

# CS 421 Lecture 9: Bottom-up Parsing

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- Announcements
- OCaml self-help hints
- Lecture outline
  - Bottom-up parsing
  - ocaml yacc

# Announcements

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- MP4 has been posted
  - MiniJava lexer
- Reminder: midterm exam date – Thursday, July 2

# OCaml self-help hints

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- Consult the CS 421 resource guide:
  - <http://www.cs.uiuc.edu/class/su09/cs421/>
  - Use “Tips for using OCaml top level” to speed up working with the interactive environment
  - Consult the OCaml manual when you want a definitive answer about something
    - May be technical, not “user-friendly”
- Ask on the newsgroup
  - If you are having a problem, it’s likely somebody has run into it already, or they will in the future.
- Ask Google
  - It probably knows...

# OCaml self-help hints

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- Be careful about
  - Data types, and type inference
  - Operator precedence
- Common OCaml error messages:
  - syntax error (underlined)
  - unbound value use (underlined)
  - Pattern matching is not exhaustive. Here is a counterexample:  
...
  - This expression has type *<type1>* but is here used with *<type2>*
    - Watch out especially for "unit"
  - *<whatever error>* in *<file>.ml* at line *<line>* characters *<chars>*

# Top-down vs. bottom-up parsing

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- Why is top-down called “top-down?”
  - As we consume tokens, we build a parse tree.
  - At any one time, we are filling in the children of a particular non-terminal.
  - *As soon as we decide which production to use*, we can fill in the tree.
  - In this sense, we are building the tree from the top (root) down (to the leaves).
    - Nature and Computer Science disagree on this point

# Top-down parsing

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- Example:

- $E \rightarrow id \ T$

- $T \rightarrow \varepsilon \mid + E \mid * E$

Input:  $x + y * z$

# Bottom-up parsing

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- Works by creating small parse trees and joining them together into larger ones.
- Example: Input:  $x + y * z$ 
  - $E \rightarrow id \ T$
  - $T \rightarrow \varepsilon \mid + E \mid * E$
- Start constructing trees, put them on stack:
  - Construct tree  $x$ :  $\{x\}$
  - Add tree  $+$ :  $\{x, +\}$
  - Add tree  $y$ :  $\{x, +, y\}$
  - Add tree  $*$ :  $\{x, +, y, *\}$
  - Add tree  $z$ :  $\{x, +, y, *, z\}$

# Bottom-up parsing (cont)

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- Construct parse tree by merging:
  - $\{x, +, y, *, z\}$
  - Apply  $T \rightarrow \varepsilon$ 
    - $\{x, +, y, *, z, T \rightarrow \varepsilon\}$
  - ...



# How bottom-up parsing works

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- Keep a stack of small parse trees. Based on what's in this stack, and the next input token, take one of these actions:
  - Shift: move lookahead token to stack
  - Reduce  $A \rightarrow \alpha$ : if roots of trees on stack match  $\alpha$ , replace those trees on stack by single tree with root  $A$
  - Accept: reduce when non-terminal is the start symbol, lookahead is EOF
  - Reject
- Bottom-up parsing is also called *shift-reduce parsing*

# Shift-reduce example 1

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- Example:

- $L \rightarrow L ; E \mid E$

- $E \rightarrow id$

Input:  $x ; y ; z$

<u>Action</u>	<u>Stack</u>	<u>Input</u>
S		$x ; y ; z$
R $E \rightarrow id$	$x$	$; y ; z$
...		

# Shift-reduce example 1

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- Example:
  - $L \rightarrow L ; E \mid E$
  - $E \rightarrow id$

Action

Stack

Input

# Shift-reduce example 2

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- Example:

- $E \rightarrow E + T \mid T$

- $T \rightarrow T * P \mid P$

- $P \rightarrow id \mid int$

Input:  $x + 10 * y$

Action

Stack

Input

S

$x + 10 * y$

R  $P \rightarrow id$

x

$+ 10 * y$

...

# Shift-reduce example 2

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- Example:
  - $E \rightarrow E + T \mid T$
  - $T \rightarrow T * P \mid P$
  - $P \rightarrow id \mid int$

Action

Stack

Input

# Bottom-up parsing

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- This is hard!
  - How can we build a parser that works like this?
- Shift-reduce parsing is not usually done “by hand”
  - Automated parser generator tools
  - Generate parser code based on grammar specification
    - Similar to ocamllex and regular expressions for lexing
- Ocaml’s parser generator is called ocaml yacc
  - “yet another compiler-compiler”

# Using ocaml yacc

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- Create grammar specification in a text file
  - `<grammar>.mly`
- Execute
  - `ocaml yacc <grammar>.mly`
- Produces
  - code for parser in `<grammar>.ml`
  - interface (including type declaration for tokens) in `<grammar.mli>`

