Programming Languages and Compilers (CS 421)

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http://courses.engr.illinois.edu/cs421

Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha

Mechanics

Put table of reg exp and corresponding actions (written in ocaml) into a file <*filename*>.mll

Call

ocamllex < *filename*>.mll

 Produces Ocaml code for a lexical analyzer in file <*filename>*.ml

Sample Input

```
rule main = parse
[0'-9']+ \{ print string "Int n" \}
| ['0'-'9']+'.'['0'-'9']+ { print_string "Float\n"}
[ ['a'-'z']+ { print_string "String\n"}
{ main lexbuf }
let newlexbuf = (Lexing.from channel stdin) in
main newlexbuf
```

General Input

```
{ header }
let ident = regexp ...
rule entrypoint [arg1... argn] = parse
     regexp { action }
   | regexp { action }
and entrypoint [arg1... argn] = parse ...and
  . . .
{ trailer }
```

Ocamllex Input

header and trailer contain arbitrary ocaml code put at top an bottom of <filename>.ml

Iet *ident* = *regexp* ... Introduces *ident* for use in later regular expressions

Ocamllex Input

<filename>.ml contains one lexing function per entrypoint

- Name of function is name given for entrypoint
- Each entry point becomes an Ocaml function that takes n+1 arguments, the extra implicit last argument being of type Lexing.lexbuf

arg1... argn are for use in action

Ocamllex Regular Expression

- Single quoted characters for letters:
 'a'
- _: (underscore) matches any letter
- Eof: special "end_of_file" marker
- Concatenation same as usual
- *string*": concatenation of sequence of characters
- e_1 / e_2 : choice what was $e_1 \vee e_2$

Ocamllex Regular Expression

- [C₁ C₂]: choice of any character between first and second inclusive, as determined by character codes
- [^c₁ c₂]: choice of any character NOT in set
- *e**: same as before
- e+: same as e e*
- e?: option was $e \vee \epsilon$
- (*e*): same as *e*

Ocamllex Regular Expression

- *e*₁ # *e*₂: the characters in *e*₁ but not in *e*₂;
 *e*₁ and *e*₂ must describe just sets of characters
- *ident*: abbreviation for earlier reg exp in let *ident* = *regexp*
- *e*₁ as *id*: binds the result of *e*₁ to *id* to be used in the associated *action*

Ocamllex Manual

 More details can be found at
 Version for ocaml 4.07: <u>https://v2.ocaml.org/releases/4.07/htmlman/le</u> <u>xyacc.html</u>

Current version (ocaml 4.14)

https://v2.ocaml.org/releases/4.14/htmlman/le xyacc.html

(same, except formatting, I think)

Example : test.mll

{ type result = Int of int | Float of float | String of string } let digit = ['0'-'9']let digits = digit + let lower case = ['a'-'z']let upper_case = ['A'-'Z']let letter = upper case | lower case let letters = letter +

Example : test.mll

rule main = parse

- (digits)'.'digits as f { Float (float_of_string f) }
 digits as n (Int (int of string n))
- digits as n
- | letters as s

- { Int (int_of_string n) }
 { String s}
- | _ { main lexbuf }
- { let newlexbuf = (Lexing.from_channel stdin) in
 print_newline ();
 main newlexbuf }

Example

#use "test.ml";;

val main : Lexing.lexbuf -> result = <fun>

- val __ocaml_lex_main_rec : Lexing.lexbuf -> int ->
 result = <fun>
- hi there 234 5.2
- : result = String "hi"

What happened to the rest?!?

. . .

Example

- # let b = Lexing.from_channel stdin;;
- # main b;;
- hi 673 there
- : result = String "hi"
- # main b;;
- : result = Int 673
- # main b;;
- : result = String "there"

Problem

- How to get lexer to look at more than the first token at one time?
- Answer: action has to tell it to -- recursive calls
 - Not what you want to sew this together with ocamlyacc
- Side Benefit: can add "state" into lexing
- Note: already used this with the _ case



```
rule main = parse
  (digits) '.' digits as f { Float
  (float_of_string f) :: main lexbuf}
                     { Int (int_of_string n) ::
| digits as n
  main lexbuf }
                     { String s :: main
| letters as s
  lexbuf}
 eof
                      { [] }
                      { main lexbuf }
```

Example Results

hi there 234 5.2

 result list = [String "hi"; String "there"; Int 234; Float 5.2]

#

Used Ctrl-d to send the end-of-file signal

Dealing with comments

First Attempt

Dealing with comments

| open_comment { comment lexbuf}
| eof { [] }
| _ { main lexbuf }
and comment = parse
close_comment { main lexbuf }
| _ { comment lexbuf }

Dealing with nested comments

```
rule main = parse ...
 open_comment { comment 1 lexbuf}
l eof
                { [] }
| { main lexbuf }
and comment depth = parse
 open comment { comment (depth+1) lexbuf
 close_comment { if depth = 1
                then main lexbuf
               else comment (depth - 1) lexbuf }
               { comment depth lexbuf }
```

Dealing with nested comments

rule main = parse

- (digits) '.' digits as f { Float (float_of_string f) :: main lexbuf}
- | digits as n { Int (int_of_string n) :: main lexbuf }
- letters as s { String s :: main lexbuf}
- open_comment { (comment 1 lexbuf}
- | eof { [] }
- | _ { main lexbuf }

Dealing with nested comments

and comment depth = parse open_comment { comment (depth+1) lexbuf } | close_comment { if depth = 1 then main lexbuf else comment (depth - 1) lexbuf } { comment depth lexbuf }

Types of Formal Language Descriptions

- Regular expressions, regular grammars
- Context-free grammars, BNF grammars, syntax diagrams
- Finite state automata
- Pushdown automata
- Whole family more of grammars and automata – covered in automata theory

BNF Grammars

Start with a set of characters, a,b,c,... We call these *terminals*

Add a set of different characters, X,Y,Z,...

We call these *nonterminals*

One special nonterminal S called *start* symbol

BNF Grammars

BNF rules (aka *productions*) have form

X ::= *y*

where **X** is any nonterminal and y is a string of terminals and nonterminals

BNF grammar is a set of BNF rules such that every nonterminal appears on the left of some rule

Sample Grammar

Terminals: 0 1 + () Nonterminals: <Sum> Start symbol = <Sum> Sum> ::= 0 Sum >::= 1 Sum> ::= <Sum> + <Sum> Sum> ::= (<Sum>) Can be abbreviated as <Sum> ::= 0 | 1 <Sum> + <Sum> | (<Sum>)

BNF Deriviations

Given rules

X::= *y***Z***w* and **Z::**=*v*

we may replace Z by v to say

X => yZW => yVW

- Sequence of such replacements called derivation
- Derivation called *right-most* if always replace the right-most non-terminal

BNF Semantics

The meaning of a BNF grammar is the set of all strings consisting only of terminals that can be derived from the Start symbol



Start with the start symbol:

<Sum> =>



Pick a non-terminal



BNF Derivations

Pick a rule and substitute: <Sum> ::= <Sum> + <Sum> <Sum> => <Sum> + <Sum>



Pick a non-terminal:

<Sum> => <Sum> + <Sum >

BNF Derivations

Pick a rule and substitute: <Sum> ::= (<Sum>) <Sum> => <Sum> + <Sum > => (<Sum>) + <Sum>



Pick a non-terminal:

<Sum> => <Sum> + <Sum > => (<Sum>) + <Sum>

BNF Derivations

Pick a rule and substitute: <Sum> ::= <Sum> + <Sum> <Sum> => <Sum> + <Sum > => (<Sum>) + <Sum> => (<Sum> + <Sum>) + <Sum> => (<Sum> + <Sum>) + <Sum>



Pick a non-terminal:

<Sum> => <Sum> + <Sum > => (<Sum>) + <Sum> => (<Sum> + <Sum>) + <Sum>

BNF Derivations

Pick a rule and substitute: <Sum >::= 1 <Sum> => <Sum> + <Sum > => (<Sum>) + <Sum> => (<Sum> + <Sum>) + <Sum> => (<Sum> + <Sum>) + <Sum> => (<Sum> + 1) + <Sum>



Pick a non-terminal:

<Sum> => <Sum> + <Sum > => (<Sum>) + <Sum> => (<Sum> + <Sum>) + <Sum> => (<Sum> + 1) + <Sum>

