Contact Information – Sasa Misailovic

- Office: 4110 SC
- Office hours:
  - Tuesday, Thursday 12:40pm – 1:30pm
  - Also by appointment
- Email: misailo@illinois.edu
Course TAs

John Lee

Stephen Skeirik
Contact Information - TAs

- Teaching Assistants Office: 0207 SC
- John Lee
  - Email: jlee170@illinois.edu
  - Hours: Tue 9:00am – 9:50am
    Fri 2:00pm – 2:50pm
- Stephen Skeirik
  - Email: skeirik2@illinois.edu
  - Hours: Mon, Thu 10:00am – 10:50am
Course Website

- [https://courses.engr.illinois.edu/cs421/fa2017/CS421A](https://courses.engr.illinois.edu/cs421/fa2017/CS421A)
- Main page - summary of news items
- Policy - rules governing course
- Lectures - syllabus and slides
- MPs - information about assignments
- Exams
- Unit Projects - for 4 credit students
- Resources - tools and helpful info
- FAQ
Some Course References

- No required textbook
- Some suggested references

9/12/17
Some Course References

- No required textbook.
- Pictures of the books on previous slide
- Additional ones for Ocaml given separately
Course Grading

- Assignments 20%
  - About 12 Web Assignments (WA) (~7%)
  - About 6 MPs (in Ocaml) (~7%)
  - About 5 Labs (~6%)
  - All WAs and MPs Submitted by PrairieLearn
  - Late submission penalty: 20%
  - Labs in Computer-Based Testing Center (Grainger)
  - Self-scheduled over a three day period
  - No extensions beyond the three day period
  - Fall back: Labs become MPs
Course Grading

- 2 Midterms - 20% each
  - Labs in Computer-Based Testing Center (Grainger)
  - Self-scheduled over a three day period
  - No extensions beyond the three day period

- Fall back: In class backup dates – **Oct 8, Nov 11**

- **DO NOT MISS EXAM DATES!**

- Final 40% - Dec 18, 8:00am – 11:00am
- May use CBTC for Final
- Percentages are approximate
You may discuss assignments and their solutions with others.

You may work in groups, but you must list members with whom you worked if you share solutions or solution outlines.

Each student must write up and turn in their own solution separately.

You may look at examples from class and other similar examples from any source – cite appropriately.

Note: University policy on plagiarism still holds - cite your sources if you are not the sole author of your solution.
Three Main Topics of the Course

I
New Programming Paradigm

II
Language Translation

III
Language Semantics
Programming Languages & Compilers

I New Programming Paradigm

II Language Translation

III Language Semantics

Order of Evaluation

Specification to Implementation
Functional Programming
Environments and Closures
Patterns of Recursion
Continuation Passing Style
Programming Languages & Compilers

Order of Evaluation

Operational Semantics

Lambda Calculus

Axiomatic Semantics

Specification to Implementation

CS422

CS426
CS477
Course Objectives

- New programming paradigm
  - Functional programming
  - Environments and Closures
  - Patterns of Recursion
  - Continuation Passing Style
- Phases of an interpreter / compiler
  - Lexing and parsing
  - Type systems
  - Interpretation
- Programming Language Semantics
  - Lambda Calculus
  - Operational Semantics
  - Axiomatic Semantics
OCAML

• Locally:
  • Compiler is on the EWS-linux systems at /usr/local/bin/ocaml

• Globally:
  • Main CAML home: http://ocaml.org
  • To install OCAML on your computer see: http://ocaml.org/docs/install.html
References for OCaml

Supplemental texts (not required):

- The Objective Caml system release 4.05, by Xavier Leroy, online manual
- Introduction to the Objective Caml Programming Language, by Jason Hickey
- Developing Applications With Objective Caml, by Emmanuel Chailloux, Pascal Manoury, and Bruno Pagano, on O’Reilly
  - Available online from course resources
OCAML Background

- CAML is European descendant of original ML
  - American/British version is SML
  - O is for object-oriented extension
- ML stands for Meta-Language
- ML family designed for implementing theorem provers
  - It was the meta-language for programming the “object” language of the theorem prover
  - Despite obscure original application area, OCAMML is a full general-purpose programming language
Features of OCAML

- Higher order applicative language
- Call-by-value parameter passing
- Modern syntax
- Parametric polymorphism
  - Aka structural polymorphism
- Automatic garbage collection
- User-defined algebraic data types

It’s fast - winners of the 1999 and 2000 ICFP Programming Contests used OCAML
Why learn OCAML?

