

# Programming Languages and Compilers (CS 421)

Elsa L Gunter  
2112 SC, UIUC



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Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

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## Example: If Then Else Rule

$$\frac{}{(if\ x > 5\ then\ y := 2 + 3\ else\ y := 3 + 4\ fi,\ \{x \rightarrow 7\}) \Downarrow ?}$$

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## Example: If Then Else Rule

$$\frac{(x > 5, \{x \rightarrow 7\}) \Downarrow ?}{(if\ x > 5\ then\ y := 2 + 3\ else\ y := 3 + 4\ fi,\ \{x \rightarrow 7\}) \Downarrow ?}$$

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## Example: Arith Relation

$$\frac{? > ? = ? \quad (x, \{x \rightarrow 7\}) \Downarrow ? \quad (5, \{x \rightarrow 7\}) \Downarrow ?}{(x > 5, \{x \rightarrow 7\}) \Downarrow ?}$$

$$\frac{}{(if\ x > 5\ then\ y := 2 + 3\ else\ y := 3 + 4\ fi,\ \{x \rightarrow 7\}) \Downarrow ?}$$

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## Example: Identifier(s)

$$\frac{7 > 5 = true \quad (x, \{x \rightarrow 7\}) \Downarrow 7 \quad (5, \{x \rightarrow 7\}) \Downarrow 5}{(x > 5, \{x \rightarrow 7\}) \Downarrow ?}$$

$$\frac{}{(if\ x > 5\ then\ y := 2 + 3\ else\ y := 3 + 4\ fi,\ \{x \rightarrow 7\}) \Downarrow ?}$$

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## Example: Arith Relation

$$\frac{7 > 5 = true \quad (x, \{x \rightarrow 7\}) \Downarrow 7 \quad (5, \{x \rightarrow 7\}) \Downarrow 5}{(x > 5, \{x \rightarrow 7\}) \Downarrow true}$$

$$\frac{}{(if\ x > 5\ then\ y := 2 + 3\ else\ y := 3 + 4\ fi,\ \{x \rightarrow 7\}) \Downarrow ?}$$

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### Example: If Then Else Rule

$$\frac{\frac{7 > 5 = \text{true}}{(x, \{x \rightarrow 7\}) \Downarrow 7 \quad (5, \{x \rightarrow 7\}) \Downarrow 5} \quad \frac{(y := 2 + 3, \{x \rightarrow 7\})}{\Downarrow ?}}{(x > 5, \{x \rightarrow 7\}) \Downarrow \text{true} \quad \Downarrow ?} \quad .$$

$$\frac{}{(if \ x > 5 \ \text{then} \ y := 2 + 3 \ \text{else} \ y := 3 + 4 \ \text{fi}, \{x \rightarrow 7\}) \Downarrow ?}$$

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### Example: Assignment

$$\frac{\frac{7 > 5 = \text{true}}{(x, \{x \rightarrow 7\}) \Downarrow 7 \quad (5, \{x \rightarrow 7\}) \Downarrow 5} \quad \frac{(2 + 3, \{x \rightarrow 7\}) \Downarrow ?}{(y := 2 + 3, \{x \rightarrow 7\}) \Downarrow ?}}{(x > 5, \{x \rightarrow 7\}) \Downarrow \text{true} \quad \Downarrow ?} \quad .$$

$$\frac{}{(if \ x > 5 \ \text{then} \ y := 2 + 3 \ \text{else} \ y := 3 + 4 \ \text{fi}, \{x \rightarrow 7\}) \Downarrow ?}$$

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### Example: Arith Op

$$\frac{\frac{7 > 5 = \text{true}}{(x, \{x \rightarrow 7\}) \Downarrow 7 \quad (5, \{x \rightarrow 7\}) \Downarrow 5} \quad \frac{\frac{? + ? = ?}{(2, \{x \rightarrow 7\}) \Downarrow ? \quad (3, \{x \rightarrow 7\}) \Downarrow ?} \quad \frac{(2 + 3, \{x \rightarrow 7\}) \Downarrow ?}{(y := 2 + 3, \{x \rightarrow 7\}) \Downarrow ?}}{(x > 5, \{x \rightarrow 7\}) \Downarrow \text{true} \quad \Downarrow ?} \quad .$$

$$\frac{}{(if \ x > 5 \ \text{then} \ y := 2 + 3 \ \text{else} \ y := 3 + 4 \ \text{fi}, \{x \rightarrow 7\}) \Downarrow ?}$$