BNF Derivations

Pick a rule and substitute: Sum >::= 0 $\langle Sum \rangle = \langle Sum \rangle + \langle Sum \rangle$ => (<Sum>) + <Sum> => (<Sum> + <Sum>) + <Sum> => (<Sum> + 1) + <Sum> => (<Sum> + 1) + 0



Pick a non-terminal:

<Sum> => <Sum> + <Sum > => (<Sum>) + <Sum> => (<Sum> + <Sum>) + <Sum> => (<Sum> + 1) + <Sum> => (<Sum> + 1) + 0

BNF Derivations

Pick a rule and substitute Sum> ::= 0 $\langle Sum \rangle = \langle Sum \rangle + \langle Sum \rangle$ => (<Sum>) + <Sum> => (<Sum> + <Sum>) + <Sum> => (<Sum> + 1) + <Sum> => (<mark><Sum></mark> + 1) 0 =>(0+1)+0

BNF Derivations (0+1)+0 is generated by grammar $\langle Sum \rangle = \langle Sum \rangle + \langle Sum \rangle$ => (<Sum>) + <Sum> => (<Sum> + <Sum>) + <Sum> => (<Sum> + 1) + <Sum> => (<Sum > + 1) + 0=>(0+1)+0

Extended BNF Grammars

- Alternatives: allow rules of from X::= y/z
 - Abbreviates X::= y, X::= z
- Options: X::= y[v]z
 - Abbreviates X::= yvz, X::= yz
- Repetition: X::= y{ v}*z
 - Can be eliminated by adding new nonterminal V and rules X::= yZ, X::= yVZ, V::= v, V::= W

Parse Trees

- Graphical representation of derivation
- Each node labeled with either non-terminal or terminal
- If node is labeled with a terminal, then it is a leaf (no sub-trees)
- If node is labeled with a non-terminal, then it has one branch for each character in the right-hand side of rule used to substitute for it

Example

Consider grammar: <exp> ::= <factor> | <factor> + <factor> <factor> ::= <bin> | <bin> * <exp> <bin> ::= 0 | 1

Problem: Build parse tree for 1 * 1 + 0 as an <exp>



■ 1 * 1 + 0: <exp>

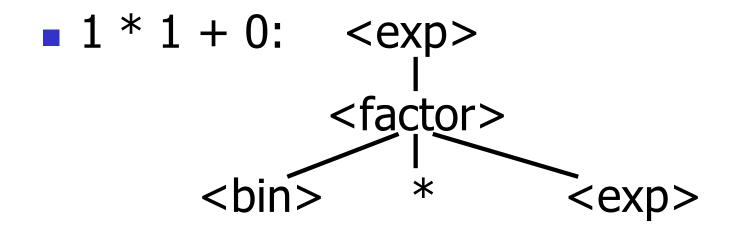
<exp> is the start symbol for this parse tree



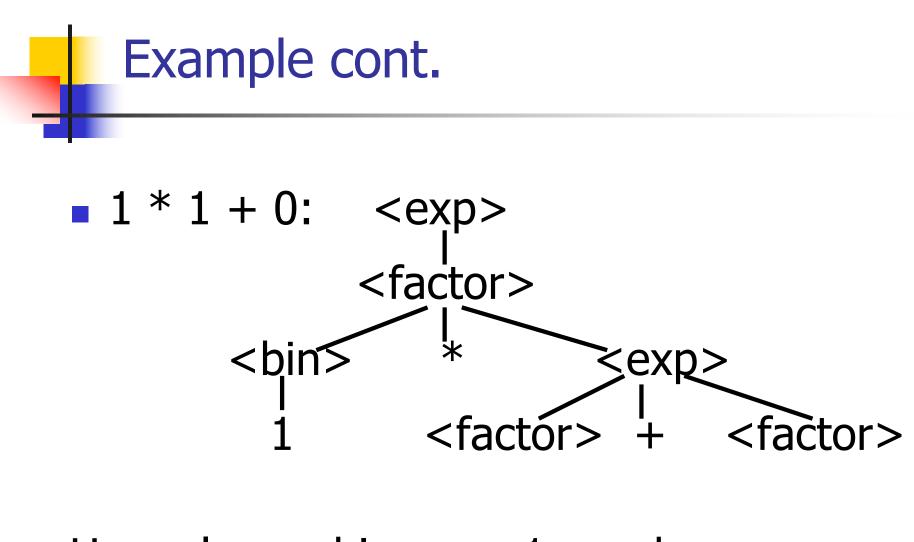
1 * 1 + 0: <exp> | <factor>

Use rule: <exp> ::= <factor>



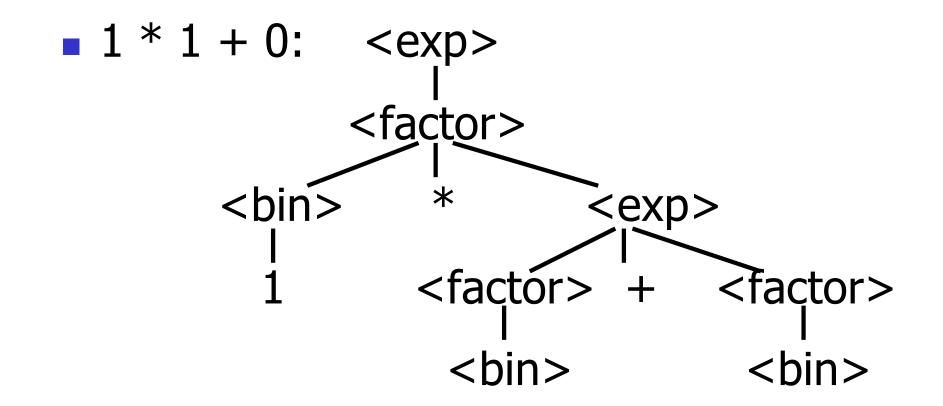


Use rule: <factor> ::= <bin> * <exp>



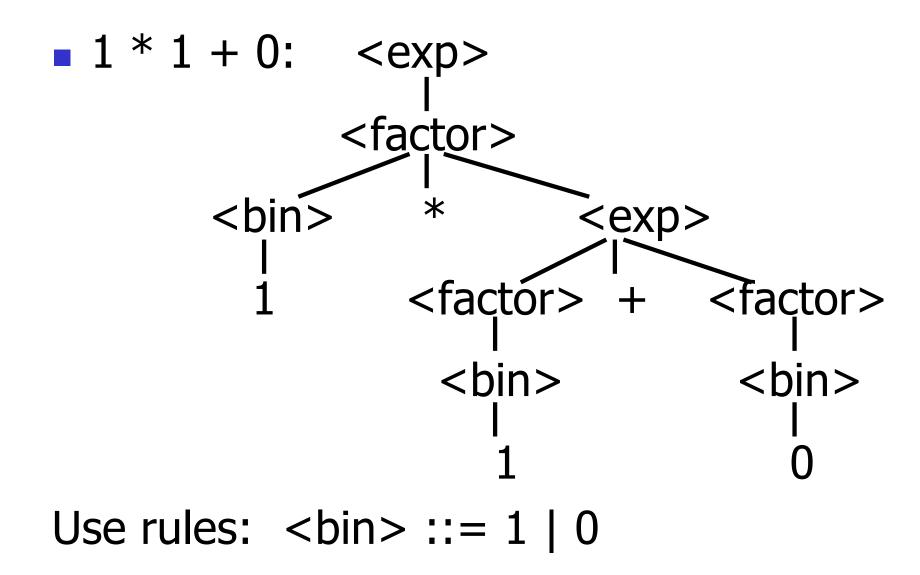
Use rules: <bin> ::= 1 and <exp> ::= <factor> + <factor>