- Many features not clearly in languages you have already learned
- Assumed basis for much research in programming language research
- OCAML is particularly efficient for programming tasks involving languages (eg parsing, compilers, user interfaces)
- Industrially Relevant: Jane Street trades billions of dollars per day using OCaml programs
- Similar languages: Microsoft F#, SML, Haskell, Scala
Session in OCAML

% ocaml

Objective Caml version 4.01

# (* Read-eval-print loop; expressions and declarations *)
  2 + 3;; (* Expression *)

- : int = 5

# 3 < 2;;

- : bool = false
No Overloading for Basic Arithmetic Operations

# 15 * 2;;
- : int = 30

# 1.35 + 0.23;; (* Wrong type of addition *)
Characters 0-4:
    1.35 + 0.23;; (* Wrong type of addition *)
    ^^^^^^

Error: This expression has type float but an expression was expected of type int

# 1.35 +. 0.23;;
- : float = 1.58
No Implicit Coercion

# 1.0 * 2;; (* No Implicit Coercion *)

Characters 0-3:

1.0 * 2;; (* No Implicit Coercion *)

^ ^ ^

Error: This expression has type float but an expression was expected of type int
Sequencing Expressions

# "Hi there";; (* has type string *)
- : string = "Hi there"

# print_string "Hello world\n";; (* has type unit *)
Hello world
- : unit = ()

# (print_string "Bye\n"; 25);; (* Sequence of exp *)
Bye
- : int = 25
Declarations; Sequencing of Declarations

# let x = 2 + 3;;  (* declaration *)
val x : int = 5

# let test = 3 < 2;;
val test : bool = false

# let a = 1 let b = a + 4;;  (* Sequence of dec *
val a : int = 1
val b : int = 5
Environments

- *Environments* record what value is associated with a given identifier
- Central to the semantics and implementation of a language
- Notation

\[
\rho = \{\text{name}_1 \rightarrow \text{value}_1, \text{name}_2 \rightarrow \text{value}_2, \ldots\}
\]

Using set notation, but describes a partial function

- Often stored as list, or stack
  - To find value start from left and take first match
Environments

X \rightarrow 3

name \rightarrow “Steve”

y \rightarrow 17

region \rightarrow (5.4, 3.7)

b \rightarrow true

id \rightarrow \{Name = “Paul”,
               Age = 23,
               SSN = 999888777\}
Global Variable Creation

# 2 + 3;; (* Expression *)
// doesn’t affect the environment
# let test = 3 < 2;; (* Declaration *)
val test : bool = false
// ρ₁ = \{test → false\}
# let a = 1 let b = a + 4;; (* Seq of dec *)
// ρ₂ = \{b → 5, a → 1, test → false\}
Environments

test $\rightarrow$ true

a $\rightarrow$ 1

b $\rightarrow$ 5
// $\rho_2 = \{ b \rightarrow 5, a \rightarrow 1, \text{test} \rightarrow \text{false} \}$

let test = 3.7;;

- What is the environment after this declaration?
New Bindings Hide Old

// \( \rho_2 = \{b \rightarrow 5, \ a \rightarrow 1, \ test \rightarrow \text{false}\} \)
let test = 3.7;;

What is the environment after this declaration?

// \( \rho_3 = \{\text{test} \rightarrow 3.7, \ a \rightarrow 1, \ b \rightarrow 5\} \)
Environments

test ➔ 3.7

a ➔ 1   b ➔ 5
Now it’s your turn

You should be able to do WA1
Problem 1, parts (* 1 *) and (* 2 *)
Local Variable Creation

// \( \rho_3 = \{\text{test} \rightarrow 3.7, \text{a} \rightarrow 1, \text{b} \rightarrow 5\} \)

# let b = 5 \times 4

// \( \rho_4 = \{\text{b} \rightarrow 20, \text{test} \rightarrow 3.7, \text{a} \rightarrow 1\} \)

in 2 \times b;;

- : int = 40

// \( \rho_5 = \rho_3 = \{\text{test} \rightarrow 3.7, \text{a} \rightarrow 1, \text{b} \rightarrow 5\} \)

# b;;

- : int = 5
Local let binding

// ρ5 = {test → 3.7, a → 1, b → 5}
# let c =
  let b = a + a
// ρ6 = {b → 2} + ρ3
// ={b → 2, test → 3.7, a → 1}
  in b * b;;
val c : int = 4
// ρ7 = {c → 4, test → 3.7, a → 1, b → 5}
# b;;
- : int = 5
Local let binding

