

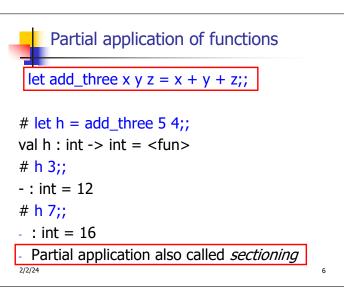
- Let $\rho_{\text{add_three}}$ be the environment before the declaration
- Remember:

let add_three =

fun x -> (fun y -> (fun z -> x + y + z));;

Value: $\langle x \rangle$ (fun z \rangle x + y + z), $\rho_{add three}$

2/2/24



Functions as arguments

val h : int -> int = $\langle fun \rangle$

h 3;;

h 7;;

2/2/24

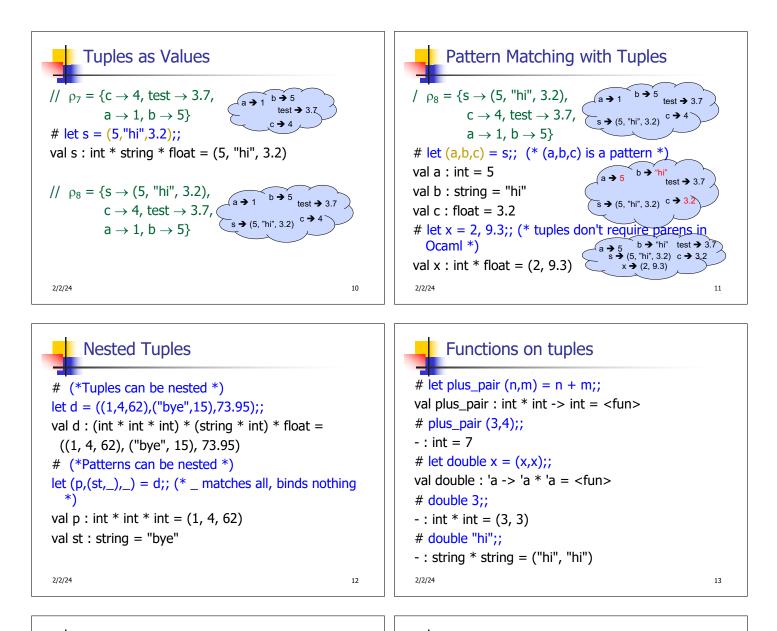
4

-: int = 12

-: int = 16

let thrice f x = f (f (f x));; val thrice : ('a -> 'a) -> ('a -> 'a) = <fun> # let g = thrice plus_two;; val g : int -> int = <fun> # g 4;; - : int = 10 # thrice (fun s -> "Hi! " ^ s) "Good-bye!";; - : string = "Hi! Hi! Hi! Good-bye!"

5



Curried vs Uncurried

Recall
val add_three : int -> int -> int -> int = <fun>
How does it differ from
let add_triple (u,v,w) = u + v + w;;
val add_triple : int * int * int -> int = <fun>
add_three is *curried*;

