

## Programming Languages and Compilers (CS 421)

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<https://courses.engr.illinois.edu/cs421/fa2017/CS421A>

Based in part on slides by Mattox Beckman, as updated by Vikram Adve, Gul Agha, and Elsa Gunter

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## Contact Information – Sasa Misailovic

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## Course Website

- <https://courses.engr.illinois.edu/cs421/fa2018/CS421A>
- Main page - summary of news items
- Policy - rules governing course
- Lectures - syllabus and slides
- MPs - information about assignments
- Exams
- Unit Projects - for 4 credit students
- Resources - tools and helpful info
- FAQ

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## Some Course References

- No required textbook
- Some suggested references



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## Course Grading

- Assignments 20%
  - About 12 Web Assignments (WA) (~7%)
  - About 6 MPs (in Ocaml) (~7%)
  - About 5 Labs (~6%)
  - All WAs and MPs Submitted through **PrairieLearn**
  - Late submission penalty: 20%
  - Labs in Computer-Based Testing Center (Grainger)
  - Self-scheduled over a three day period
  - No extensions beyond the three day period
  - Fall back: Labs become MPs

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## Course Grading

- 2 Midterms - 20% each
  - Labs in Computer-Based Testing Center (Grainger)
  - Self-scheduled over a three day period
  - No extensions beyond the three day period
  - Dates: **Oct 2-4 (Midterm 1) Nov 6-8 (Midterm 2)**
  - Fall back: In class backup dates – Oct 9, Nov 13
  - **DO NOT MISS EXAM DATES!**
- Final 40% - Dec 19, 8:00am – 11:00am (nominally)
- Will likely use CBTF for Final (3 day window)
- Percentages are approximate

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## Course Assignments – WA & MP

- You may discuss assignments and their solutions with others
- You may work in groups, but you must **list members with whom you worked** if you share solutions or solution outlines
- **Each student must write up and turn in their own solution separately**
- You may look at examples from class and other similar examples from any source – **cite appropriately**
  - Note: University policy on plagiarism still holds - cite your sources if you are not the sole author of your solution

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## Course Objectives

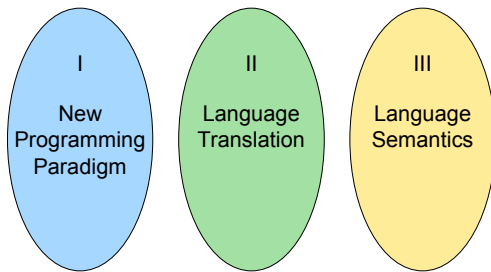
- New programming paradigm
  - Functional programming
  - Environments and Closures
  - Patterns of Recursion
  - Continuation Passing Style
- Phases of an interpreter / compiler
  - Lexing and parsing
  - Type systems
  - Interpretation
- Programming Language Semantics
  - Lambda Calculus
  - Operational Semantics
  - Axiomatic Semantics

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## Programming Languages & Compilers

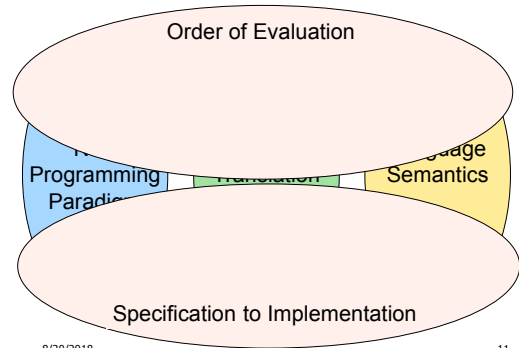
Three Main Topics of the Course



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## Programming Languages & Compilers

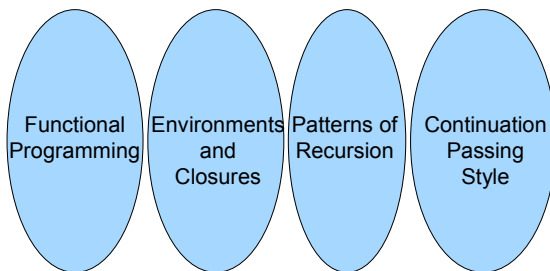


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## Programming Languages & Compilers

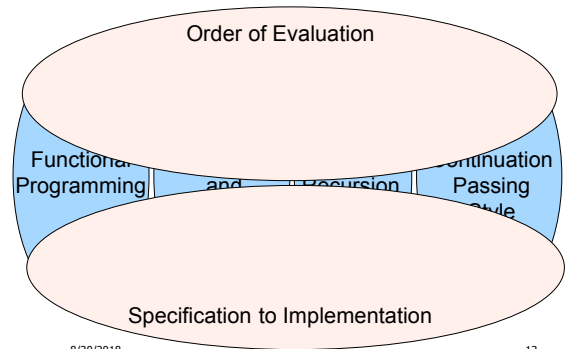
I : New Programming Paradigm



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## Programming Languages & Compilers

