Programming Languages and Compilers (CS 421)

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https://courses.engr.illinois.edu/cs421/fa2017/CS421A

Based on slides by Elsa Gunter, which were inspired by earlier slides by Mattox Beckman, Vikram Adve, and Gul Agha

Data type in Ocaml: lists

- Frequently used lists in recursive program
- Matched over two structural cases
 - [] the empty list
 - (x :: xs) a non-empty list
- Covers all possible lists
- type 'a list = [] | (::) of 'a * 'a list
 - Not quite legitimate declaration because of special syntax

Variants - Syntax (slightly simplified)

- type name = C_1 [of ty_1] ... | C_n [of ty_n]
- Introduce a type called name
- (fun x -> C_i x) : ty_i -> name
- C_i is called a *constructor*; if the optional type argument is omitted, it is called a *constant*
- Constructors are the basis of almost all pattern matching

Enumeration Types as Variants

An enumeration type is a collection of distinct values



In C and Ocaml they have an order structure; order by order of input

Enumeration Types as Variants

```
# type weekday = Monday | Tuesday | Wednesday
  | Thursday | Friday | Saturday | Sunday;;
type weekday =
  Monday
 | Tuesday
 | Wednesday
 | Thursday
 | Friday
 | Saturday
 | Sunday
```

Functions over Enumerations

let day after day = match day with Monday -> Tuesday Tuesday -> Wednesday Wednesday -> Thursday Thursday -> Friday Friday -> Saturday Saturday -> Sunday Sunday -> Monday;; val day after : weekday -> weekday = <fun>

Functions over Enumerations

Write a function days_later n day that computes a day which is n days away from the day. Note that n can be greater than 7 (more than one week) and also negative (meaning a day before

let rec days later n day = match n with 0 -> day -> if n > 0 then day_after (days_later (n - 1) day) else days_later (n + 7) day;; val days later : int -> weekday -> weekday=<fun> 9/27/2018 7

Functions over Enumerations

- # days_later 2 Tuesday;;
- : weekday = Thursday
- # days_later (-1) Wednesday;;
- : weekday = Tuesday
- # days_later (-4) Monday;;
- : weekday = Thursday

Problem:

type weekday = Monday | Tuesday | Wednesday | Thursday | Friday | Saturday | Sunday;;
Write function is_weekend : weekday -> bool
let is_weekend day =

Problem:

type weekday = Monday | Tuesday | Wednesday | Thursday | Friday | Saturday | Sunday;; Write function is weekend : weekday -> bool let is weekend day = match day with Saturday -> true | Sunday -> true

Example Enumeration Types

type mon_op = HdOp | TIOp | FstOp | SndOp

Disjoint Union Types

Disjoint union of types, with some possibly occurring more than once



We can also add in some new singleton elements

Disjoint Union Types

```
type id = DriversLicense of int |
 SocialSecurity of int | Name of string
# let check id id =
   match id with
     DriversLicense num ->
      not (List.mem num [13570; 99999])
   SocialSecurity num -> num < 90000000</pre>
   Name str -> not (str = "John Doe");;
val check id : id -> bool = <fun>
```

Problem

 Create a type to represent the currencies for US, UK, Europe and Japan

Hint: Dollar, Pound, Euro, Yen

Problem

- Create a type to represent the currencies for US, UK, Europe and Japan
- type currency =
 - Dollar of int
 - | Pound of int
 - | Euro of int
 - Yen of int

Example Disjoint Union Type

type const = **BoolConst of bool** | IntConst of int | FloatConst of float StringConst of string | NilConst | UnitConst

Example Disjoint Union Type

How to represent 7 as a const?Answer: IntConst 7

Polymorphism in Variants

The type 'a option gives us something to represent non-existence or failure

type 'a option = Some of 'a | None;;
type 'a option = Some of 'a | None

Used to encode partial functions
Often can replace the raising of an exception

Functions producing option

type 'a option =
 Some of 'a
 None;;

- # first (fun x -> x > 3) [1;3;4;2;5];;
- : int option = Some 4
- # first (fun x -> x > 5) [1;3;4;2;5];;
- : int option = None

Functions over option

type 'a option =
 Some of 'a
 None;;

let result_ok r =
 match r with None -> false
 Some _ -> true;;
val result_ok : 'a option -> bool = <fun>

result_ok (first (fun x -> x > 3) [1;3;4;2;5]);;

- : bool = true

result_ok (first (fun x -> x > 5) [1;3;4;2;5]);;

- : bool = false

Problem

type 'a option =
 Some of 'a
 None;;

Write a hd and tl on lists that doesn't raise an exception and works at all types of lists.