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### Example: Numerals

$$\frac{\frac{7 > 5 = \text{true}}{(x, \{x \rightarrow 7\}) \Downarrow 7 \quad (5, \{x \rightarrow 7\}) \Downarrow 5} \quad \frac{\frac{2 + 3 = 5}{(2, \{x \rightarrow 7\}) \Downarrow 2 \quad (3, \{x \rightarrow 7\}) \Downarrow 3} \quad \frac{(2 + 3, \{x \rightarrow 7\}) \Downarrow ?}{(y := 2 + 3, \{x \rightarrow 7\}) \Downarrow ?}}{(x > 5, \{x \rightarrow 7\}) \Downarrow \text{true} \quad \Downarrow ?} \quad .$$

$$\frac{}{(if \ x > 5 \ \text{then} \ y := 2 + 3 \ \text{else} \ y := 3 + 4 \ \text{fi}, \{x \rightarrow 7\}) \Downarrow ?}$$

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### Example: Arith Op

$$\frac{\frac{7 > 5 = \text{true}}{(x, \{x \rightarrow 7\}) \Downarrow 7 \quad (5, \{x \rightarrow 7\}) \Downarrow 5} \quad \frac{\frac{2 + 3 = 5}{(2, \{x \rightarrow 7\}) \Downarrow 2 \quad (3, \{x \rightarrow 7\}) \Downarrow 3} \quad \frac{(2 + 3, \{x \rightarrow 7\}) \Downarrow 5}{(y := 2 + 3, \{x \rightarrow 7\}) \Downarrow ?}}{(x > 5, \{x \rightarrow 7\}) \Downarrow \text{true} \quad \Downarrow ?} \quad .$$

$$\frac{}{(if \ x > 5 \ \text{then} \ y := 2 + 3 \ \text{else} \ y := 3 + 4 \ \text{fi}, \{x \rightarrow 7\}) \Downarrow ?}$$

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### Example: Assignment

$$\frac{\frac{7 > 5 = \text{true}}{(x, \{x \rightarrow 7\}) \Downarrow 7 \quad (5, \{x \rightarrow 7\}) \Downarrow 5} \quad \frac{\frac{2 + 3 = 5}{(2, \{x \rightarrow 7\}) \Downarrow 2 \quad (3, \{x \rightarrow 7\}) \Downarrow 3} \quad \frac{(2 + 3, \{x \rightarrow 7\}) \Downarrow 5}{(y := 2 + 3, \{x \rightarrow 7\}) \Downarrow \{x \rightarrow 7, y \rightarrow 5\}}}{(x > 5, \{x \rightarrow 7\}) \Downarrow \text{true} \quad \Downarrow \{x \rightarrow 7, y \rightarrow 5\}} \quad .$$

$$\frac{}{(if \ x > 5 \ \text{then} \ y := 2 + 3 \ \text{else} \ y := 3 + 4 \ \text{fi}, \{x \rightarrow 7\}) \Downarrow ?}$$

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## Example: If Then Else Rule

$$\begin{array}{c}
 2 + 3 = 5 \\
 \frac{(2, \{x \rightarrow 7\}) \Downarrow 2 \quad (3, \{x \rightarrow 7\}) \Downarrow 3}{(2+3, \{x \rightarrow 7\}) \Downarrow 5} \\
 \frac{7 > 5 = \text{true} \quad (y := 2 + 3, \{x \rightarrow 7\}) \Downarrow 5}{(x > 5, \{x \rightarrow 7\}) \Downarrow \text{true} \quad \Downarrow \{x \rightarrow 7, y \rightarrow 5\}} \\
 \frac{}{(if\ x > 5\ then\ y := 2 + 3\ else\ y := 3 + 4\ fi, \\ \{x \rightarrow 7\}) \Downarrow \{x \rightarrow 7, y \rightarrow 5\}}
 \end{array}$$