// \( \rho_5 = \{ \text{test} \rightarrow 3.7, \ a \rightarrow 1, \ b \rightarrow 5 \} \)
# let c =
  let b = a + a
// \( \rho_6 = \{ b \rightarrow 2 \} + \rho_3 \)
// \( =\{ b \rightarrow 2, \ \text{test} \rightarrow 3.7, \ a \rightarrow 1 \} \)
in b * b;;
val c : int = 4
// \( \rho_7 = \{ c \rightarrow 4, \ \text{test} \rightarrow 3.7, \ a \rightarrow 1, \ b \rightarrow 5 \} \)
# b;;
- : int = 5
Local let binding

// $\rho_5 = \{\text{test} \rightarrow 3.7, \ a \rightarrow 1, \ b \rightarrow 5\}$

# let c =

let b = a + a

// $\rho_6 = \{b \rightarrow 2\} + \rho_3$

// $=\{b \rightarrow 2, \ \text{test} \rightarrow 3.7, \ a \rightarrow 1\}$

in b * b;;

val c : int = 4

// $\rho_7 = \{c \rightarrow 4, \ \text{test} \rightarrow 3.7, \ a \rightarrow 1, \ b \rightarrow 5\}$

# b;;

- : int = 5
Now it’s your turn

You should be able to do WA1
Problem 1, parts (* 3 *) and (* 4 *)
Booleans (aka Truth Values)

# true;;
- : bool = true

# false;;
- : bool = false

// \( \rho_7 = \{c \rightarrow 4, \text{test} \rightarrow 3.7, a \rightarrow 1, b \rightarrow 5\} \)

# if b > a then 25 else 0;;
- : int = 25
Booleans and Short-Circuit Evaluation

# 3 > 1 && 4 > 6;;
- : bool = false

# 3 > 1 || 4 > 6;;
- : bool = true

# (print_string "Hi\n"; 3 > 1) || 4 > 6;;
Hi
- : bool = true

# 3 > 1 || (print_string "Bye\n"; 4 > 6);;
- : bool = true

# not (4 > 6);;
- : bool = true
Now it’s your turn

You should be able to do WA1 Problem 1, part (* 5 *)
Tuples as Values

// ρ₇ = {c → 4, test → 3.7,
         a → 1, b → 5}

# let s = (5,"hi",3.2);;
val s : int * string * float = (5, "hi", 3.2)

// ρ₈ = {s → (5, "hi", 3.2),
         c → 4, test → 3.7,
         a → 1, b → 5}
Pattern Matching with Tuples

\[
\rho_8 = \{ s \rightarrow (5, "hi", 3.2), \\
    c \rightarrow 4, test \rightarrow 3.7, \\
    a \rightarrow 1, b \rightarrow 5 \}
\]

# let (a,b,c) = s;; (* (a,b,c) is a pattern *)
val a : int = 5
val b : string = "hi"
val c : float = 3.2

# let x = 2, 9.3;; (* tuples don't require parens in Ocaml *)
val x : int * float = (2, 9.3)
Nested Tuples

(* Tuples can be nested *)

let d = ((1,4,62),("bye",15),73.95);;

val d : (int * int * int) * (string * int) * float =
((1, 4, 62), ("bye", 15), 73.95)

(* Patterns can be nested *)

let (p,(st,_),_) = d;; (* _ matches all, binds nothing *)

val p : int * int * int = (1, 4, 62)

val st : string = "bye"
Now it’s your turn

You should be able to do WA1 Problem 1, part (* 6 *)
Functions

# let plus_two n = n + 2;;
val plus_two : int -> int = <fun>
# plus_two 17;;
- : int = 19
let plus_two \( n = n + 2 \);

```
plus_two 17
- : int = 19
```
Nameless Functions (aka Lambda Terms)

\[
\text{fun } n \rightarrow n + 2; ;
\]

\[
(f\text{un } n \rightarrow n + 2)\ 17; ;
\]

\[- : \text{int} = 19\]
# let plus_two n = n + 2;;
val plus_two : int -> int = <fun>
# plus_two 17;;
- : int = 19
# let plus_two = fun n -> n + 2;;
val plus_two : int -> int = <fun>
# plus_two 14;;
- : int = 16

First definition syntactic sugar for second
Using a nameless function

# (fun x -> x * 3) 5;; (* An application *)
- : int = 15

# ((fun y -> y +. 2.0), (fun z -> z * 3));;
(* As data *)
- : (float -> float) * (int -> int) = (<fun>, <fun>)

Note: in fun v -> exp(v), scope of variable is only the body exp(v)
Values fixed at declaration time

```ocaml
# let x = 12;;
val x : int = 12

# let plus_x y = y + x;;
val plus_x : int -> int = <fun>

# plus_x 3;;
```

What is the result?
Values fixed at declaration time

# let x = 12;;
val x : int = 12

# let plus_x y = y + x;;
val plus_x : int -> int = <fun>

# plus_x 3;;
- : int = 15
Values fixed at declaration time

# let x = 7;; (* New declaration, not an update *)
val x : int = 7

# plus_x 3;;

What is the result this time?
Values fixed at declaration time

```ocaml
# let x = 7;; (* New declaration, not an update *)
val x : int = 7
# plus_x 3;;
```

What is the result this time?
# let x = 7;; (* New declaration, not an update *)

val x : int = 7

# plus_x 3;;

- : int = 15
Observation: Functions are first-class values in this language

Question: What value does the environment record for a function variable?

