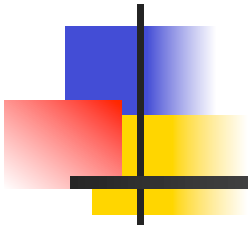


Programming Languages and Compilers (CS 421)

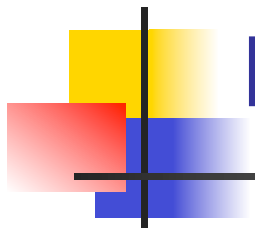


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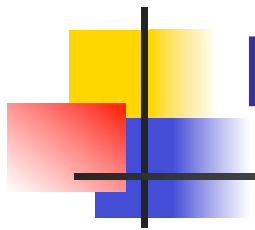
<http://courses.engr.illinois.edu/cs421>

Based in part on slides by Mattox Beckman, as updated by Vikram Adve and Gul Agha



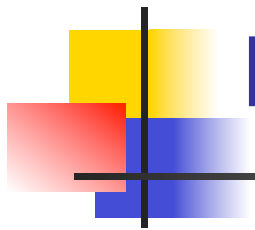
Recursive Descent Parsing

- Recursive descent parsers are a class of parsers derived fairly directly from BNF grammars
- A recursive descent parser traces out a parse tree in top-down order, corresponding to a left-most derivation (LL - left-to-right scanning, leftmost derivation)



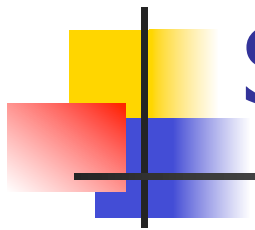
Recursive Descent Parsing

- Each nonterminal in the grammar has a subprogram associated with it; the subprogram parses all phrases that the nonterminal can generate
- Each nonterminal in right-hand side of a rule corresponds to a recursive call to the associated subprogram



Recursive Descent Parsing

- Each subprogram must be able to decide how to begin parsing by looking at the left-most character in the string to be parsed
 - May do so directly, or indirectly by calling another parsing subprogram
- Recursive descent parsers, like other top-down parsers, cannot be built from left-recursive grammars
 - Sometimes can modify grammar to suit



Sample Grammar

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle \mid \langle \text{term} \rangle + \langle \text{expr} \rangle$
 $\mid \langle \text{term} \rangle - \langle \text{expr} \rangle$

$\langle \text{term} \rangle ::= \langle \text{factor} \rangle \mid \langle \text{factor} \rangle * \langle \text{term} \rangle$
 $\mid \langle \text{factor} \rangle / \langle \text{term} \rangle$

$\langle \text{factor} \rangle ::= \langle \text{id} \rangle \mid (\langle \text{expr} \rangle)$



Tokens as OCaml Types

- + - * / () <id>

- Becomes an OCaml datatype

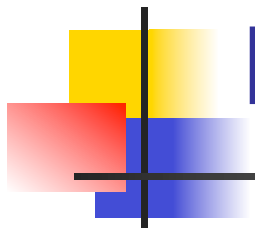
type token =

 Id_token of string

 | Left_parenthesis | Right_parenthesis

 | Times_token | Divide_token

 | Plus_token | Minus_token

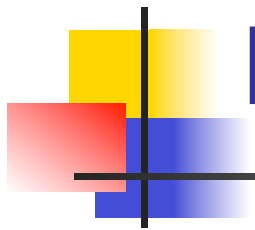


Parse Trees as Datatypes

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle \mid \langle \text{term} \rangle + \langle \text{expr} \rangle$
 $\mid \langle \text{term} \rangle - \langle \text{expr} \rangle$

type expr =

Term_as_Expr of term
| Plus_Expr of (term * expr)
| Minus_Expr of (term * expr)



Parse Trees as Datatypes

$$\begin{aligned} \langle \text{term} \rangle ::= & \langle \text{factor} \rangle \mid \langle \text{factor} \rangle * \\ & \langle \text{term} \rangle \\ & \mid \langle \text{factor} \rangle / \langle \text{term} \rangle \end{aligned}$$

and term =

Factor_as_Term of factor
| Mult_Term of (factor * term)
| Div_Term of (factor * term)