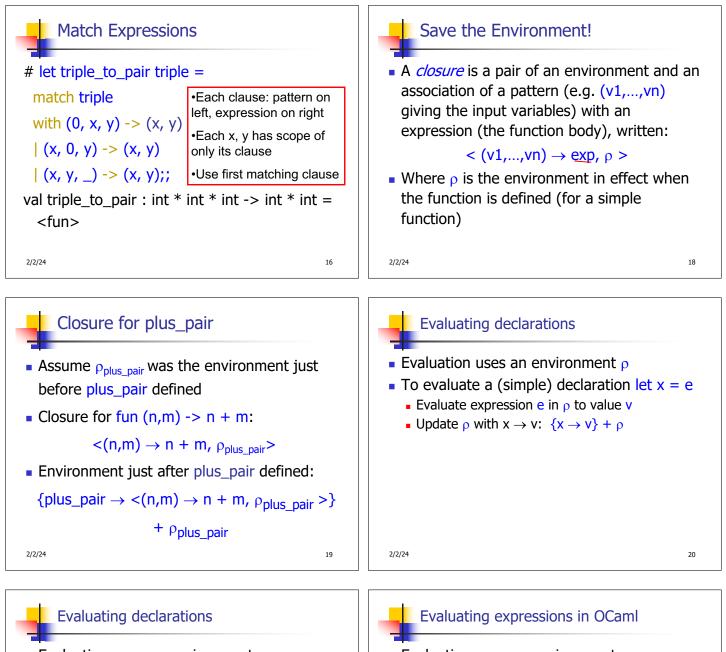
add_triple is uncurried

2/2/24

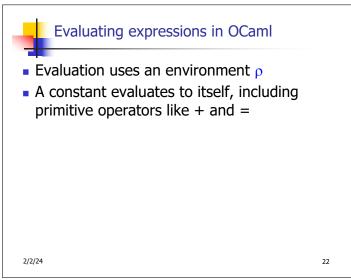
14

Curried vs Uncurried

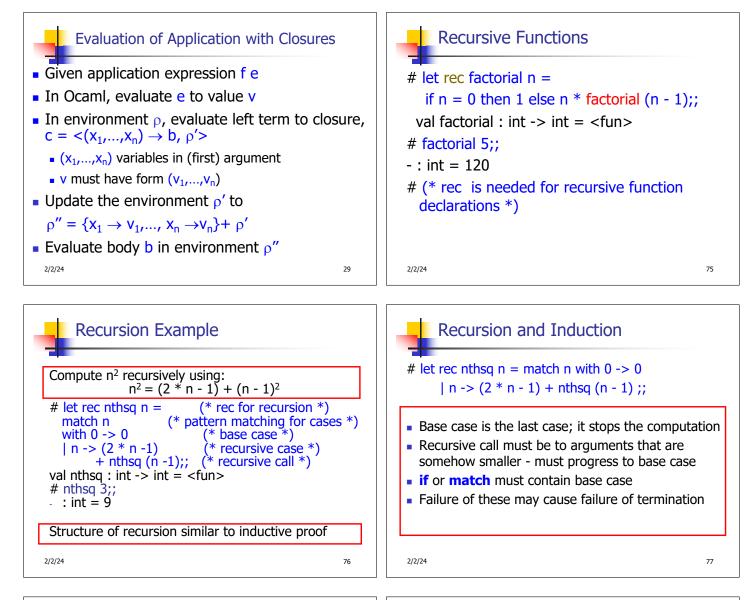
add_triple (6,3,2);; - : int = 11 # add_triple 5 4;; Characters 0-10: add_triple 5 4;; $\land\land\land\land\land\land\land\land\land\land\land$ This function is applied to too many arguments, maybe you forgot a `;' # fun x -> add_triple (5,4,x);; : int -> int = <fun>



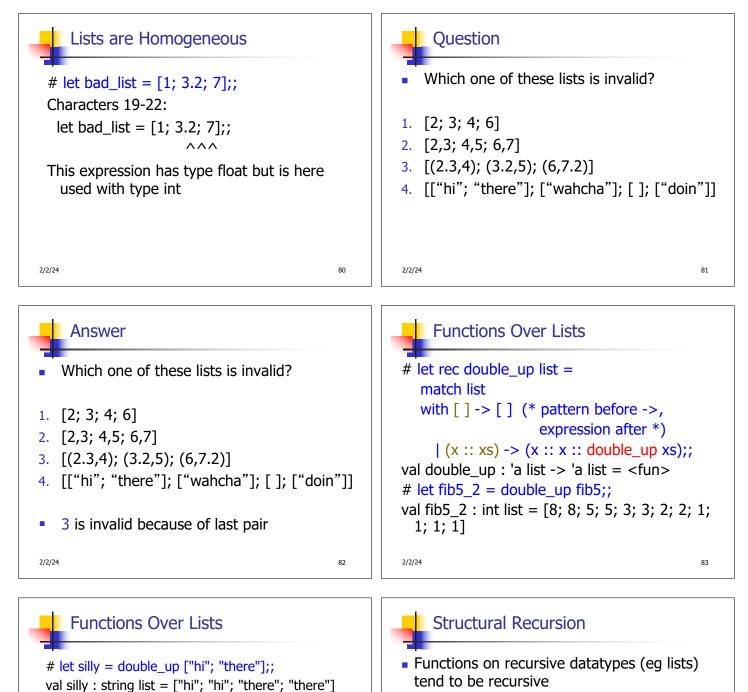
- Evaluation uses an environment p
- To evaluate a (simple) declaration let x = e
 - Evaluate expression e in ρ to value v
 - Update ρ with x v: $\{x \rightarrow v\} + \rho$
- Update: $\rho_1 + \rho_2$ has all the bindings in ρ_1 and all those in ρ_2 that are not rebound in ρ_1 $\{x \rightarrow 2, y \rightarrow 3, a \rightarrow \text{``hi''}\} + \{y \rightarrow 100, b \rightarrow 6\}$ = $\{x \rightarrow 2, y \rightarrow 3, a \rightarrow \text{``hi''}, b \rightarrow 6\}$











- Recursion over recursive datatypes generally by structural recursion
 - Recursive calls made to components of structure of the same recursive type
 - Base cases of recursive types stop the recursion of the function

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2/2/24
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84

let rec poor_rev list =

| (x::xs) -> poor_rev xs @ [x];;

val poor_rev : 'a list -> 'a list = <fun>

- : string list = ["there"; "there"; "hi"; "hi"]

match list

with [] -> []

poor_rev silly;;

2/2/24