Answer: a closure
A **closure** is a pair of an environment and an association of a sequence of variables (the input variables) with an expression (the function body), written:

\[ f \rightarrow < (v_1, \ldots, v_n) \rightarrow \text{exp}, \ \rho_f > \]

Where \( \rho_f \) is the environment in effect when \( f \) is defined (if \( f \) is a simple function)
Closure for plus_x

- When plus_x was defined, had environment:
  \[ \rho_{plus_x} = \{ ..., x \rightarrow 12, ... \} \]

- Recall: \texttt{let plus_x y = y + x} is really \texttt{let plus_x = fun y -> y + x}

- Closure for \texttt{fun y -> y + x}:
  \[ \langle y \rightarrow y + x, \rho_{plus_x} \rangle \]

- Environment just after plus_x defined:
  \[ \{ plus_x \rightarrow \langle y \rightarrow y + x, \rho_{plus_x} \rangle \} + \rho_{plus_x} \]
Now it’s your turn

You should be able to do WA1 Problem 1, parts (* 7 *) and (* 8 *)
Evaluation of Application of plus_x;;

- Have environment:
  \[ \rho = \{ \text{plus}_x \rightarrow <y \rightarrow y + x, \ \rho_{\text{plus}_x} >, \ldots, \ y \rightarrow 3, \ldots \} \]
  where \( \rho_{\text{plus}_x} = \{ x \rightarrow 12, \ldots, y \rightarrow 24, \ldots \} \)

- Eval (plus_x y, \( \rho \)) rewrites to
- Eval (App <y \rightarrow y + x, \( \rho_{\text{plus}_x} > 3, \rho \)) rewrites to
- Eval (y + x, \{y \rightarrow 3\} +\( \rho_{\text{plus}_x} )\) rewrites to
- Eval (3 + 12 , \( \rho_{\text{plus}_x} \)) = 15
Functions with more than one argument

```ocaml
# let add_three x y z = x + y + z;;
val add_three : int -> int -> int -> int = <fun>
# let t = add_three 6 3 2;;
val t : int = 11
# let add_three =
  fun x -> (fun y -> (fun z -> x + y + z));;
val add_three : int -> int -> int -> int = <fun>
```

Again, first syntactic sugar for second argument.
Partial application of functions

```ocaml
let add_three x y z = x + y + z;;

# let h = add_three 5 4;;
val h : int -> int = <fun>
# h 3;;
- : int = 12
# h 7;;
- : int = 16
```
Functions as arguments

# let thrice f x = f (f (f x));;
val thrice : ('a -> 'a) -> 'a -> 'a = <fun>
# let g = thrice plus_two;;
val g : int -> int = <fun>
# g 4;;
- : int = 10
# thrice (fun s -> "Hi! " ^ s) "Good-bye!";;
- : string = "Hi! Hi! Hi! Good-bye!"
Functions on tuples

# let plus_pair (n,m) = n + m;;
val plus_pair : int * int -> int = <fun>
# plus_pair (3,4);;
- : int = 7
# let double x = (x,x);;
val double : 'a -> 'a * 'a = <fun>
# double 3;;
- : int * int = (3, 3)
# double "hi";;
- : string * string = ("hi", "hi")
# let triple_to_pair triple =

match triple
with (0, x, y) -> (x, y)
| (x, 0, y) -> (x, y)
| (x, y, _) -> (x, y);

val triple_to_pair : int * int * int -> int * int = <fun>

• Each clause: pattern on left, expression on right
• Each x, y has scope of only its clause
• Use first matching clause
Closure for \texttt{plus\_pair}

- Assume $\rho_{\text{plus\_pair}}$ was the environment just before \texttt{plus\_pair} defined

- Closure for \texttt{plus\_pair}:
  \[
  \langle (n,m) \rightarrow n + m, \rho_{\text{plus\_pair}} \rangle
  \]

- Environment just after \texttt{plus\_pair} defined:
  \[
  \{ \text{plus\_pair} \rightarrow \langle (n,m) \rightarrow n + m, \rho_{\text{plus\_pair}} \rangle \}
  \]
  \[+ \rho_{\text{plus\_pair}} \]