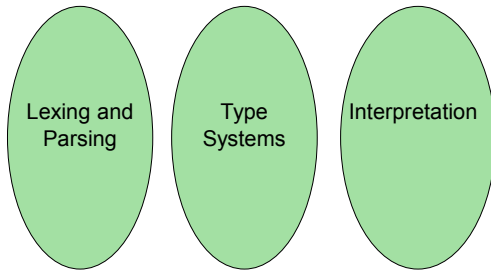


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## Programming Languages & Compilers

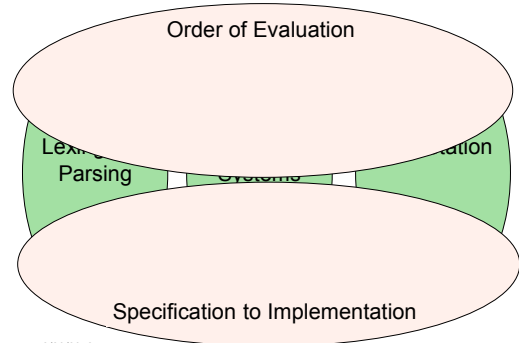
### II : Language Translation



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## Programming Languages & Compilers

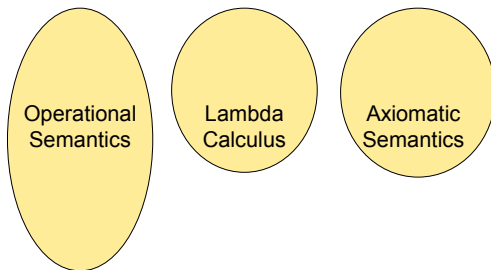


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## Programming Languages & Compilers

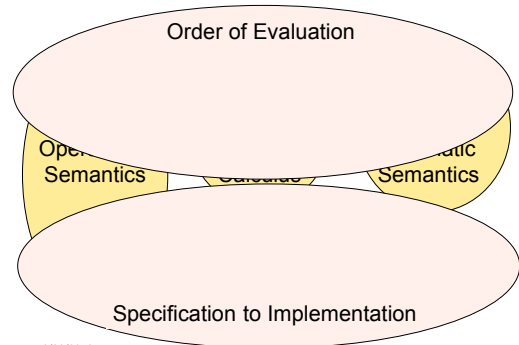
### III : Language Semantics



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## Programming Languages & Compilers



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## OCAML

- Locally:
  - Compiler is on the EWS-linux systems at `/usr/local/bin/ocaml`
  - Be sure to **module load ocaml/2.07.0** in EWS!
- Globally:
  - Main CAML home: <http://ocaml.org>
  - To install OCAML on your computer see: <http://ocaml.org/docs/install.html>
  - Or use one of the online OCAML compilers...

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## References for OCaml

- Supplemental texts (not required):
  - The Objective Caml system release 4.07, by Xavier Leroy, online manual
  - Introduction to the Objective Caml Programming Language, by Jason Hickey
  - Developing Applications With Objective Caml, by Emmanuel Chailloux, Pascal Manoury, and Bruno Pagano, on O'Reilly
    - Available online from course resources

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## Why learn OCAML?

- Many features not clearly in languages you have already learned
- Assumed basis for much research in programming language research
- OCAML is particularly efficient for programming tasks involving languages (eg parsing, compilers, user interfaces)

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## Why Learn OCAML?

- Industrially Relevant: Jane Street trades billions of dollars per day using OCaml programs
- Similar languages: Microsoft F#, SML, Haskell, Scala, Scheme
- Who uses functional programming?
  - Google – MapReduce
  - Microsoft – LinQ
  - Twitter – Scala
  - Bonus: who likes set comprehensions in Python?

```
>>> squares = [x**2 for x in range(10)]
```

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## OCAML Background

- CAML is European descendant of original ML
  - American/British version is SML
  - **O** is for object-oriented extension
- ML stands for **Meta-Language**
- ML family designed for implementing theorem provers (back in 1970s)
  - It was the meta-language for programming the “object” language of the theorem prover
  - Despite obscure original application area, OCAML is a full general-purpose programming language