Problem

type 'a option =
 Some of 'a
 None;;

- Write a hd and tl on lists that doesn't raise an exception and works at all types of lists.
- let hd list = match list with [] -> None (x::xs) -> Some x let tl list = match list with [] -> None (x::xs) -> Some xs 9/27/2018

Mapping over Variants

```
# let optionMap f opt =
    match opt with
    None -> None
    | Some x -> Some (f x);;
val optionMap : ('a -> 'b) -> 'a option -> 'b
    option = <fun>
```

optionMap
 (fun x -> x - 2)
 (first (fun x -> x > 3) [1;3;4;2;5]);;
- : int option = Some 2

Folding over Variants

let optionFold someFun noneVal opt =
 match opt with
 None -> noneVal
 Some x -> someFun x;;
val optionFold : ('a -> 'b) -> 'b -> 'a option
 -> 'b = <fun>

let optionMap f opt =
 optionFold (fun x -> Some (f x)) None opt;;
val optionMap : ('a -> 'b) -> 'a option -> 'b
 option = <fun>

Recursive Types

The type being defined may be a component of itself



- # type int_Bin_Tree =
 Leaf of int
 Node of (int_Bin_Tree * int_Bin_Tree);;
- type int_Bin_Tree = Leaf of int | Node of (int_Bin_Tree * int_Bin_Tree)

Recursive Data Type Values

let bin_tree =
Node(Node(Leaf 3, Leaf 6),Leaf (-7));;

val bin_tree : int_Bin_Tree = Node (Node (Leaf 3, Leaf 6), Leaf (-7)) **Recursive Data Type Values**



```
# type exp =
     VarExp of string
   ConstExp of const
   MonOpAppExp of mon op * exp
     BinOpAppExp of bin op * exp * exp
     IfExp of exp* exp * exp
   AppExp of exp * exp
FunExp of string * exp
```

How to represent 6 as an exp?

How to represent 6 as an exp?Answer: ConstExp (IntConst 6)

How to represent (6, 3) as an exp?

How to represent (6, 3) as an exp?
BinOpAppExp (CommaOp,

ConstExp (IntConst 6), ConstExp (IntConst 3)

type bin op = IntPlusOp | IntMinusOp | EqOp | CommaOp | ConsOp | ... # type const = BoolConst of bool | IntConst of int | \dots # type exp = VarExp of string | ConstExp of const | BinOpAppExp of bin_op * exp * exp | ... How to represent [(6, 3)] as an exp? BinOpAppExp (ConsOp, BinOpAppExp (CommaOp, ConstExp (IntConst 6), ConstExp (IntConst 3)),

ConstExp NilConst))));;

Recursive Functions

```
# let rec first leaf value tree =
    match tree
       with (Leaf n) -> n
    Node (left tree, right tree) ->
                first leaf value left tree;;
val first leaf value : int Bin Tree -> int
  = \langle fun \rangle
# let left = first leaf value bin tree;;
val left : int = 3
```

Problem

type int_Bin_Tree =
 Leaf of int

- Node of (int_Bin_Tree * int_Bin_Tree);;
- Write sum_tree : int_Bin_Tree -> int
- Adds all ints in tree
- let rec sum_tree t =
- type int_Bin_Tree =Leaf of int
- Node of (int_Bin_Tree * int_Bin_Tree);;
- Write sum_tree : int_Bin_Tree -> int
- Adds all ints in tree
- let rec sum_tree t =
 - match t with Leaf n -> n
 - Node(tl,t2) -> sum_tree tl + sum_tree t2

Recursion over Recursive Data Types

How to count the number of variables in an exp?