Parse Trees as Datatypes

$\langle \text{factor} \rangle ::= \langle \text{id} \rangle \mid (\langle \text{expr} \rangle)$

and factor =

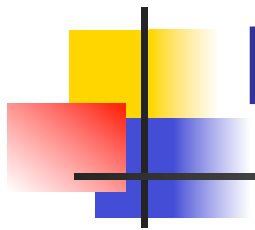
Id_as_Factor of string

| Parenthesized_Expr_as_Factor of expr



Parsing Lists of Tokens

- Will create three mutually recursive functions:
 - $\text{expr} : \text{token list} \rightarrow (\text{expr} * \text{token list})$
 - $\text{term} : \text{token list} \rightarrow (\text{term} * \text{token list})$
 - $\text{factor} : \text{token list} \rightarrow (\text{factor} * \text{token list})$
- Each parses what it can and gives back parse and remaining tokens



Parsing an Expression

```
<expr> ::= <term> [ ( + | - ) <expr> ]  
let rec expr tokens =  
  (match term tokens  
   with ( term_parse , tokens_after_term) ->  
        (match tokens_after_term  
         with( Plus_token  :: tokens_after_plus) ->
```



Parsing an Expression

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle [(+ \mid -) \langle \text{expr} \rangle]$

let rec expr tokens =

(match **term tokens**

with (term_parse , tokens_after_term) ->

(match tokens_after_term

with (Plus_token :: tokens_after_plus) ->



Parsing a Plus Expression

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle [(+ \mid -) \langle \text{expr} \rangle]$

let rec expr tokens =
 (match term tokens
 with (**term_parse** , tokens_after_term) ->
 (match tokens_after_term
 with (Plus_token :: tokens_after_plus) ->



Parsing a Plus Expression

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle \underline{[(+ | -) \langle \text{expr} \rangle]}$

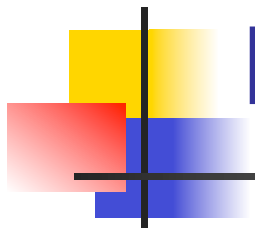
let rec expr tokens =

(match term tokens

with (**term_parse** , tokens_after_term) ->

(match **tokens_after_term**

with (Plus_token :: tokens_after_plus) ->



Parsing a Plus Expression

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle [(+ | -) \langle \text{expr} \rangle]$

let rec expr tokens =

(match term tokens

with (term_parse , tokens_after_term) ->

(match tokens_after_term

with (**Plus_token** :: tokens_after_plus) ->

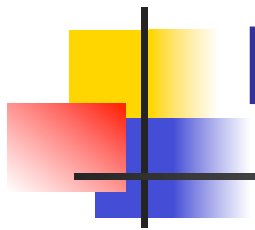




Parsing a Plus Expression

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle + \langle \text{expr} \rangle$

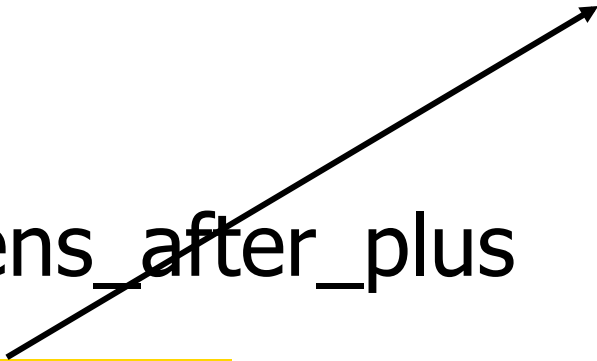
(match **expr tokens_after_plus**
with (expr_parse , tokens_after_expr) ->
(Plus_Expr (term_parse , expr_parse),
tokens_after_expr))



