control of the software execution.



Better performance, but less reliable



# Example

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- Component with mean time to failure = 10 years. Compare the reliability of:
  - a) Using this component alone
  - b) TMR using three versions of this component



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**Answer:**

$$\text{a) } r(t) = e^{-\lambda t} = e^{-(1/10) \cdot 1} = 0.9048$$



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After 1 year

**Answer:**

a)  $r(t) = e^{-\lambda t} = e^{-(1/10) \cdot 1} = 0.9048$

b)  $r(t)^3 + 3r(t)^2 (1 - r(t)) = 0.9745$



# Example

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- Component with mean time to failure = 10 years. Compare the reliability of:
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**After 15 years**



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$$\text{a) } r(t) = e^{-\lambda t} = e^{-(1/10) \cdot 15} = \mathbf{0.2231}$$





# Example

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**After 15 years**

**Answer:**

a)  $r(t) = e^{-\lambda t} = e^{-(1/10) \cdot 15} = 0.2231$

b)  $r(t)^3 + 3r(t)^2 (1 - r(t)) = 0.1271$



# Example

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- Component with mean time to failure = 10 years.  
Compare the reliability of:
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  - c) Using this component with a reduced complexity backup ( $C = 0.1$ )

After 15 years



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After 15 years

**Answer:**

$$c) r_1(t) = e^{-\lambda t} = 0.2231, r_b(t) = e^{-0.1\lambda t} = 0.8607$$



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Compare the reliability of:
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**Answer:**

$$c) r_1(t) = e^{-\lambda t} = 0.2231, r_b(t) = e^{-0.1\lambda t} = 0.8607$$

$$1 - (1 - r_1(t))(1 - r_b(t)) = 0.8918$$



# Example

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- Component with mean time to failure = 10 years (at unit complexity and unit budget). Compare the reliability of:
  - a) Using this component alone
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After 1 year



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- Component with mean time to failure = 10 years (at unit complexity and unit budget). Compare the reliability of:
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After 1 year

**Answer:**

a)  $r(t) = e^{-\lambda t} = e^{-(1/10) \cdot 1} = 0.9048$

b)  $r_2(t) = e^{-3 \lambda t} = 0.7408$

$$r_2(t)^3 + 3r_2(t)^2 (1 - r_2(t)) = 0.8333$$



# Lessons Learned?

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# Lessons Learned

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- More components/redundancy is not always better
- When budget is finite, more components means “spreading thinner” → lower reliability
- Having a simple (i.e., low complexity) back-up significantly improves reliability!



# Well Formed Dependencies

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- *Informal intuition:* A reliable component should not *depend* on a less reliable component (it defeats the purpose).



# Well Formed Dependencies

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- *Informal intuition:* A reliable component should not *depend* on a less reliable component (it defeats the purpose).
- Design guideline: **Use but do not depend** on less reliable components



# Well Formed Dependencies

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- Component A is said to depend on B, if the correctness of A's service depends on B's correctness.
- Component A is said to *use* the service of B, but not depend on it for its critical service S, if S can function correctly in spite of all B's faults.
- A system's dependency relations are said to be well-formed if and only if critical components may *use but do not depend* on the less critical components



# Design Philosophy

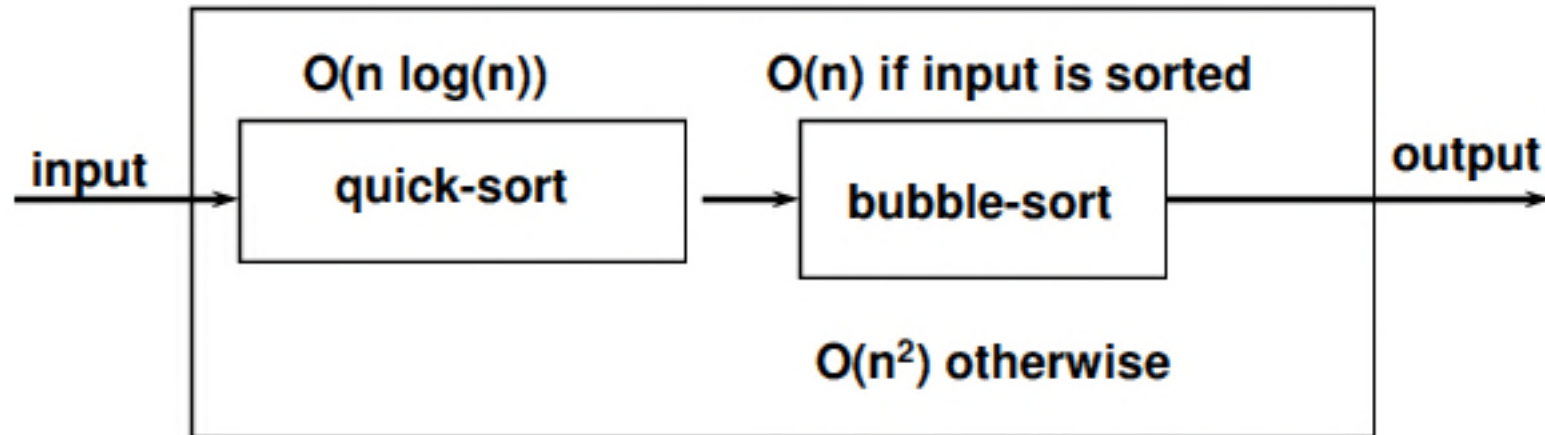
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- Build the system out of a reliable core and less reliable components
- Ensure that the reliable core is *minimal* (must be simple to reduce complexity – see lessons learned from reliability examples )
- The reliable core can use but do not depend on other components (i.e., failures elsewhere should not affect reliable core)
- The reliable core should ensure safety or recover from failures of other components