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## Session in OCAML

```
% ocaml
Objective Caml version 4.07
# _
# (* Read-eval-print loop; expressions and declarations *)
  2 + 3;; (* Expression *)
- : int = 5
# 3 < 2;;
- : bool = false
```

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## No Overloading for Basic Arithmetic Operations

```
# 15 * 2;;
- : int = 30
# 1.35 + 0.23;; (* Wrong type of addition *)
Characters 0-4:
  1.35 + 0.23;; (* Wrong type of addition *)
^^^^
Error: This expression has type float but an expression
was expected of type int
# 1.35 +. 0.23;;
- : float = 1.58
```

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## No Implicit Coercion

```
# 1.0 * 2;; (* No Implicit Coercion *)
Characters 0-3:
  1.0 * 2;;
^^^
Error: This expression has type float but an expression
was expected of type int

# 1.0 *. 2;; (* No Implicit Coercion *)
Characters 7-8:
  1.0 *. 2;;
^^
Error: This expression has type int but an expression was
expected of type float
```

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## Sequencing Expressions

```
# "Hi there"; (* has type string *)
- : string = "Hi there"
# print_string "Hello world\n"; (* has type unit *)
Hello world
- : unit = ()
# (print_string "Bye\n"; 25); (* Sequence of exp *)
Bye
- : int = 25
```

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## Declarations; Sequencing of Declarations

```
# let x = 2 + 3;; (* declaration *)
val x : int = 5
# let test = 3 < 2;;
val test : bool = false
# let a = 1 let b = a + 4;; (* Sequence of dec *)
val a : int = 1
val b : int = 5
```

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## Environments

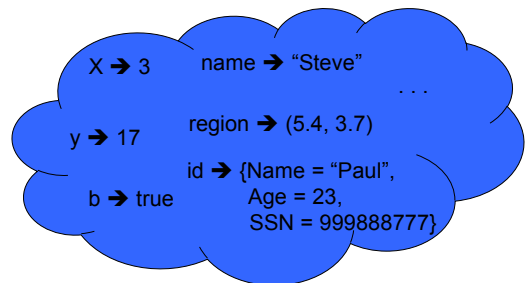
- *Environments* record what value is associated with a given identifier
- Central to the semantics and implementation of a language
- Notation
$$\rho = \{\text{name}_1 \rightarrow \text{value}_1, \text{name}_2 \rightarrow \text{value}_2, \dots\}$$

Using set notation, but describes a partial function
- Implementation: Often stored as list, or stack
  - To find value start from left and take first match

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## Environments



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## Global Variable Creation

```
# 2 + 3;; (* Expression *)
// doesn't affect the environment
# let test = 3 < 2;; (* Declaration *)
val test : bool = false
//  $\rho_1 = \{\text{test} \rightarrow \text{false}\}$ 
# let a = 1 let b = a + 4;; (* Seq of dec *)
//  $\rho_2 = \{\text{b} \rightarrow 5, \text{a} \rightarrow 1, \text{test} \rightarrow \text{false}\}$ 
```

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## New Bindings Hide Old

```
//  $\rho_2 = \{\text{b} \rightarrow 5, \text{a} \rightarrow 1, \text{test} \rightarrow \text{false}\}$ 
let test = 3.7;;
```

- What is the environment after this declaration?

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## New Bindings Hide Old

```
// ρ2 = {b → 5, a → 1, test → false}
let test = 3.7;
```

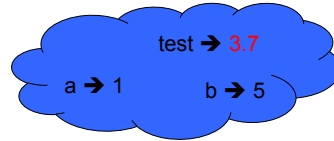
■ What is the environment after this declaration?

```
// ρ3 = {test → 3.7, a → 1, b → 5}
```

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## Environments

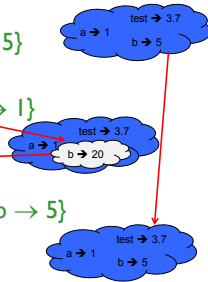


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## Local Variable Creation

```
// ρ3 = {test → 3.7, a → 1, b → 5}
# let b = 5 * 4
// ρ4 = {b → 20, test → 3.7, a → 1}
  in 2 * b;;
- : int = 40
// ρ5 = ρ3 = {test → 3.7, a → 1, b → 5}
# b;;
- : int = 5
```



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## Local let binding

```
// ρ5 = {test → 3.7, a → 1, b → 5}
# let c =
  let b = a + a
  in b * b;;
# b;;
```

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## Local let binding

```
// ρ5 = {test → 3.7, a → 1, b → 5}
# let c =
  let b = a + a
  in b * b;;
val c : int = 4
// ρ7 = {c → 4, test → 3.7, a → 1, b → 5}
# b;;
- : int = 5
```