Parsing a Plus Expression

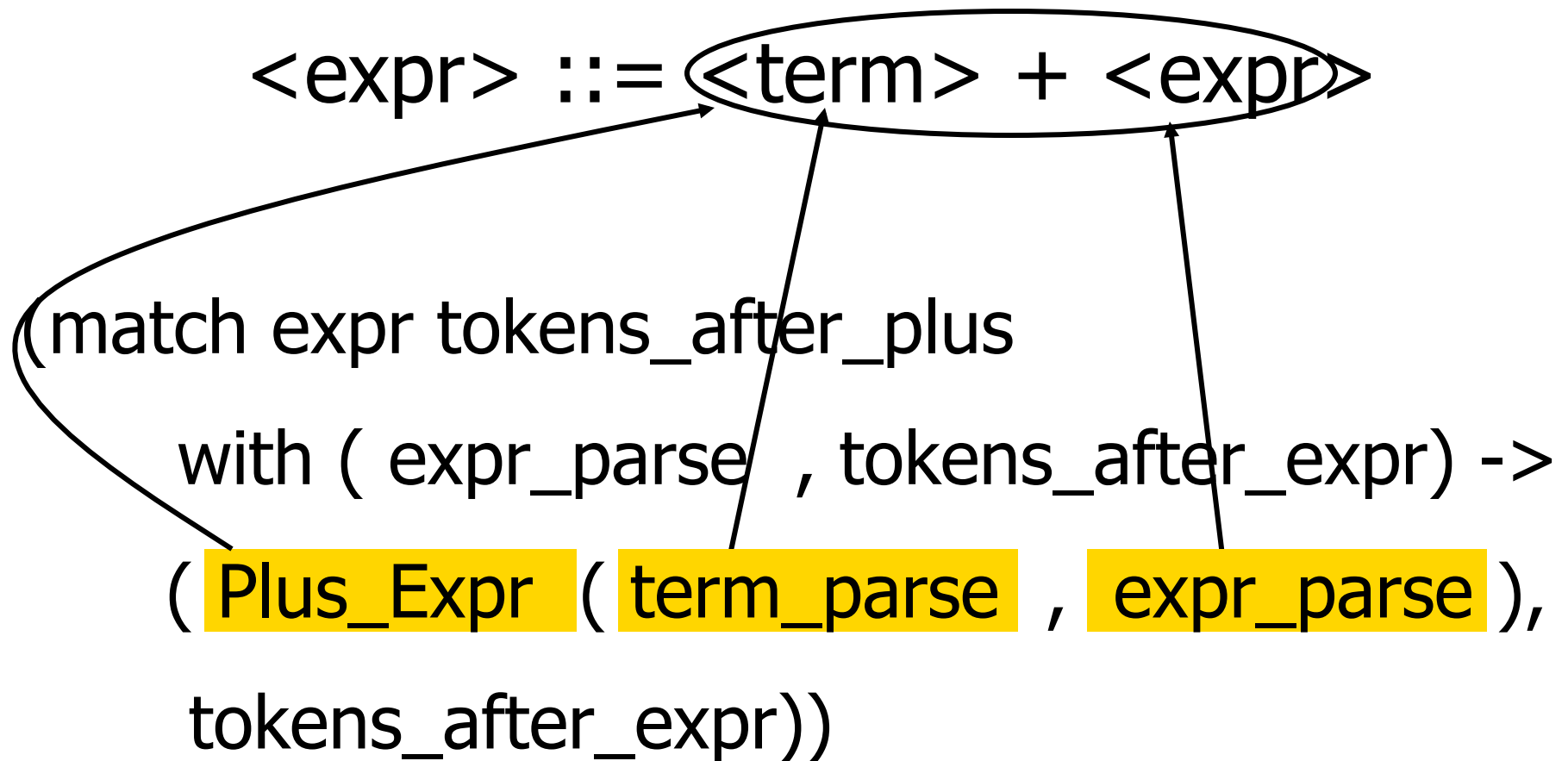
$\langle \text{expr} \rangle ::= \langle \text{term} \rangle + \langle \text{expr} \rangle$

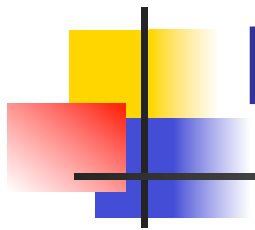
(match expr tokens_after_plus
with (**expr_parse** , tokens_after_expr) ->
(Plus_Expr (term_parse , expr_parse),
tokens_after_expr))





Building Plus Expression Parse Tree





Parsing a Minus Expression

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle - \langle \text{expr} \rangle$

```
| ( Minus_token :: tokens_after_minus) ->  
  (match expr tokens_after_minus  
   with ( expr_parse , tokens_after_expr) ->  
    ( Minus_Expr ( term_parse , expr_parse ),  
      tokens_after_expr))
```