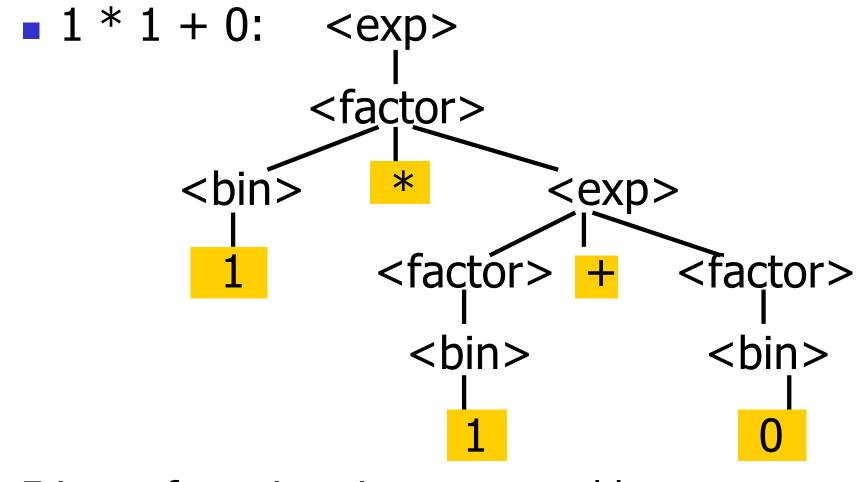


Use rule: <factor> ::= <bin>









Fringe of tree is string generated by grammar

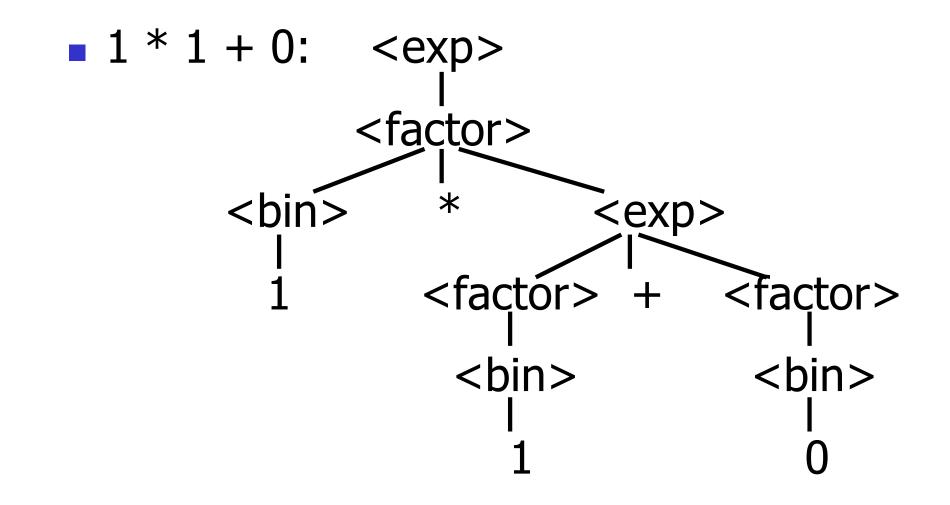
Parse Tree Data Structures

- Parse trees may be represented by OCaml datatypes
- One datatype for each nonterminal
- One constructor for each rule
- Defined as mutually recursive collection of datatype declarations

Example

Recall grammar: <exp> ::= <factor> | <factor> + <factor> < factor > ::= < bin > | < bin > * < exp ><bin> ::= 0 | 1 type exp = Factor2Exp of factor | Plus of factor * factor and factor = Bin2Factor of bin | Mult of bin * exp and bin = Zero | One







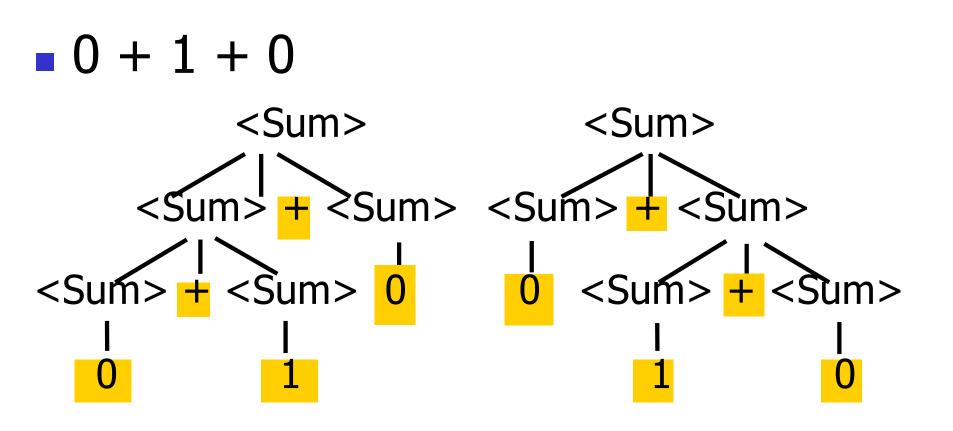
Can be represented as

Factor2Exp (Mult(One, Plus(Bin2Factor One, Bin2Factor Zero)))

Ambiguous Grammars and Languages

- A BNF grammar is *ambiguous* if its language contains strings for which there is more than one parse tree
- If all BNF's for a language are ambiguous then the language is *inherently ambiguous*

Example: Ambiguous Grammar



Two Major Sources of Ambiguity

- Lack of determination of operator precedence
- Lack of determination of operator assoicativity

Not the only sources of ambiguity

Disambiguating a Grammar

 Given ambiguous grammar G, with start symbol S, find a grammar G' with same start symbol, such that

language of G = language of G'

- Not always possible
- No algorithm in general

Disambiguating a Grammar

- Idea: Each non-terminal represents all strings having some property
- Identify these properties (often in terms of things that can't happen)
- Use these properties to inductively guarantee every string in language has a unique parse

Steps to Grammar Disambiguation

- Identify the rules and a smallest use that display ambiguity
- Decide which parse to keep; why should others be thrown out?
- What syntactic restrictions on subexpressions are needed to throw out the bad (while keeping the good)?
- Add a new non-terminal and rules to describe this set of restricted subexpressions (called stratifying, or refactoring)
- Characterize each non-terminal by a language invariant
- Replace old rules to use new non-terminals
- Rinse and repeat



Ambiguous grammar: <exp> ::= 0 | 1 | <exp> + <exp> | <exp> * <exp> String with more then one parse: 0 + 1 + 0 1 * 1 + 1 Sourceof ambiuity: associativity and

precedence

Two Major Sources of Ambiguity

- Lack of determination of operator precedence
- Lack of determination of operator assoicativity

Not the only sources of ambiguity

How to Enforce Associativity

Have at most one recursive call per production

When two or more recursive calls would be natural leave right-most one for right assoicativity, left-most one for left assoiciativity

Example

Sum> ::= 0 | 1 | <Sum> + <Sum> | (<Sum>)

Becomes

- Sum> ::= <Num> | <Num> + <Sum>
- Num> ::= 0 | 1 | (<Sum>)

<Sum> + <Sum> + <Sum>

Operator Precedence

 Operators of highest precedence evaluated first (bind more tightly).

- Precedence for infix binary operators given in following table
- Needs to be reflected in grammar

Precedence Table - Sample

	Fortan	Pascal	C/C++	Ada	SML
highest	**	*, /, div, mod	++,	**	div, mod, /, *
	*,/	+,-	*,/, %	*, /, mod	+, -, ^
	+,-		+,-	+, -	

Predence in Grammar

- Higher precedence translates to longer derivation chain
- Example:
- <exp> ::= 0 | 1 | <exp> + <exp> | <exp> * <exp>

Becomes

Parser Code

- *grammar*>.mly defines one parsing function per entry point
- Parsing function takes a lexing function (lexer buffer to token) and a lexer buffer as arguments
- Returns semantic attribute of corresponding entry point

Ocamlyacc Input

File format: %{ <header> %} < declarations> %% <rules> %%

<trailer>

Ocamlyacc < header>

- Contains arbitrary Ocaml code
- Typically used to give types and functions needed for the semantic actions of rules and to give specialized error recovery
- May be omitted
- < footer> similar. Possibly used to call parser

Ocamlyacc <declarations>

%token symbol ... symbol

- Declare given symbols as tokens
 %token < type> symbol ... symbol
- Declare given symbols as token constructors, taking an argument of type <*type*>

%start symbol ... symbol

 Declare given symbols as entry points; functions of same names in < grammar>.ml

Ocamlyacc < declarations>

%type <type> symbol ... symbol

Specify type of attributes for given symbols. Mandatory for start symbols

- %left symbol ... symbol
- %right symbol ... symbol
- %nonassoc symbol ... symbol

Associate precedence and associativity to given symbols. Same line, same precedence; earlier line, lower precedence (broadest scope)

Ocamlyacc <*rules*>

- nonterminal :
 symbol ... symbol { semantic_action }
 ...
 symbol ... symbol { semantic_action }
- Semantic actions are arbitrary Ocaml expressions
- Must be of same type as declared (or inferred) for *nonterminal*
- Access semantic attributes (values) of symbols by position: \$1 for first symbol, \$2 to second ...

