

## Programming Languages and Compilers (CS 421)

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Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

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## EOH!

- Engineering Open House is Friday and Saturday
- They are taking this room
  
- On Friday only, we will meet in Zoom only:
- **Zoom Info:** Meeting Id: 838 6324 1301  
**Passcode:** cs421  
**URL:** <https://illinois.zoom.us/j/83863241301?pwd=U2dtRm9RUmhVQUw4d3dFOVJxNHY4UT09>

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## Example : test.ml

```
{ type result = Int of int | Float of float |
  String of string }
let digit = ['0'-'9']
let digits = digit +
let lower_case = ['a'-'z']
let upper_case = ['A'-'Z']
let letter = upper_case | lower_case
let letters = letter +
```

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## Example : test.ml

```
rule main = parse
  (digits)'.'digits as f { Float (float_of_string f) }
  | digits as n          { Int (int_of_string n) }
  | letters as s         { String s}
  | _ { main lexbuf }
{ let newlexbuf = (Lexing.from_channel stdin) in
  print_newline ();
  main newlexbuf }
```

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## Example

```
# #use "test.ml";;
...
val main : Lexing.lexbuf -> result = <fun>
val _ocaml_lex_main_rec : Lexing.lexbuf -> int ->
  result = <fun>
hi there 234 5.2
- : result = String "hi"
```

What happened to the rest?!?

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## Example

```
# let b = Lexing.from_channel stdin;;
# main b;;
hi 673 there
- : result = String "hi"
# main b;;
- : result = Int 673
# main b;;
- : result = String "there"
```

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## Problem

- How to get lexer to look at more than the first token at one time?
- Answer: *action* has to tell it to -- recursive calls
  - Not what you want to sew this together with `ocaml yacc`
- Side Benefit: can add “state” into lexing
- Note: already used this with the `_` case

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## Example

```
rule main = parse
  (digits) '.' digits as f { Float
    (float_of_string f) :: main lexbuf }
  | digits as n      { Int (int_of_string n) ::
    main lexbuf }
  | letters as s     { String s :: main
    lexbuf }
  | eof              { [] }
  | _                { main lexbuf }
```

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## Example Results

```
hi there 234 5.2
- : result list = [String "hi"; String "there"; Int
  234; Float 5.2]
#
```

Used Ctrl-d to send the end-of-file signal

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## Dealing with comments

### First Attempt

```
let open_comment = "("
let close_comment = ")"
rule main = parse
  (digits) '.' digits as f { Float (float_of_string
    f) :: main lexbuf }
  | digits as n      { Int (int_of_string n) ::
    main lexbuf }
  | letters as s     { String s :: main lexbuf }
```

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## Dealing with comments

```
| open_comment      { comment lexbuf }
| eof                { [] }
| _ { main lexbuf }
and comment = parse
  close_comment     { main lexbuf }
  | _               { comment lexbuf }
```

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## Dealing with nested comments

```
rule main = parse ...
  | open_comment     { comment 1 lexbuf }
  | eof              { [] }
  | _ { main lexbuf }
and comment depth = parse
  open_comment       { comment (depth+1) lexbuf }
  | close_comment    { if depth = 1
    then main lexbuf
    else comment (depth - 1) lexbuf }
  | _                { comment depth lexbuf }
```

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## Dealing with nested comments

```
rule main = parse
  (digits) '!' digits as f { Float (float_of_string f) ::
  main lexbuf }
| digits as n      { Int (int_of_string n) :: main
  lexbuf }
| letters as s     { String s :: main lexbuf }
| open_comment    { (comment 1 lexbuf)
| eof             { [] }
| _ { main lexbuf }
```

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## Dealing with nested comments

```
and comment depth = parse
  open_comment    { comment (depth+1) lexbuf
  }
| close_comment   { if depth = 1
                    then main lexbuf
                    else comment (depth - 1) lexbuf }
| _               { comment depth lexbuf }
```

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## Types of Formal Language Descriptions

- Regular expressions, regular grammars
- Context-free grammars, BNF grammars, syntax diagrams
- Finite state automata
- Pushdown automata
- Whole family more of grammars and automata – covered in automata theory

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## BNF Grammars

- Start with a set of characters, **a,b,c,...**
  - We call these *terminals*
- Add a set of different characters, **X,Y,Z,...**
  - We call these *nonterminals*
- One special nonterminal **S** called *start symbol*

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## Sample Grammar

- Language: Parenthesized sums of 0's and 1's
- $\langle \text{Sum} \rangle ::= 0$
- $\langle \text{Sum} \rangle ::= 1$
- $\langle \text{Sum} \rangle ::= \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$
- $\langle \text{Sum} \rangle ::= (\langle \text{Sum} \rangle)$