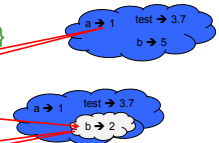


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## Local let binding

```
// ρ5 = {test → 3.7, a → 1, b → 5}
# let c =
  let b = a + a
  in b * b;;
val c : int = 4
// ρ7 = {c → 4, test → 3.7, a → 1, b → 5}
# b;;
- : int = 5
```

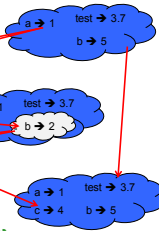


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## Local let binding

```
// ρ5 = {test → 3.7, a → 1, b → 5}
# let c =
  let b = a * a
// ρ6 = {b → 2} + ρ5
// = {b → 2, test → 3.7, a → 1}
  in b * b;;
val c : int = 4
// ρ7 = {c → 4, test → 3.7, a → 1, b → 5}
# b;;
- : int = 5
```



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## Booleans (aka Truth Values)

```
# true;;
- : bool = true

# false;;
- : bool = false

// ρ7 = {c → 4, test → 3.7, a → 1, b → 5}
# if b > a then 25 else 0;;
- : int = 25
```

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## Booleans and Short-Circuit Evaluation

```
# 3 > 1 && 4 > 6;;
- : bool = false

# 3 > 1 || 4 > 6;;
- : bool = true

# not (4 > 6);;
- : bool = true

# (print_string "Hi\n"; 3 > 1) || 4 > 6;;
Hi
- : bool = true

# 3 > 1 || (print_string "Bye\n"; 4 > 6);;
- : bool = true
```

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## Tuples as Values

```
// ρ0 = {c → 4, a → 1, b → 5}
# let s = (5, "hi", 3.2);;
val s : int * string * float = (5, "hi", 3.2)

// ρ = {s → (5, "hi", 3.2), c → 4, a → 1, b → 5}
```

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## Pattern Matching with Tuples

```
// ρ = {s → (5, "hi", 3.2), a → 1, b → 5, c → 4}

# let (a,b,c) = s;;      (* (a,b,c) is a pattern *)
val a : int = 5
val b : string = "hi"
val c : float = 3.2

# let (a, _, _) = s;;
val a : int = 5

# let x = 2, 9.3;;      (* tuples don't require parens in Ocaml *)
val x : int * float = (2, 9.3)
```

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## Nested Tuples

```
# (*Tuples can be nested *)
# let d = ((1,4,62), ("bye", 15), 73.95);;
val d : (int * int * int) * (string * int) * float =
  ((1, 4, 62), ("bye", 15), 73.95)

# (*Patterns can be nested *)
# let (p, (st, _) , _) = d;;
      (* _ matches all, binds nothing *)
val p : int * int * int = (1, 4, 62)
val st : string = "bye"
```

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## Functions

```
# let plus_two n = n + 2;;  
val plus_two : int -> int = <fun>
```

```
# plus_two 17;;  
- : int = 19
```

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## Functions

```
let plus_two n = n + 2;;  
plus_two 17;;  
- : int = 19
```

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## Nameless Functions (aka Lambda Terms)

```
fun n -> n + 2;;  
(fun n -> n + 2) 17;;  
- : int = 19
```



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## Functions

```
# let plus_two n = n + 2;;  
val plus_two : int -> int = <fun>  
# plus_two 17;;  
- : int = 19
```

```
# let plus_two = fun n -> n + 2;;  
val plus_two : int -> int = <fun>  
# plus_two 14;;  
- : int = 16
```

First definition syntactic sugar for second

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## Using a nameless function

```
(* An application *)  
# (fun x -> x * 3) 5;;  
: int = 15
```

```
(* As data *)  
# ((fun y -> y +. 2.0), (fun z -> z * 3));;  
- : (float -> float) * (int -> int) = (<fun>, <fun>)
```

Note: in fun v -> exp(v), scope of variable is only the body exp(v)

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## Values fixed at declaration time

```
# let x = 12;;  
val x : int = 12  
# let plus_x y = y + x;;  
val plus_x : int -> int = <fun>  
# plus_x 3;;
```

What is the result?

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### Values fixed at declaration time

```
# let x = 12;;  
val x : int = 12  
# let plus_x y = y + x;;  
val plus_x : int -> int = <fun>  
# plus_x 3;;  
- : int = 15
```

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### Values fixed at declaration time

```
# let x = 7;; (* New declaration, not an update *)  
val x : int = 7  
  
# plus_x 3;;
```

What is the result this time?