Example - Base types

```
(* File: expr.ml *)
type expr =
  Term_as_Expr of term
 | Plus_Expr of (term * expr)
 | Minus_Expr of (term * expr)
and term =
  Factor as Term of factor
  Mult Term of (factor * term)
 Div Term of (factor * term)
and factor =
  Id_as_Factor of string
 | Parenthesized_Expr_as_Factor of expr
```

Example - Lexer (exprlex.mll)

```
{ (*open Exprparse*) }
let numeric = ['0' - '9']
let letter = ['a' - 'z' 'A' - 'Z']
rule token = parse
  "+" {Plus_token}
  "-" {Minus token}
  "*" {Times_token}
 | "/" {Divide_token}
 | "(" {Left_parenthesis}
 | ")" {Right_parenthesis}
  letter (letter numeric "_")* as id {Id_token id}
 | [' ' ' t' ' n'] \{token lexbuf\}
 | eof {EOL}
```

%{ open Expr %} %token <string> Id_token %token Left_parenthesis Right_parenthesis %token Times token Divide token %token Plus token Minus token %token EOL %start main %type <expr> main %%

expr: term { Term_as_Expr \$1 } | term Plus_token expr { Plus_Expr (\$1, \$3) } | term Minus_token expr { Minus_Expr (\$1, \$3) }

term:

factor
{ Factor_as_Term \$1 }
| factor Times_token term
{ Mult_Term (\$1, \$3) }
| factor Divide_token term
{ Div_Term (\$1, \$3) }

factor: Id token { Id as Factor \$1 } | Left _parenthesis expr Right_parenthesis {Parenthesized_Expr_as_Factor \$2 } main: | expr EOL { \$1 }

Example - Using Parser

```
# #use "expr.ml";;
```

```
# #use "exprparse.ml";;
```

```
# #use "exprlex.ml";;
```

. . .

```
# let test s =
```

```
let lexbuf = Lexing.from_string (s^"\n") in
main token lexbuf;;
```

Example - Using Parser

test "a + b";;

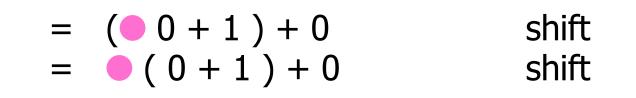
- -: expr =
- Plus_Expr
 - (Factor_as_Term (Id_as_Factor "a"),
 - Term_as_Expr (Factor_as_Term (Id_as_Factor "b")))

LR Parsing

- Read tokens left to right (L)
- Create a rightmost derivation (R)
- How is this possible?
- Start at the bottom (left) and work your way up
- Last step has only one non-terminal to be replaced so is right-most
- Working backwards, replace mixed strings by non-terminals
- Always proceed so that there are no nonterminals to the right of the string to be replaced

<Sum> =>

= (0 + 1) + 0 shift



$$=> (0 + 1) + 0 reduce= (0 + 1) + 0 shift= (0 + 1) + 0 shift$$

$$= (+ 1) + 0 \qquad shift=> (0 + 1) + 0 \qquad reduce= (0 + 1) + 0 \qquad shift= (0 + 1) + 0 \qquad shift$$

$$= (+ • 1) + 0 \qquad shift \\ = (• + 1) + 0 \qquad shift \\ => (0 • + 1) + 0 \qquad reduce \\ = (• 0 + 1) + 0 \qquad shift \\ = • (0 + 1) + 0 \qquad shift \\ = • (0 + 1) + 0 \qquad shift \end{cases}$$

<Sum> =>

$$=> (+ 1 •) + 0$$

= (+ • 1) + 0
= (• + 1) + 0
=> (0 • + 1) + 0
= (• 0 + 1) + 0
= (0 + 1) + 0

reduce shift shift reduce shift shift

$$=> (+) + 0 reduce => (+ 1) + 0 reduce = (+ 1) + 0 shift = (+ 1) + 0 shift => (0 + 1) + 0 reduce = (0 + 1) + 0 shift = (0 + 1) + 0 shift = (0 + 1) + 0 shift shift = (0 + 1) + 0 shift shift$$

$$= (•) + 0 \qquad \text{shift} \\ => (+ •) + 0 \qquad \text{reduce} \\ => (+ 1 •) + 0 \qquad \text{reduce} \\ = (+ • 1) + 0 \qquad \text{shift} \\ = (• + 1) + 0 \qquad \text{shift} \\ => (0 • + 1) + 0 \qquad \text{reduce} \\ = (• 0 + 1) + 0 \qquad \text{shift} \\ = • (0 + 1) + 0 \qquad \text{shift} \\ = • (0 + 1) + 0 \qquad \text{shift} \end{cases}$$

$$=> () + 0 reduce$$

$$= () + 0 shift$$

$$=> (+) + 0 reduce$$

$$= (+ 1 + 0) + 0 reduce$$

$$= (+ 1) + 0 shift$$

$$= (+ 1) + 0 shift$$

$$= (<0 + 1) + 0 reduce$$

$$= (0 + 1) + 0 shift$$

$$= (0 + 1) + 0 shift$$

$$= (0 + 1) + 0 shift$$

$$= \langle Sum \rangle \bullet + 0 \qquad \text{shift}$$

$$= \rangle (\langle Sum \rangle \bullet + 0 \qquad \text{reduce}$$

$$= (\langle Sum \rangle \bullet + 0 \qquad \text{shift}$$

$$= \rangle (\langle Sum \rangle + \langle Sum \rangle \bullet) + 0 \qquad \text{reduce}$$

$$= (\langle Sum \rangle + 1 \bullet) + 0 \qquad \text{reduce}$$

$$= (\langle Sum \rangle \bullet + 1) + 0 \qquad \text{shift}$$

$$= \langle 0 \bullet + 1 \rangle + 0 \qquad \text{reduce}$$

$$= (\bullet 0 + 1) + 0 \qquad \text{reduce}$$

$$= (\bullet 0 + 1) + 0 \qquad \text{shift}$$

$$= \bullet (0 + 1) + 0 \qquad \text{shift}$$

<Sum> =>

shift = <Sum> + • 0 shift = <Sum > = +0=> (<Sum>) • + 0 reduce = (< Sum >) + 0shift => (<Sum> + <Sum>) + 0 reduce => (<Sum> + 1 •) + 0 reduce = (<Sum > + = 1) + 0shift = (< Sum > = + 1) + 0shift => (0 • + 1) + 0 reduce = ($\bigcirc 0 + 1$) + 0 shift = (0 + 1) + 0 shift

$$= \langle Sum \rangle + 0 \quad \text{reduce}$$

$$= \langle Sum \rangle + 0 \quad \text{shift}$$

$$= \langle Sum \rangle + 0 \quad \text{shift}$$

$$= \rangle (\langle Sum \rangle) + 0 \quad \text{reduce}$$

$$= (\langle Sum \rangle + \langle Sum \rangle) + 0 \quad \text{reduce}$$

$$= \langle (Sum \rangle + \langle Sum \rangle) + 0 \quad \text{reduce}$$

$$= \langle (Sum \rangle + 1) + 0 \quad \text{reduce}$$

$$= (\langle Sum \rangle + 1) + 0 \quad \text{shift}$$

$$= \langle (Sum \rangle + 1) + 0 \quad \text{shift}$$

$$= \langle 0 + 1 \rangle + 0 \quad \text{shift}$$

$$= (0 + 1) + 0 \quad \text{shift}$$

$$= (0 + 1) + 0 \quad \text{shift}$$

reduce <Sum> => <Sum> + <Sum > ● => <Sum> + 0 reduce = <Sum > + = 0shift shift = <Sum > = + 0=> (<Sum>) • + 0 reduce = (< Sum >) + 0shift => (<Sum> + <Sum>) + 0 reduce => (<Sum> + 1 •) + 0 reduce = (<Sum > + = 1) + 0shift = (< Sum > + 1) + 0shift => (0 • + 1) + 0 reduce = ($\bigcirc 0 + 1$) + 0 shift = (0 + 1) + 0 shift

reduce <Sum> => <Sum> + <Sum > = => <Sum> + 0 reduce = <Sum > + = 0shift shift = <Sum > = + 0=> (<Sum>) • + 0 reduce = (< Sum >) + 0shift => (<Sum> + <Sum>) + 0 reduce => (<Sum> + 1 •) + 0 reduce = (<Sum > + = 1) + 0shift = (< Sum > + 1) + 0shift => (0 • + 1) + 0 reduce = ($\bigcirc 0 + 1$) + 0 shift = (0 + 1) + 0 shift