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## Let in Command

$$\frac{(E, m) \Downarrow v \quad (C, m[I \leftarrow v]) \Downarrow m'}{(let\ I = E\ in\ C, m) \Downarrow m''}$$

Where  $m''(y) = m'(y)$  for  $y \neq I$  and  $m''(I) = m(I)$  if  $m(I)$  is defined, and  $m''(I)$  is undefined otherwise

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## Example

$$\frac{(x, \{x \rightarrow 5\}) \Downarrow 5 \quad (3, \{x \rightarrow 5\}) \Downarrow 3}{(x+3, \{x \rightarrow 5\}) \Downarrow 8} \\
 \frac{(5, \{x \rightarrow 17\}) \Downarrow 5 \quad (x := x+3, \{x \rightarrow 5\}) \Downarrow \{x \rightarrow 8\}}{(let\ x = 5\ in\ (x := x+3), \{x \rightarrow 17\}) \Downarrow ?}$$

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## Example

$$\frac{(x, \{x \rightarrow 5\}) \Downarrow 5 \quad (3, \{x \rightarrow 5\}) \Downarrow 3}{(x+3, \{x \rightarrow 5\}) \Downarrow 8} \\
 \frac{(5, \{x \rightarrow 17\}) \Downarrow 5 \quad (x := x+3, \{x \rightarrow 5\}) \Downarrow \{x \rightarrow 8\}}{(let\ x = 5\ in\ (x := x+3), \{x \rightarrow 17\}) \Downarrow \{x \rightarrow 17\}}$$

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## Comment

- Simple Imperative Programming Language introduces variables *implicitly* through assignment
- The let-in command introduces scoped variables *explicitly*
- Clash of constructs apparent in awkward semantics

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## Interpretation Versus Compilation

- A **compiler** from language L1 to language L2 is a program that takes an L1 program and for each piece of code in L1 generates a piece of code in L2 of same meaning
- An **interpreter** of L1 in L2 is an L2 program that executes the meaning of a given L1 program
- Compiler would examine the body of a loop once; an interpreter would examine it every time the loop was executed

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## Interpreter

- An *Interpreter* represents the operational semantics of a language L1 (source language) in the language of implementation L2 (target language)
- Built incrementally
  - Start with literals
  - Variables
  - Primitive operations
  - Evaluation of expressions
  - Evaluation of commands/declarations

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## Interpreter

- Takes abstract syntax trees as input
  - In simple cases could be just strings
- One procedure for each syntactic category (nonterminal)
  - eg one for expressions, another for commands
- If Natural semantics used, tells how to compute final value from code
- If Transition semantics used, tells how to compute next "state"
  - To get final value, put in a loop

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## Natural Semantics Example

- $\text{compute\_exp}(\text{Var}(v), m) = \text{look\_up } v \text{ } m$
- $\text{compute\_exp}(\text{Int}(n), \_) = \text{Num}(n)$
- ...
- $\text{compute\_com}(\text{IfExp}(b, c1, c2), m) =$   
if  $\text{compute\_exp}(b, m) = \text{Bool}(\text{true})$   
then  $\text{compute\_com}(c1, m)$   
else  $\text{compute\_com}(c2, m)$

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## Natural Semantics Example

- $\text{compute\_com}(\text{While}(b, c), m) =$   
if  $\text{compute\_exp}(b, m) = \text{Bool}(\text{false})$   
then  $m$   
else  $\text{compute\_com}(\text{While}(b, c), \text{compute\_com}(c, m))$
- May fail to terminate - exceed stack limits
- Returns no useful information then

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## Transition Semantics

- Form of operational semantics
- Describes how each program construct transforms machine state by *transitions*
- Rules look like  
 $(C, m) \rightarrow (C', m')$  or  $(C, m) \rightarrow m'$
- $C, C'$  is code remaining to be executed
- $m, m'$  represent the state/store/memory/environment
  - Partial mapping from identifiers to values
  - Sometimes  $m$  (or  $C$ ) not needed
- Indicates exactly one step of computation