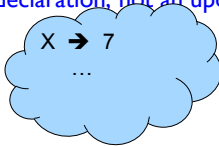
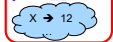
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### Values fixed at declaration time

```
# let x = 7;; (* New declaration, not an update *)  
val x : int = 7
```

```
# plus_x 3;;
```



What is the result this time?

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### Values fixed at declaration time

```
# let x = 7;; (* New declaration, not an update *)  
val x : int = 7  
  
# plus_x 3;;  
- : int = 15
```

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### Question

- Observation: Functions are **first-class values** in this language
- Question: What value does the environment record for a function variable?
- Answer: a **closure**

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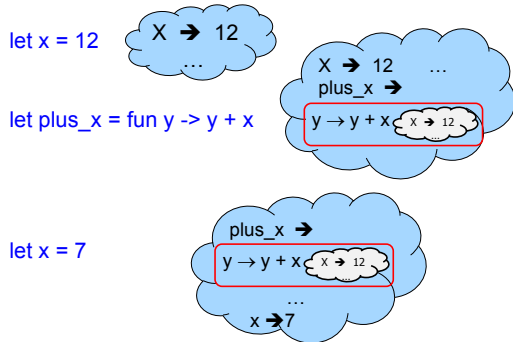
### Save the Environment!

- A **closure** is a pair of an environment and an association of a sequence of variables (the input variables) with an expression (the function body), written:  
$$\langle (v_1, \dots, v_n) \rightarrow \text{exp}, \rho \rangle$$
- Where  $\rho$  is the environment in effect when the function is defined (for a simple function)

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Recall: `let plus_x = fun x => y + x`



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Closure for `plus_x`

- When `plus_x` was defined, had environment:

$\rho_{plus\_x} = \{\dots, x \rightarrow 12, \dots\}$

- Recall: `let plus_x y = y + x`  
is really `let plus_x = fun y -> y + x`

- Closure for `fun y -> y + x`:

$\langle y \rightarrow y + x, \rho_{plus\_x} \rangle$

- Environment just after `plus_x` defined:

$\{plus\_x \rightarrow \langle y \rightarrow y + x, \rho_{plus\_x} \rangle\} + \rho_{plus\_x}$

Like set union!  
(but subtle differences;  
new decl. replaces old)

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Functions with more than one argument

```
# let add_three x y z = x + y + z;;
val add_three : int -> int -> int -> int = <fun>

# let t = add_three 6 3 2;;
val t : int = 11

# let add_three =
  fun x -> (fun y -> (fun z -> x + y + z));;
val add_three : int -> int -> int -> int = <fun>
```

Again, first syntactic sugar for second

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Functions on tuples

```
# let plus_pair (n,m) = n + m;;
val plus_pair : int * int -> int = <fun>

# plus_pair (3,4);;
- : int = 7

# let twice x = (x,x);;
val twice : 'a -> 'a * 'a = <fun>

# twice 3;;
- : int * int = (3, 3)

# twice "hi";;
- : string * string = ("hi", "hi")
```

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Curried vs Uncurried

- Recall
 

```
# let add_three u v w = u + v + w;;
val add_three : int -> int -> int -> int = <fun>
```
- How does it differ from
 

```
# let add_triple (u,v,w) = u + v + w;;
val add_triple : int * int * int -> int = <fun>
```
- `add_three` is **curried**;
- `add_triple` is **uncurried**

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Curried vs Uncurried

```
# add_three 6 3 2;;
- : int = 11

# add_triple (6,3,2);;
- : int = 11

# add_triple 5 4;;
Characters 0-10: add_triple 5 4;;
^^^^^^^^^^^^^

This function is applied to too many arguments,
maybe you forgot a `;'

# fun x -> add_triple (5,4,x);;
: int -> int = <fun>
```

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## Partial application of functions

```
let add_three x y z = x + y + z;;
```

```
# let h = add_three 5 4;;  
val h : int -> int = <fun>
```

```
# h 3;;  
- : int = 12
```

```
# h 7;;  
- : int = 16
```

Partial application also called *sectioning*

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## Match Expressions

```
# let triple_to_pair triple =
```

```
  match triple
```

```
  with (0, x, y) -> (x, y)
```

```
  | (x, 0, y) -> (x, y)
```

```
  | (x, y, _) -> (x, y);;
```

```
val triple_to_pair : int * int * int -> int * int =  
  <fun>
```

- Each clause: pattern on left, expression on right
- Each x, y has scope of only its clause
- Use first matching clause

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