Parsing a Minus Expression

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle - \langle \text{expr} \rangle$

| (**Minus_token** :: tokens_after_minus) ->
(match expr tokens_after_minus
with (expr_parse , tokens_after_expr) ->
(**Minus_Expr** (**term_parse** , **expr_parse**),
tokens_after_expr))



Parsing an Expression as a Term

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle$

| _ -> (Term_as_Expr **term_parse** ,
tokens_after_term)))



- Code for **term** is same except for replacing addition with multiplication and subtraction with division



Parsing Factor as Id

`<factor> ::= <id>`

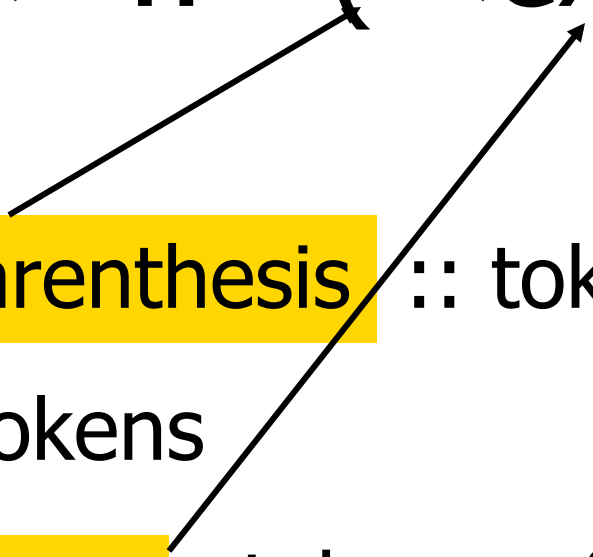
```
and factor tokens =  
  (match tokens  
   with (Id_token id_name :: tokens_after_id) =  
        ( Id_as_Factor id_name, tokens_after_id)
```



Parsing Factor as Parenthesized Expression

$\langle \text{factor} \rangle ::= (\langle \text{expr} \rangle)$

| factor (Left_parenthesis :: tokens) =
 (match expr tokens
 with (expr_parse , tokens_after_expr) ->

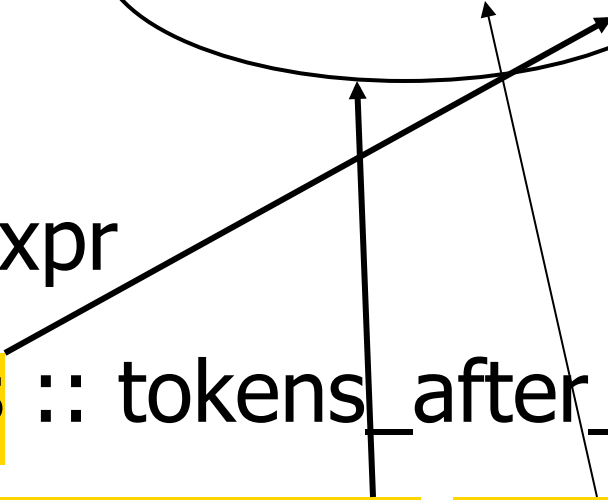




Parsing Factor as Parenthesized Expression

$\langle \text{factor} \rangle ::= (\langle \text{expr} \rangle)$

(match tokens_after_expr
with **Right_parenthesis** :: tokens_after_rparen ->
(**Parenthesized_Expr_as_Factor** **expr_parse** ,
tokens_after_rparen)





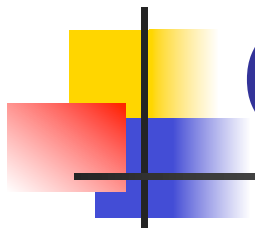
Error Cases

- What if no matching right parenthesis?

```
| _ -> raise (Failure "No matching  
rparen") ) )
```

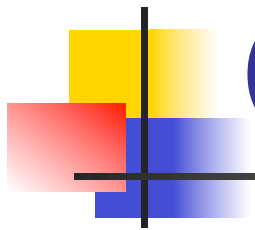
- What if no leading id or left parenthesis?

```
| _ -> raise (Failure "No id or lparen" ) );;
```