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## BNF Grammars

- BNF rules (aka *productions*) have form  
$$\mathbf{X} ::= y$$
where  $\mathbf{X}$  is any nonterminal and  $y$  is a string of terminals and nonterminals
- BNF *grammar* is a set of BNF rules such that every nonterminal appears on the left of some rule

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## Sample Grammar

- Terminals: 0 1 + ( )
- Nonterminals: <Sum>
- Start symbol = <Sum>
- <Sum> ::= 0
- <Sum> ::= 1
- <Sum> ::= <Sum> + <Sum>
- <Sum> ::= (<Sum>)
- Can be abbreviated as  
<Sum> ::= 0 | 1  
          | <Sum> + <Sum> | (<Sum>)

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## BNF Derivations

- Given rules

$$\mathbf{X} ::= y\mathbf{Z}w \text{ and } \mathbf{Z} ::= v$$

we may replace  $\mathbf{Z}$  by  $v$  to say

$$\mathbf{X} \Rightarrow y\mathbf{Z}w \Rightarrow yvw$$

- Sequence of such replacements called *derivation*
- Derivation called *right-most* if always replace the right-most non-terminal

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## BNF Semantics

- The meaning of a BNF grammar is the set of all strings consisting only of terminals that can be derived from the Start symbol

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## BNF Derivations

- Start with the start symbol:

<Sum> =>

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## BNF Derivations

- Pick a non-terminal

<Sum> =>

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## BNF Derivations

- Pick a rule and substitute:

- <Sum> ::= <Sum> + <Sum>

<Sum> => <Sum> + <Sum>

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## BNF Derivations

- Pick a non-terminal:

$\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$

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## BNF Derivations

- Pick a rule and substitute:

■  $\langle \text{Sum} \rangle ::= ( \langle \text{Sum} \rangle )$   
 $\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$   
 $\Rightarrow ( \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle$

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## BNF Derivations

- Pick a non-terminal:

$\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$   
 $\Rightarrow ( \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle$

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## BNF Derivations

- Pick a rule and substitute:

■  $\langle \text{Sum} \rangle ::= \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$   
 $\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$   
 $\Rightarrow ( \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle$   
 $\Rightarrow ( \langle \text{Sum} \rangle + \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle$

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## BNF Derivations

- Pick a non-terminal:

$\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$   
 $\Rightarrow ( \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle$   
 $\Rightarrow ( \langle \text{Sum} \rangle + \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle$

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## BNF Derivations

- Pick a rule and substitute:

■  $\langle \text{Sum} \rangle ::= 1$   
 $\langle \text{Sum} \rangle \Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle$   
 $\Rightarrow ( \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle$   
 $\Rightarrow ( \langle \text{Sum} \rangle + \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle$   
 $\Rightarrow ( \langle \text{Sum} \rangle + 1 ) + \langle \text{Sum} \rangle$

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## BNF Derivations

- Pick a non-terminal:

$$\begin{aligned}\langle \text{Sum} \rangle &\Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + 1 ) + \langle \text{Sum} \rangle\end{aligned}$$

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## BNF Derivations

- Pick a rule and substitute:

- $\langle \text{Sum} \rangle ::= 0$

$$\begin{aligned}\langle \text{Sum} \rangle &\Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + 1 ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + 1 ) + 0\end{aligned}$$

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## BNF Derivations

- Pick a non-terminal:

$$\begin{aligned}\langle \text{Sum} \rangle &\Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + 1 ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + 1 ) + 0\end{aligned}$$

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## BNF Derivations

- Pick a rule and substitute

- $\langle \text{Sum} \rangle ::= 0$

$$\begin{aligned}\langle \text{Sum} \rangle &\Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + 1 ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + 1 ) 0 \\ &\Rightarrow ( 0 + 1 ) + 0\end{aligned}$$

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## BNF Derivations

- $( 0 + 1 ) + 0$  is generated by grammar

$$\begin{aligned}\langle \text{Sum} \rangle &\Rightarrow \langle \text{Sum} \rangle + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + \langle \text{Sum} \rangle ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + 1 ) + \langle \text{Sum} \rangle \\ &\Rightarrow ( \langle \text{Sum} \rangle + 1 ) + 0 \\ &\Rightarrow ( 0 + 1 ) + 0\end{aligned}$$

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## Extended BNF Grammars

- Alternatives: allow rules of form  $X ::= y \mid z$ 
  - Abbreviates  $X ::= y, X ::= z$
- Options:  $X ::= y [v] z$ 
  - Abbreviates  $X ::= y v z, X ::= y z$
- Repetition:  $X ::= y \{v\}^* z$ 
  - Can be eliminated by adding new nonterminal  $V$  and rules  $X ::= y z, X ::= y V z, V ::= v, V ::= v V$