# Sorting Revisited

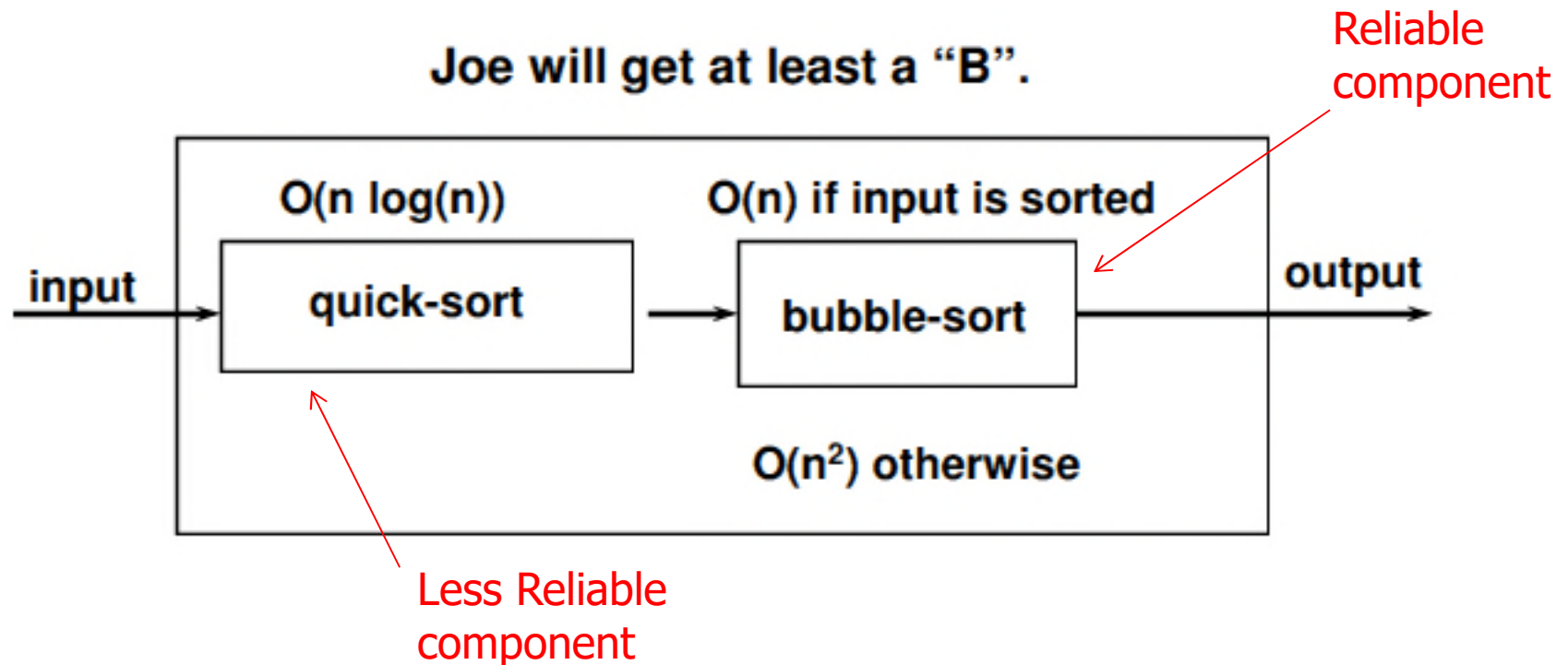
- How does the reliable component depend on the less reliable component? How to fix it?

**Joe will get at least a “B”.**



# Sorting Revisited

- How does the reliable component depend on the less reliable component? How to fix it?





# Sorting Revisited

## Ensuring Well-formed Dependencies

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- Resource sharing faults
  - Memory accessing fault: address space isolation
  - Hogging the CPU: CPU cycle limit
  - Timing fault: time out.
- Semantic fault
  - Wrong order: Bubble sort
  - Corrupt the input data item list: Export only a permutation function on a protected input list





# Safe State

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- In cyber-physical systems it is important to keep the system from harm. The reliable core must ensure that the system remains in a safe state (keep the kid away from the freeway!!) even when other components fail
- Example:
  - If your tire blows up, safely park the car on the shoulder of the road (safe state)



# Discussion: Patient Controlled Analgesia

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- When pain is severe in a post-surgery patient, the patient can push a button to get more pain medication (morphine: drug overdose will cause death). This is an example of a lethal device in the hands of an error-prone operator (the patient). How can we ensure safety of software controlled PCA?