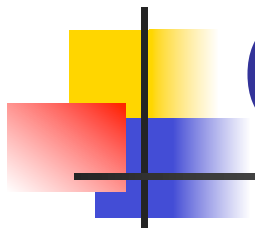


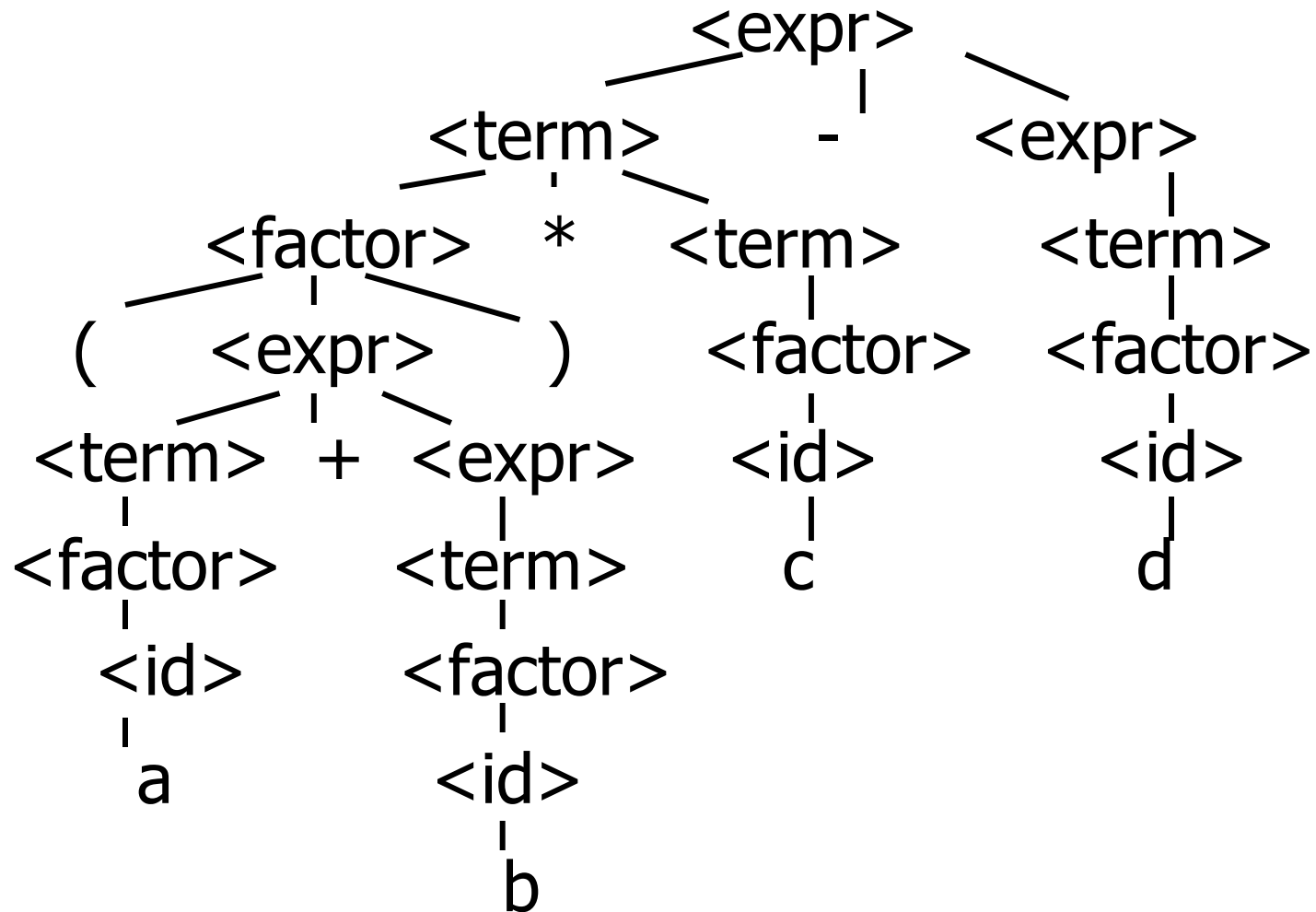
$(a + b) * c - d$

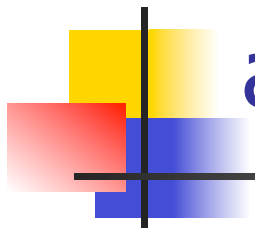
```
expr [Left_parenthesis; Id_token "a";  
      Plus_token; Id_token "b";  
      Right_parenthesis; Times_token;  
      Id_token "c"; Minus_token;  
      Id_token "d"];;
```