(0 + 1) + 0

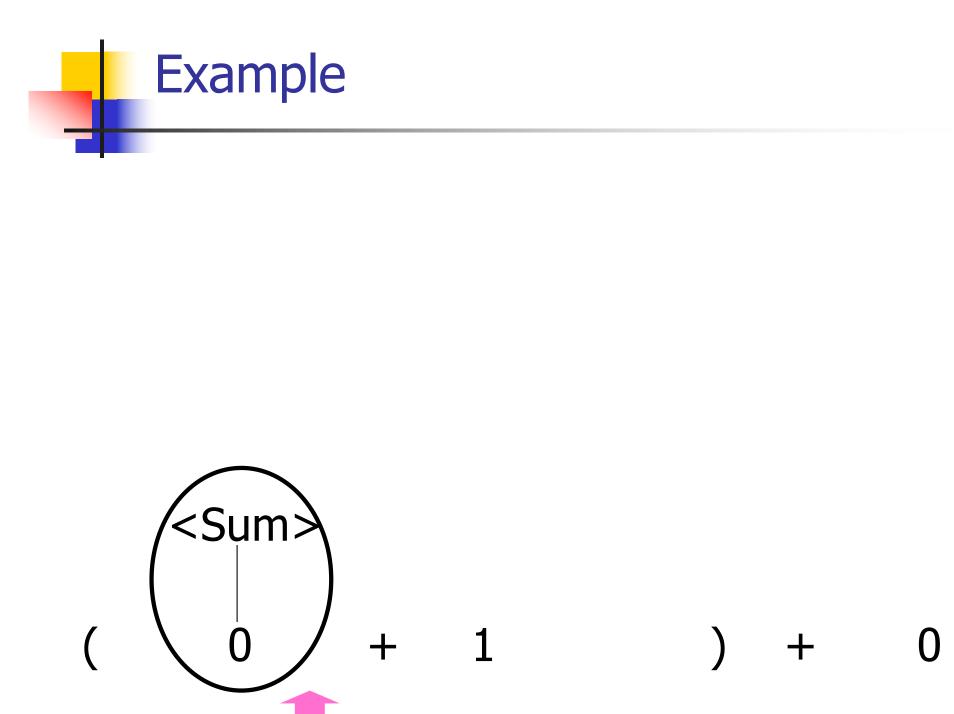
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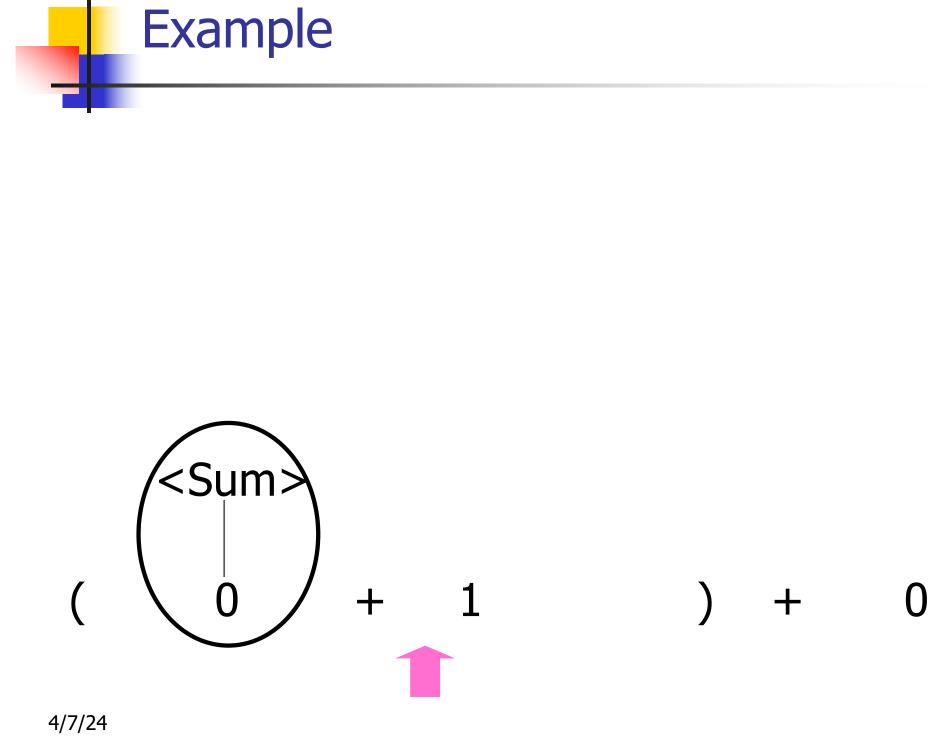