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## Parse Trees

- Graphical representation of derivation
- Each node labeled with either non-terminal or terminal
- If node is labeled with a terminal, then it is a leaf (no sub-trees)
- If node is labeled with a non-terminal, then it has one branch for each character in the right-hand side of rule used to substitute for it

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## Example

- Consider grammar:  
 $\langle \text{exp} \rangle ::= \langle \text{factor} \rangle$   
 $\quad \quad \quad | \langle \text{factor} \rangle + \langle \text{factor} \rangle$   
 $\langle \text{factor} \rangle ::= \langle \text{bin} \rangle$   
 $\quad \quad \quad | \langle \text{bin} \rangle * \langle \text{exp} \rangle$   
 $\langle \text{bin} \rangle ::= 0 \mid 1$
- Problem: Build parse tree for  $1 * 1 + 0$  as an  $\langle \text{exp} \rangle$

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## Example cont.

- $1 * 1 + 0$ :  $\langle \text{exp} \rangle$

$\langle \text{exp} \rangle$  is the start symbol for this parse tree

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## Example cont.

- $1 * 1 + 0$ :  $\langle \text{exp} \rangle$   
 $\quad \quad \quad |$   
 $\quad \quad \quad \langle \text{factor} \rangle$

Use rule:  $\langle \text{exp} \rangle ::= \langle \text{factor} \rangle$

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## Example cont.

- $1 * 1 + 0$ :  $\langle \text{exp} \rangle$   
 $\quad \quad \quad |$   
 $\quad \quad \quad \langle \text{factor} \rangle$   
 $\quad \quad \quad / \quad | \quad \backslash$   
 $\quad \quad \quad \langle \text{bin} \rangle \quad * \quad \langle \text{exp} \rangle$

Use rule:  $\langle \text{factor} \rangle ::= \langle \text{bin} \rangle * \langle \text{exp} \rangle$

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## Example cont.

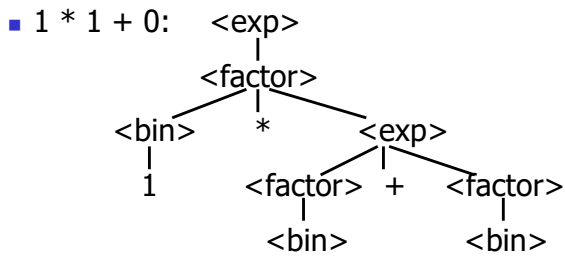
- $1 * 1 + 0$ :  $\langle \text{exp} \rangle$   
 $\quad \quad \quad |$   
 $\quad \quad \quad \langle \text{factor} \rangle$   
 $\quad \quad \quad / \quad | \quad \backslash$   
 $\quad \quad \quad \langle \text{bin} \rangle \quad * \quad \langle \text{exp} \rangle$   
 $\quad \quad \quad | \quad \quad \quad / \quad | \quad \backslash$   
 $\quad \quad \quad 1 \quad \quad \quad \langle \text{factor} \rangle \quad + \quad \langle \text{factor} \rangle$

Use rules:  $\langle \text{bin} \rangle ::= 1$  and  
 $\langle \text{exp} \rangle ::= \langle \text{factor} \rangle + \langle \text{factor} \rangle$

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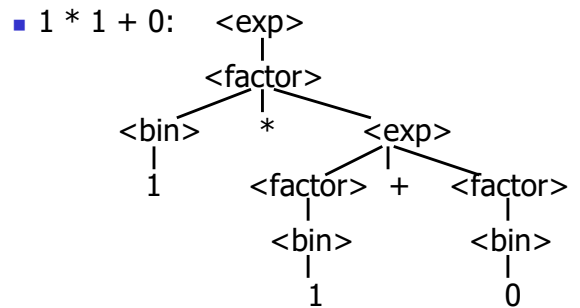
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### Example cont.



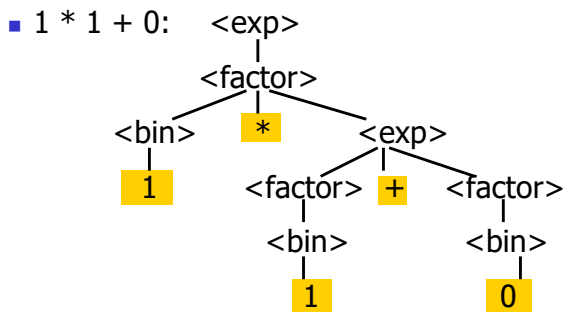
Use rule:  $\langle \text{factor} \rangle ::= \langle \text{bin} \rangle$

### Example cont.



Use rules:  $\langle \text{bin} \rangle ::= 1 \mid 0$

### Example cont.



Fringe of tree is string generated by grammar

### Your Turn: 1 \* 0 + 0 \* 1