$$(a + b) * c - d$$

```
- : expr * token list =  
(Minus_Expr  
  (Mult_Term  
    (Parenthesized_Expr_as_Factor  
      (Plus_Expr  
        (Factor_as_Term (Id_as_Factor "a"),  
          Term_as_Expr (Factor_as_Term  
            (Id_as_Factor "b")))),  
        Factor_as_Term (Id_as_Factor "c")),  
      Term_as_Expr (Factor_as_Term (Id_as_Factor  
        "d")))),  
    [])
```


$$(a + b) * c - d$$





a + b * c - d

```
# expr [Id_token "a"; Plus_token; Id_token "b";  
      Times_token; Id_token "c"; Minus_token;  
      Id_token "d"];;
```

```
- : expr * token list =
```

```
(Plus_Expr
```

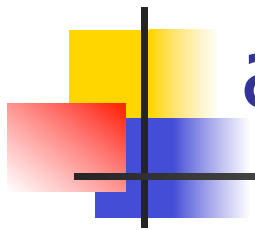
```
  (Factor_as_Term (Id_as_Factor "a"),
```

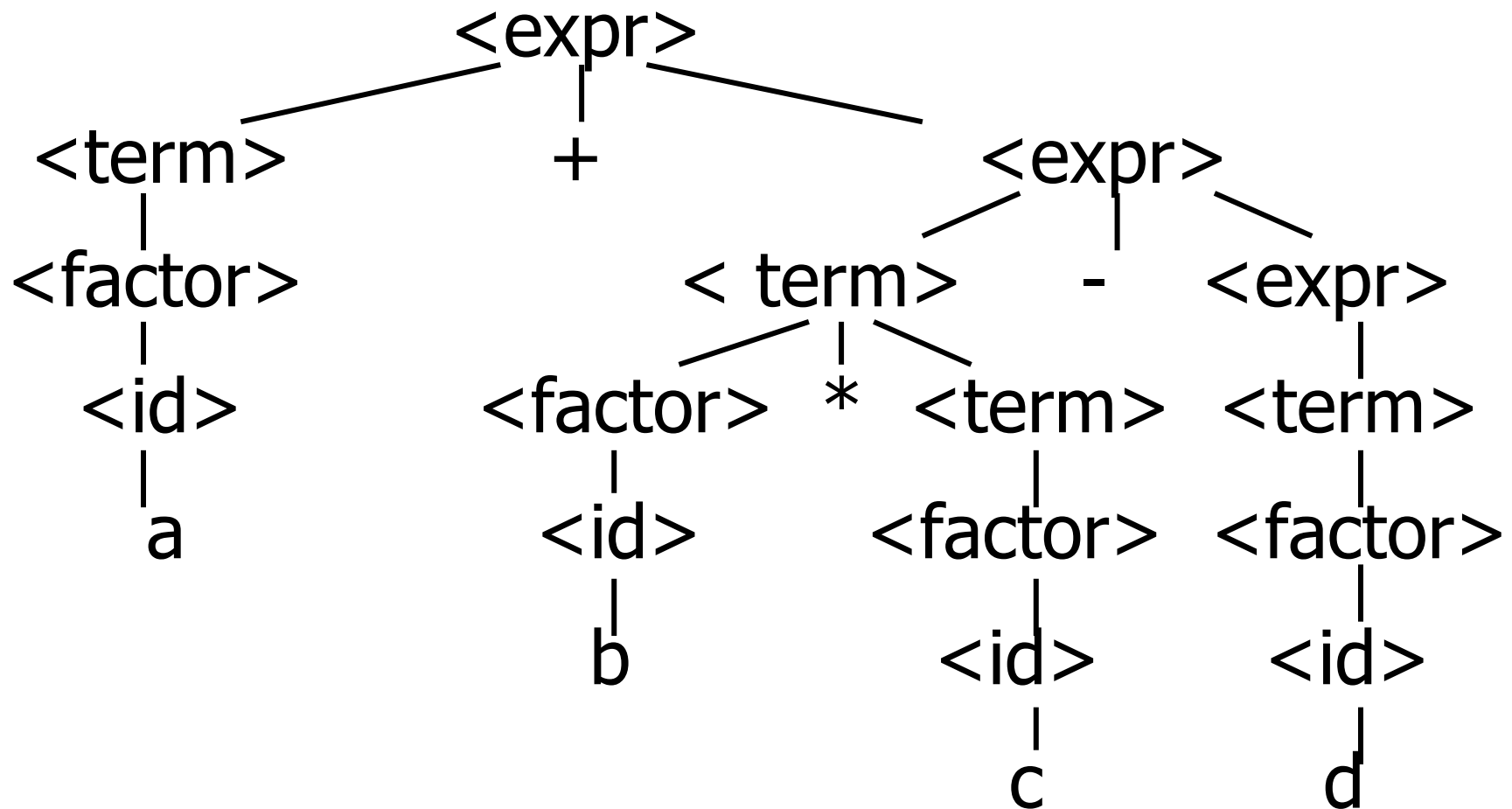
```
  Minus_Expr
```

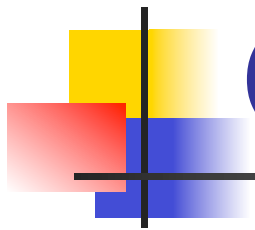
```
    (Mult_Term (Id_as_Factor "b", Factor_as_Term  
      (Id_as_Factor "c")),
```

```
    Term_as_Expr (Factor_as_Term (Id_as_Factor  
      "d")))),
```

```
[])
```


$$a + b * c - d$$



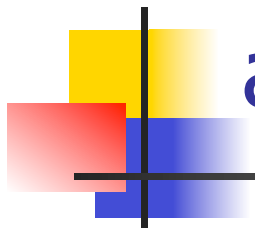


(a + b * c - d

```
# expr [Left_parenthesis; Id_token "a";  
Plus_token; Id_token "b"; Times_token;  
Id_token "c"; Minus_token; Id_token "d"];;
```

Exception: Failure "No matching rparen".

Can't parse because it was expecting a right parenthesis but it got to the end without finding one



$a + b) * c - d *$

```
expr [Id_token "a"; Plus_token; Id_token "b";  
      Right_parenthesis; Times_token; Id_token "c";  
      Minus_token; Id_token "d"];;
```

- : expr * token list =

(Plus_Expr

(Factor_as_Term (Id_as_Factor "a"),

Term_as_Expr (Factor_as_Term (Id_as_Factor
"b"))),

[Right_parenthesis; Times_token; Id_token "c";