Recursion over Recursive Data Types

- How to count the number of variables in an exp?

```
# let rec varCnt exp =
  match exp with
    VarExp x ->
    ConstExp c ->
    BinOpAppExp (b, e1, e2) ->
    FunExp (x,e) ->
    AppExp (e1, e2) ->
```

Recursion over Recursive Data Types

- # type exp = VarExp of string | ConstExp of const | BinOpAppExp of bin_op * exp * exp | FunExp of string * exp | AppExp of exp * exp
- How to count the number of variables in an exp?

```
# let rec varCnt exp =
  match exp with
    VarExp x -> 1
    ConstExp c -> 0
    BinOpAppExp (b, e1, e2) -> varCnt e1 +varCnt e2
    FunExp (x,e) -> 1 + varCnt e
    AppExp (e1, e2) -> varCnt e1 + varCnt e2
    40
```

Mapping over Recursive Types

let rec ibtreeMap f tree =
 match tree with
 (Leaf n) ->
 | Node (left_tree, right_tree) ->

Mapping over Recursive Types

```
# let rec ibtreeMap f tree =
    match tree with
      (Leaf n) -> Leaf (f n)
    Node (left tree, right_tree) ->
           Node (ibtreeMap f left_tree,
                 IbtreeMap f right tree);;
val ibtreeMap : (int -> int) -> int Bin Tree ->
 int Bin Tree = <fun>
```

Mapping over Recursive Types

let bin_tree =
Node(Node(Leaf 3, Leaf 6),Leaf (-7));;

ibtreeMap ((+) 2) bin_tree;;

- : int_Bin_Tree = Node (Node (Leaf 5, Leaf 8), Leaf (-5))

Summing up Elements of a Tree

let rec tree_sum_0 tree =
 match tree with
 Leaf n ->

Node (left_tree, right_tree) ->

Folding over Recursive Types

val ibtreeFoldRight : (int -> 'a) -> ('a -> 'a -> 'a) -> int_Bin_Tre -> 'a = <fun>

Folding over Recursive Types

let rec ibtreeFoldRight leafFun nodeFun tree =
 match tree with
 Leaf n -> leafFun n
 Node (left_tree, right_tree) ->
 nodeFun
 (ibtreeFoldRight leafFun nodeFun left_tree)
 (ibtreeFoldRight leafFun nodeFun right_tree);

val ibtreeFoldRight : (int -> 'a) -> ('a -> 'a -> 'a) -> int_Bin_Tre -> 'a = <fun>

Folding over Recursive Types

let tree_sum =
 ibtreeFoldRight (fun x -> x) (+);;
val tree_sum : int_Bin_Tree -> int = <fun>

- # tree_sum bin_tree;;
- -: int = 2

Mutually Recursive Types

```
# type 'a tree =
         TreeLeaf of 'a
       TreeNode of 'a treeList
and
   'a treeList =
         Last of 'a tree
       More of ('a tree * 'a treeList);;
type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList
```

and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList)

let tree =
 TreeNode
 (More (TreeLeaf 5,
 (More (TreeNode
 (More (TreeLeaf 3,
 Last (TreeLeaf 2))),
 Last (TreeLeaf 7))));;

val tree : int tree =

TreeNode

(More

(TreeLeaf 5,

More

(TreeNode (More (TreeLeaf 3, Last (TreeLeaf 2))), Last (TreeLeaf 7))))



A more conventional picture



Mutually Recursive Functions

```
# let rec fringe tree =
    match tree with
       (TreeLeaf x) \rightarrow [x]
  (TreeNode list) -> list_fringe list
and list fringe tree list =
    match tree list with
       (Last tree) -> fringe tree
  (More (tree,list)) ->
       (fringe tree) @ (list_fringe list);;
```

val fringe : 'a tree -> 'a list = <fun>
val list_fringe : 'a treeList -> 'a list = <fun>
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Mutually Recursive Functions

fringe tree;;