# Parser code

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- `<grammar>.ml` defines one parsing function per entry point
- Parsing function takes a lexing function (lexbuf -> token) and a lexbuf as arguments
  - Aside: we'll see more functions being passed around as arguments soon...
- Returns *semantic attribute* of corresponding entry point



# Example – expression grammar

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- We will take a simple expression grammar and create a parser to parse inputs and produce abstract syntax
- Grammar:
  - $M \rightarrow Exp\ eof$
  - $Exp \rightarrow Term \mid Term + Exp \mid Term - Exp$
  - $Term \rightarrow Factor \mid Factor * Term \mid Factor / Term$
  - $Factor \rightarrow id \mid ( Exp )$

- **Abstract syntax**

```
(* file: expr.ml *)
type expr =
  Plus of expr * expr
| Minus of expr * expr
| Mult of expr * expr
| Div of expr * expr
| Id of string
```

# Example – lexer

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```
(* file: exprlex.mll *)
let numeric = ['0' - '9']
let letter = ['a' - 'z' 'A' - 'Z']
rule tokenize = parse
  | "+" {Plus_token}
  | "-" {Minus_token}
  | "*" {Times_token}
  | "/" {Divide_token}
  | "(" {Left_parenthesis}
  | ")" {Right_parenthesis}
  | letter (letter | numeric | "_")* as id {Id_token id}
  | [' ' '\t' '\n'] {tokenize lexbuf}
  | eof {EOL}
```

# Example – parser

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```
(* file: exprparse.mly *)
%{ open Expr
%}
%token <string> Id_token
%token Left_parenthesis Right_parenthesis
%token Times_token Divide_token
%token Plus_token Minus_token
%token EOL
%start main
%type <expr> main
%%

...
```

# Example – parser (exprparse.mly)

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```
expr:
    term                                {$1}
  | term Plus_token expr                {Plus($1,$3)}
  | term Minus_token expr               {Minus($1,$3)}

term:
    factor                               {$1}
  | factor Times_token term             {Mult($1,$3)}
  | factor Divide_token term           {Div($1,$3)}

factor:
    Id_token {Id $1}
  | Left_parenthesis expr Right_parenthesis {$2}

main:
  | expr EOL                             {$1}
```

# Example – using parser

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```
# #use "expr.ml";;
...
# #use "expparse.ml";;
...
# #use "exprlex.ml";;
...
# let test s =
    let lexbuf = Lexing.from_string(s^"\n") in
      main tokenize lexbuf;;
...
# test "a + b";;
- : expr = Plus(Id "a", Id "b")
```

# ocamlyacc input

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- File format:

```
%{  
  <header>  
%}  
  <declarations>  
%%  
  <rules>  
%%  
  <trailer>
```

# ocamlyacc <*header*>

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- Contains arbitrary OCaml code
- Typically used to give types and functions needed for the semantic actions of rules and to give specialized error recovery
- May be omitted
- <*footer*> is similar. Possibly used to call parser.

# ocamlyacc <declarations>

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- `%token symbol ... symbol`
  - Declare given symbols as tokens
- `%token <type> symbol ... symbol`
  - Declare given symbols as token constructors, taking an argument of type *type*
- `%start symbol ... symbol`
  - Declare given symbols as entry points; functions of same names in <*grammar*>.ml



# ocamlyacc <declarations>

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- `%type <type> symbol ... symbol`
  - Specify type of attributes for given symbols. Mandatory for start symbol.
- `%left symbol ... symbol`
- `%right symbol ... symbol`
- `%nonassoc symbol ... symbol`
  - Associate precedences and associativities to given symbols.
  - Same line, same precedence; earlier line, lower precedence (broadest scope)

# ocamlyacc <rules>

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- *nonterminal*:

*symbol ... symbol { semantic\_action }*

| ...

| *symbol ... symbol { semantic\_action }*

;

- Semantic actions are arbitrary OCaml expressions

- Must be of the same type as declared (or inferred) for *nonterminal*

- Access values semantic attributes of symbols by position: \$1 for first symbol, \$2 for second, *etc.*

# Next class

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- Finish up parsing (yay!)
- Big question: how to choose whether to shift or reduce?
  - ocaml yacc uses a method – called *LALR(1)* – to construct tables that say which action to take.
- There are times when there is no good way to make this decision.
  - ocaml yacc will reject grammar and give an error message
  - In bottom-up parsing, these are called *conflicts*. There are two types: shift/reduce and reduce/reduce.
    - As with top-down parsing, these problems can sometimes be resolved by modifying the grammar.
    - We will discuss these conflicts and give some advice on how to resolve them.