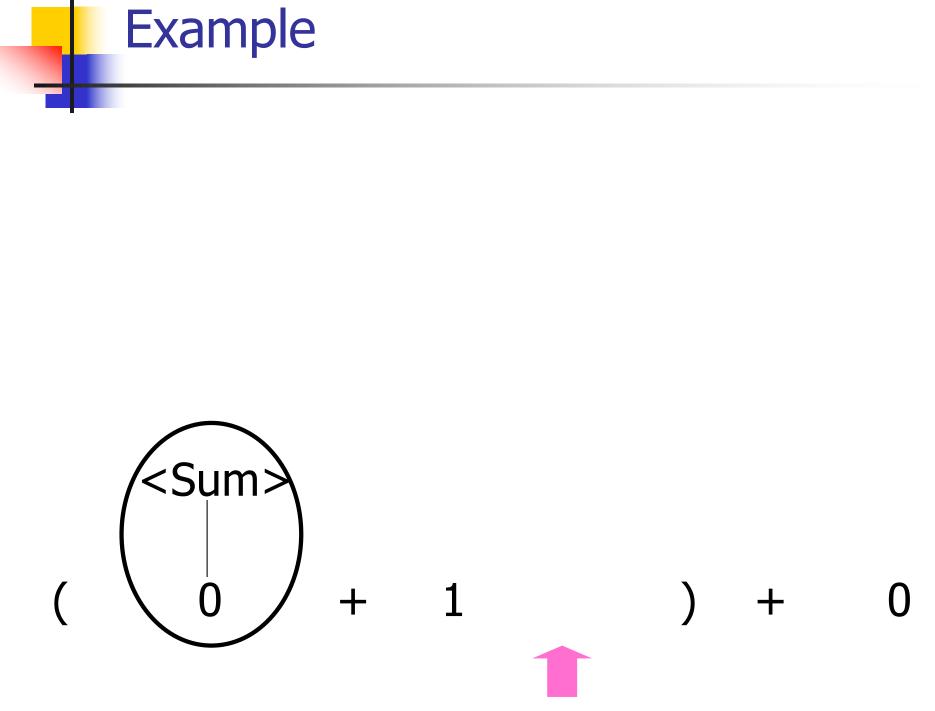
(0 + 1) + 0

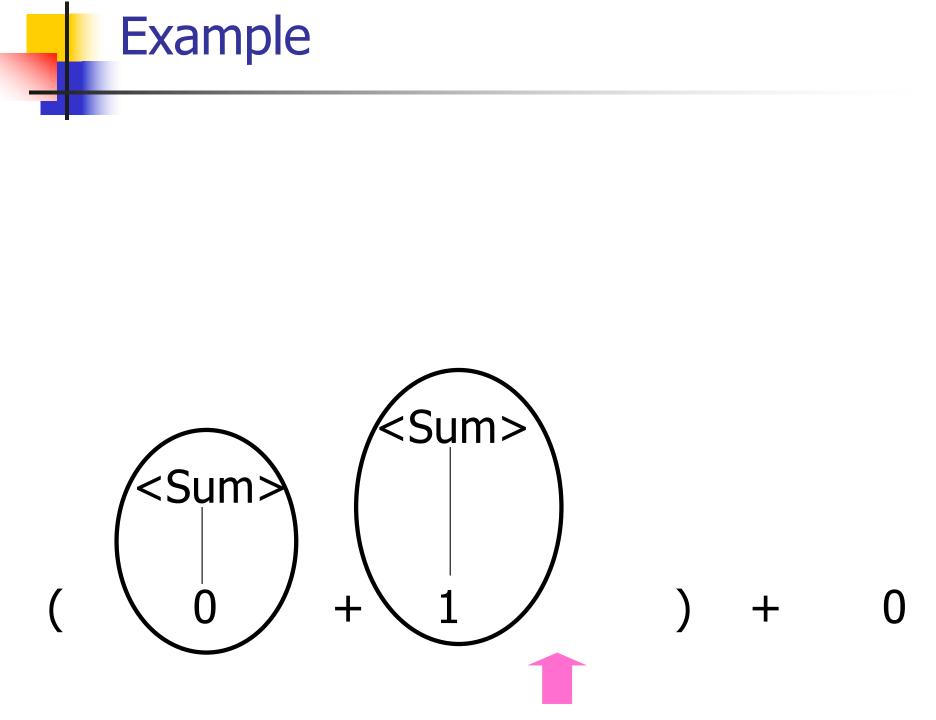


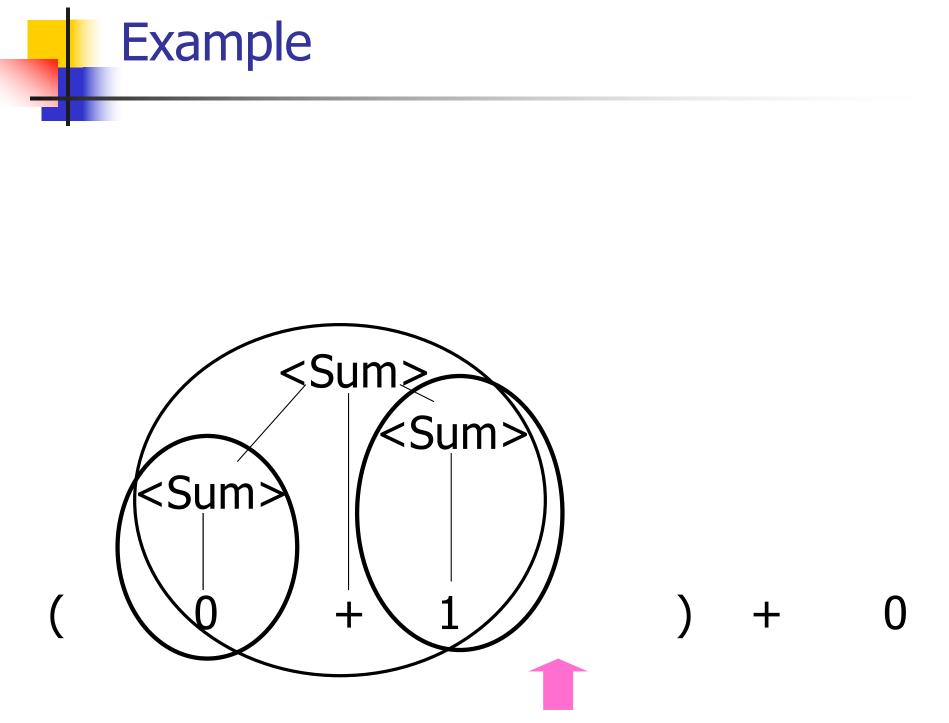
(0 + 1) + 0

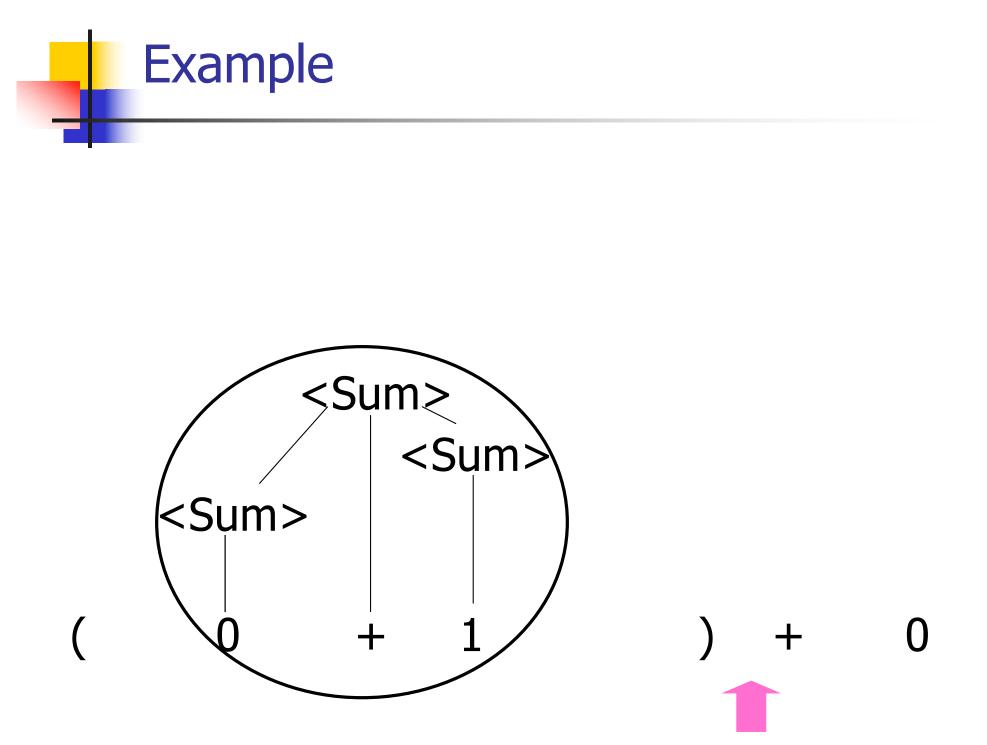


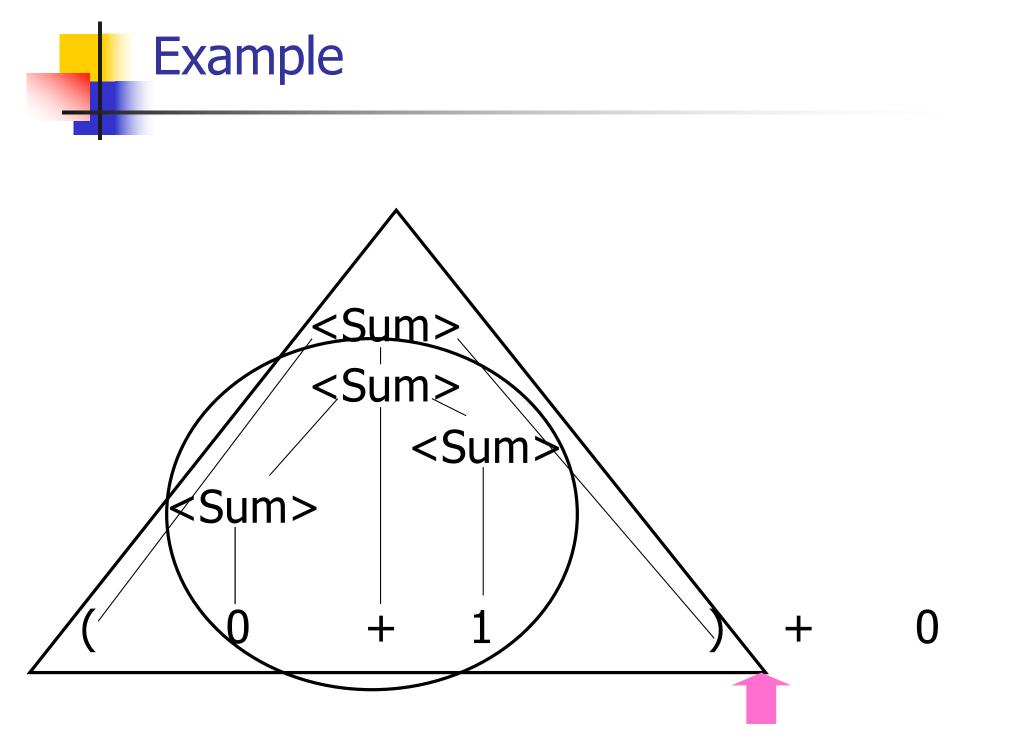


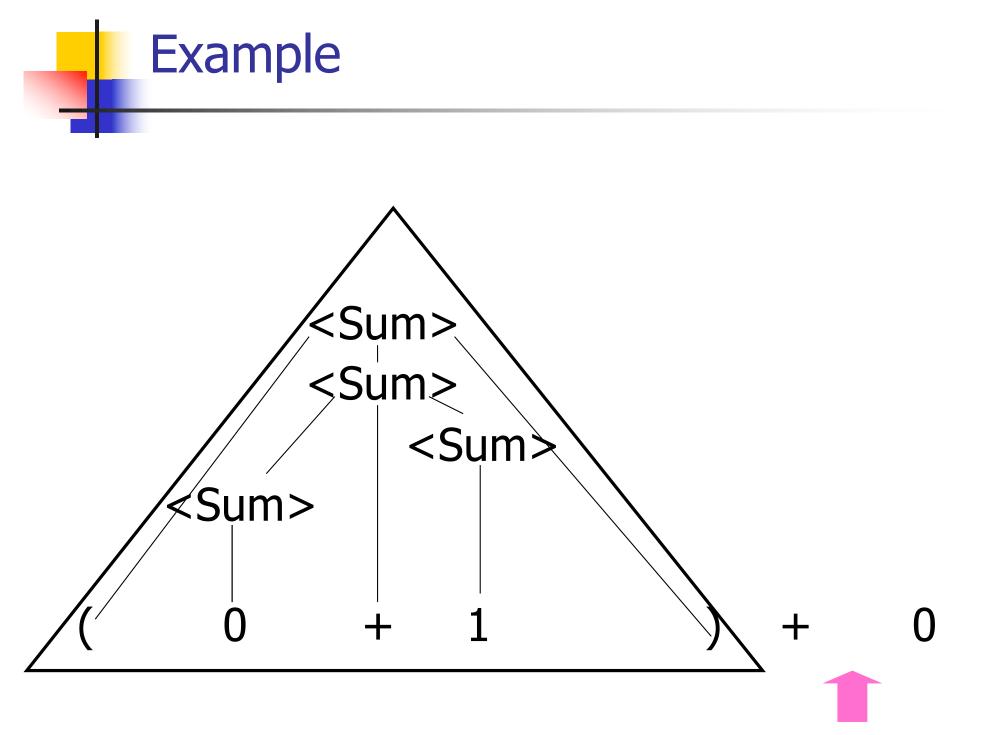


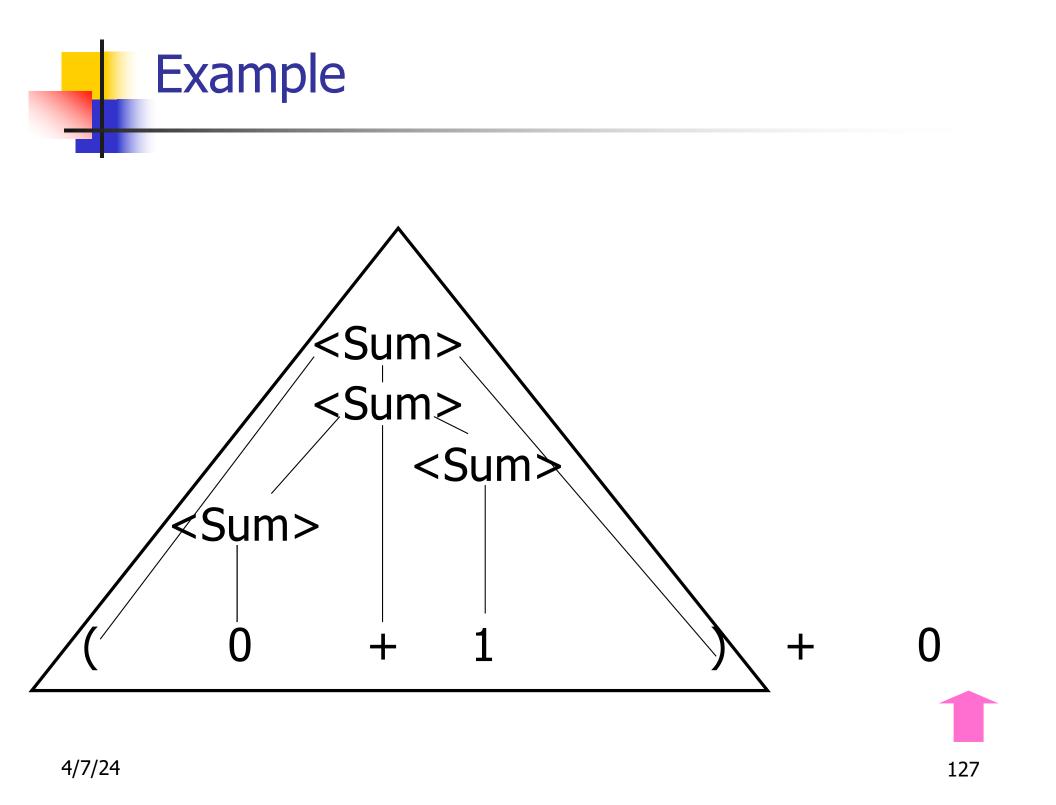


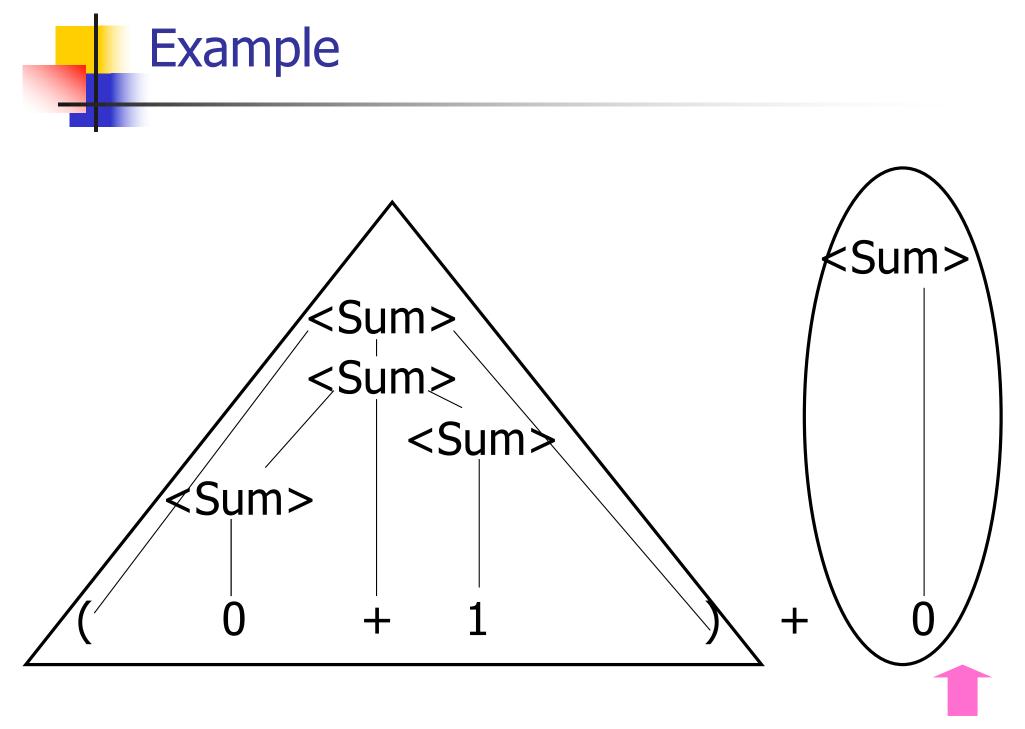


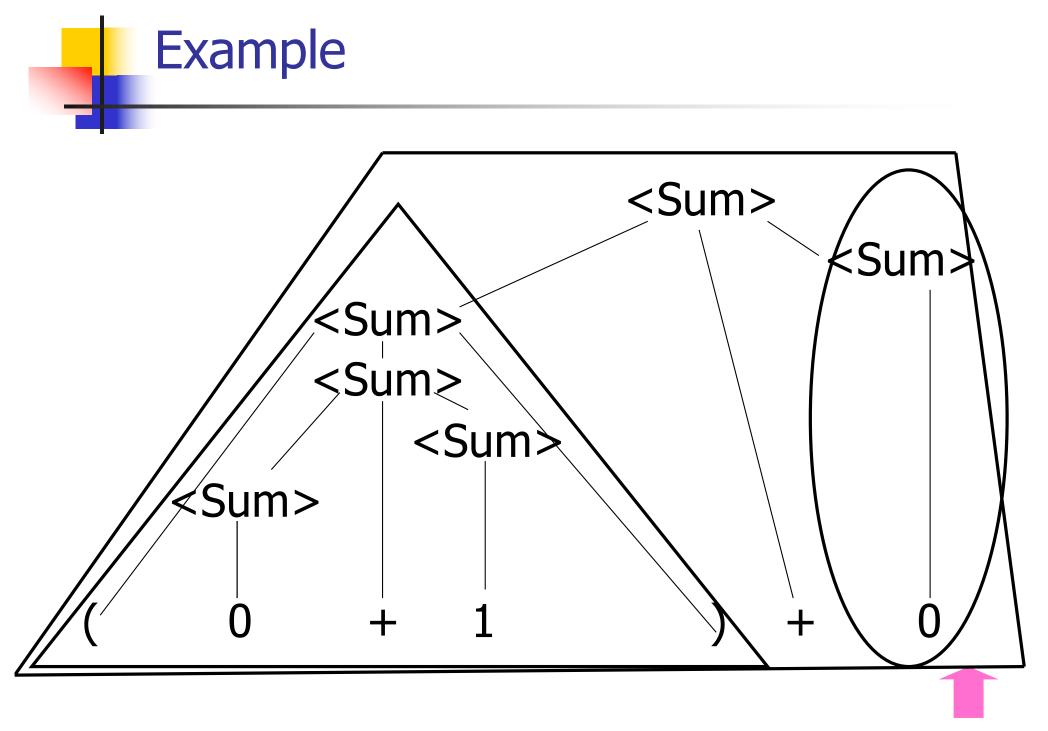


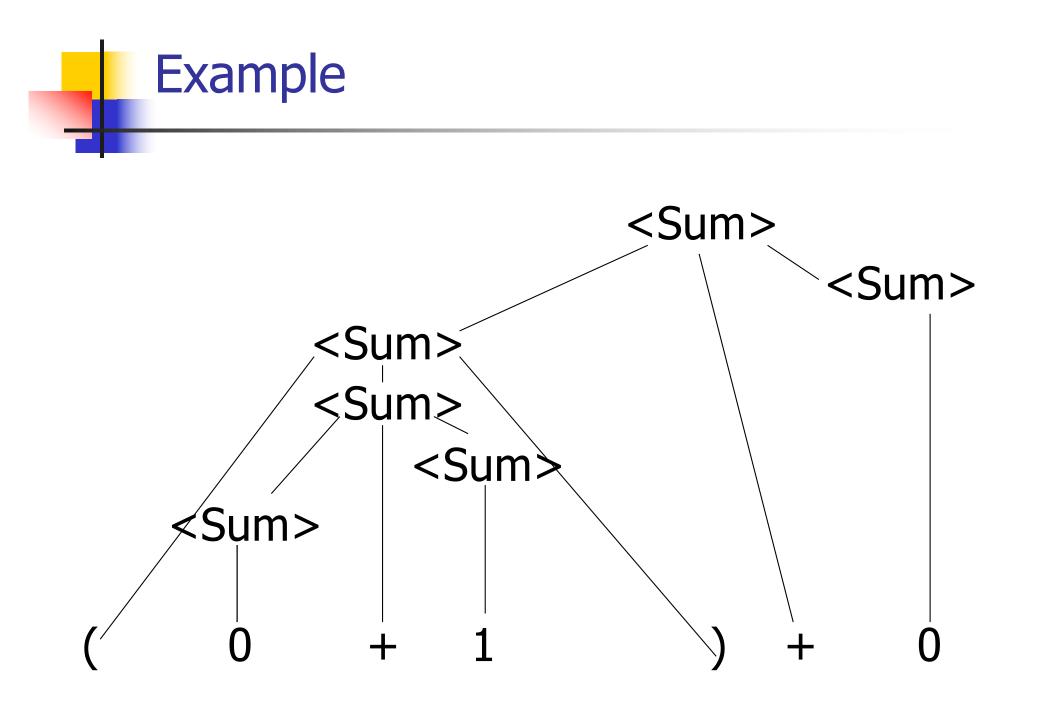












LR Parsing Tables

 Build a pair of tables, Action and Goto, from the grammar

- This is the hardest part, we omit here
- Rows labeled by states
- For Action, columns labeled by terminals and "end-of-tokens" marker
 - (more generally strings of terminals of fixed length)
- For Goto, columns labeled by nonterminals

Action and Goto Tables

- Given a state and the next input, Action table says either
 - shift and go to state n, or
 - reduce by production k (explained in a bit)
 - accept or error
- Given a state and a non-terminal, Goto table says
 - go to state *m*

- Based on push-down automata
- Uses states and transitions (as recorded in Action and Goto tables)