- : int list = [5; 3; 2; 7]

type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);; Define tree_size

type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);; Define tree_size let rec tree_size t = match t with TreeLeaf _ -> | TreeNode ts ->

type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);; Define tree_size let rec tree_size t = match t with TreeLeaf _ -> I | TreeNode ts -> treeList_size ts

type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);; Define tree size and treeList size let rec tree size t =match t with TreeLeaf -> I | TreeNode ts -> treeList size ts and treeList size ts =

type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);; Define tree size and treeList size let rec tree size t = match t with TreeLeaf -> I | TreeNode ts -> treeList size ts and treeList size ts = match ts with Last t \rightarrow | More t ts' ->

type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);; Define tree size and treeList size let rec tree size t = match t with TreeLeaf -> I | TreeNode ts -> treeList size ts and treeList size ts = match ts with Last t -> tree_size t | More t ts' -> tree size t + treeList size ts'

type 'a tree = TreeLeaf of 'a | TreeNode of 'a treeList and 'a treeList = Last of 'a tree | More of ('a tree * 'a treeList);; Define tree size and treeList size let rec tree size t = match t with TreeLeaf -> I | TreeNode ts -> treeList size ts and treeList size ts = match ts with Last t -> tree_size t More t ts' -> tree size t + treeList size ts' **Nested Recursive Types**

- # type intlist =
 Nil | Cons of (int * intlist)
- # type 'a mylist =
 Nil | Cons of ('a * 'a mylist)

If only we had control over extra syntax: " type 'a list = [] | (::) of 'a * 'a list "

Nested Recursive Types

type 'a labeled_tree =
 TreeNode of ('a * 'a labeled_tree list);;

```
type 'a labeled_tree = TreeNode of ('a * 'a
labeled_tree list)
```

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Nested Recursive Type Values

Nested Recursive Type Values



Nested Recursive Type Values



Mutually Recursive Functions

let rec flatten_tree labtree =
 match labtree with
 TreeNode (x,treelist) ->
 x::flatten tree list treelist

and flatten_tree_list treelist =
 match treelist with
 [] -> []
 labtree::labtrees ->
 flatten_tree labtree
 @ (flatten_tree_list labtrees);;

Mutually Recursive Functions

- # flatten_tree ltree;;
- : int list = [5; 3; 2; 1; 7; 5]

Nested recursive types lead to mutually recursive functions

Records

- Records serve the same programming purpose as tuples
- Provide better documentation, more readable code
- Allow components to be accessed by label instead of position
 - Labels (aka *field names)* must be **unique**
 - Fields accessed by suffix dot notation

Record Types

 Record types must be declared before they can be used in OCaml

type person = {name : string;
 ss : (int * int * int);
 age : int};;
type person = { name : string; ss :
 int * int * int; age : int; }
 person is the type being introduced

name, ss and age are the labels, or fields

Record Values

Records built with labels; order does not matter

let teacher = {name = "Elsa L. Gunter"; age = 102; ss = (119,73,6244)};;

```
val teacher : person =
  {name = "Elsa L. Gunter"; ss = (119, 73,
  6244); age = 102}
```

teacher.name;;

- : string = "Elsa L. Gunter"

Record Pattern Matching

val elsa : string = "Elsa L. Gunter"
val age : int = 102
val s3 : int = 6244
Record Field Access

let soc_sec = teacher.ss;;

```
val soc_sec : int * int * int = (119, 73,
6244)
```

Record Values

```
# let student = {
    ss=(325,40,1276);
    name="Usain Bolt";
    age=22};;
val student : person =
    {name = "Usain Bolt"; ss = (325, 40,
    1276); age = 22}
```

student = teacher;;

- : bool = false

New Records from Old

let birthday person =
 {person with age = person.age + 1};;
val birthday : person -> person = <fun>

- # birthday teacher;;
- : person = {name = "Elsa L. Gunter"; ss =
 (119, 73, 6244); age = 103}

New Records from Old

- # let new_id name soc_sec person =
 {person with name = name; ss = soc_sec};;

new_id "Lionel Messi" (523,04,6712) student;;
- : person = {name = "Lionel Messi";
- ss = (523, 4, 6712); age = 22}