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## Expressions and Values

- $C, C'$  used for commands;  $E, E'$  for expressions;  $U, V$  for values
- Special class of expressions designated as *values*
  - Eg 2, 3 are values, but 2+3 is only an expression
- Memory only holds values
  - Other possibilities exist

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## Evaluation Semantics

- Transitions successfully stops when  $E/C$  is a value/memory
- Evaluation fails if no transition possible, but not at value/memory
- Value/memory is the final *meaning* of original expression/command (in the given state)
- Coarse semantics: final value / memory
- More fine grained: whole transition sequence

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1525 minutes

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## Simple Imperative Programming Language

- $I \in \text{Identifiers}$
- $N \in \text{Numerals}$
- $B ::= \text{true} \mid \text{false} \mid B \& B \mid B \text{ or } B \mid \text{not } B \mid E < E \mid E = E$
- $E ::= N \mid I \mid E + E \mid E * E \mid E - E \mid - E$
- $C ::= \text{skip} \mid C; C \mid I ::= E \mid \text{if } B \text{ then } C \text{ else } C \text{ fi} \mid \text{while } B \text{ do } C \text{ od}$

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## Transitions for Expressions

- Numerals are values
- Boolean values = {true, false}
- Identifiers:  $(I, m) \dashrightarrow (m(I), m)$

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## Boolean Operations:

- Operators: (short-circuit)
- $$\frac{(\text{false} \& B, m) \dashrightarrow (\text{false}, m) \quad (B, m) \dashrightarrow (B'', m)}{(\text{true} \& B, m) \dashrightarrow (B, m) \quad (B \& B', m) \dashrightarrow (B'' \& B', m)}$$
- $$\frac{(\text{true} \text{ or } B, m) \dashrightarrow (\text{true}, m) \quad (B, m) \dashrightarrow (B'', m)}{(\text{false} \text{ or } B, m) \dashrightarrow (B, m) \quad (B \text{ or } B', m) \dashrightarrow (B'' \text{ or } B', m)}$$
- $$\frac{(\text{not true}, m) \dashrightarrow (\text{false}, m) \quad (B, m) \dashrightarrow (B', m)}{(\text{not false}, m) \dashrightarrow (\text{true}, m) \quad (\text{not } B, m) \dashrightarrow (\text{not } B', m)}$$

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## Relations

$$\frac{(E, m) \dashrightarrow (E', m)}{(E \sim E', m) \dashrightarrow (E' \sim E', m)}$$

$$\frac{(E, m) \dashrightarrow (E', m)}{(V \sim E, m) \dashrightarrow (V \sim E', m)}$$

$(U \sim V, m) \dashrightarrow (\text{true}, m) \text{ or } (\text{false}, m)$   
depending on whether  $U \sim V$  holds or not

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## Arithmetic Expressions

$$\frac{(E, m) \rightarrow (E', m)}{(E \text{ op } E', m) \rightarrow (E' \text{ op } E', m)}$$

$$\frac{(E, m) \rightarrow (E', m)}{(V \text{ op } E, m) \rightarrow (V \text{ op } E', m)}$$

$(U \text{ op } V, m) \rightarrow (N, m)$  where  $N$  is the specified value for  $U \text{ op } V$

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## Commands - in English

- skip means done evaluating
- When evaluating an assignment, evaluate the expression first
- If the expression being assigned is already a value, update the memory with the new value for the identifier
- When evaluating a sequence, work on the first command in the sequence first
- If the first command evaluates to a new memory (ie completes), evaluate remainder with new memory

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## Commands

$$(\text{skip}, m) \rightarrow m$$

$$\frac{(E, m) \rightarrow (E', m)}{(I ::= E, m) \rightarrow (I ::= E', m)}$$

$$(I ::= V, m) \rightarrow m[I \leftarrow V]$$

$$\frac{(C, m) \rightarrow (C', m')}{(C; C', m) \rightarrow (C'; C', m')} \quad \frac{(C, m) \rightarrow m'}{(C; C', m) \rightarrow (C', m')}$$

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