- Uses a stack containing states, terminals and non-terminals

- 0. Insure token stream ends in special "endof-tokens" symbol
- 1. Start in state 1 with an empty stack
- 2. Push **state**(1) onto stack
- → 3. Look at next *i* tokens from token stream (*toks*) (don't remove yet)
 - If top symbol on stack is state(n), look
 up action in Action table at (n, toks)

5. If action = **shift** *m*,

- a) Remove the top token from token stream and push it onto the stack
- b) Push **state**(*m*) onto stack
- c) Go to step 3

- 6. If action = **reduce** *k* where production *k* is E ::= u
 - a) Remove 2 * length(u) symbols from stack (u and all the interleaved states)
 - b) If new top symbol on stack is state(m), look up new state p in Goto(m,E)
 - c) Push E onto the stack, then push state(p) onto the stack

d) Go to step 3

7. If action = **accept**

Stop parsing, return success

8. If action = **error**,

Stop parsing, return failure

Adding Synthesized Attributes

- Add to each reduce a rule for calculating the new synthesized attribute from the component attributes
- Add to each non-terminal pushed onto the stack, the attribute calculated for it
- When performing a reduce,
 - gather the recorded attributes from each nonterminal popped from stack
 - Compute new attribute for non-terminal pushed onto stack

Shift-Reduce Conflicts

- Problem: can't decide whether the action for a state and input character should be shift or reduce
- Caused by ambiguity in grammar
- Usually caused by lack of associativity or precedence information in grammar

Example: <Sum> = 0 | 1 | (<Sum>) | <Sum> + <Sum>

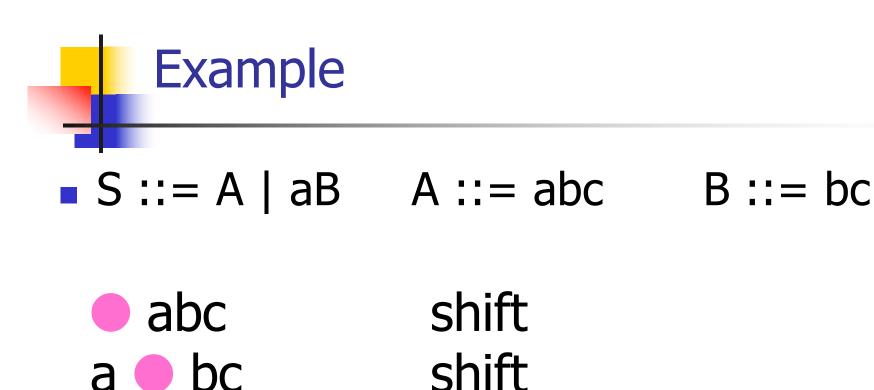
• 0 + 1 + 0 shift -> 0 + 1 + 0 reduce -> <Sum> + 1 + 0 shift -> <Sum> + 0 + 1 + 0 shift -> <Sum> + 0 + 1 + 0 reduce -> <Sum> + 0 + 0

Example - cont

- Problem: shift or reduce?
- You can shift-shift-reduce-reduce or reduce-shift-shift-reduce
- Shift first right associativeReduce first- left associative

Reduce - Reduce Conflicts

- Problem: can't decide between two different rules to reduce by
- Again caused by ambiguity in grammar
- Symptom: RHS of one production suffix of another
- Requires examining grammar and rewriting it
- Harder to solve than shift-reduce errors



Problem: reduce by B ::= bc then by S ::= aB, or by A::= abc then S::A?

shift

ab 🔵 c

abc 🛑