Minus_token; Id_token "d"])



Parsing Whole String

- Q: How to guarantee whole string parses?
- A: Check returned tokens empty

let parse tokens =

match **expr** tokens

with (expr_parse, []) -> expr_parse

| _ -> raise (Failure "No parse");;

- Fixes <expr> as start symbol



Streams in Place of Lists

- More realistically, we don't want to create the entire list of tokens before we can start parsing
- We want to generate one token at a time and use it to make one step in parsing
- Will use $(\text{token} * (\text{unit} \rightarrow \text{token}))$ or $(\text{token} * (\text{unit} \rightarrow \text{token option}))$
in place of token list



Problems for Recursive-Descent Parsing

- Left Recursion:

$A ::= Aw$

translates to a subroutine that loops forever

- Indirect Left Recursion:

$A ::= Bw$

$B ::= Av$

causes the same problem



Problems for Recursive-Descent Parsing

- Parser must always be able to choose the next action based only on the very next token
- Pairwise Disjointedness Test: Can we always determine which rule (in the non-extended BNF) to choose based on just the first token



Pairwise Disjointedness Test

- For each rule

$A ::= y$

Calculate

$\text{FIRST}(y) =$

$$\{a \mid y \Rightarrow^* aw\} \cup \{\varepsilon \mid \text{if } y \Rightarrow^* \varepsilon\}$$

- For each pair of rules $A ::= y$ and $A ::= z$, require $\text{FIRST}(y) \cap \text{FIRST}(z) = \{\}$



Example

Grammar:

$$\langle S \rangle ::= \langle A \rangle a \langle B \rangle b$$
$$\langle A \rangle ::= \langle A \rangle b \mid b$$
$$\langle B \rangle ::= a \langle B \rangle \mid a$$
$$\text{FIRST}(\langle A \rangle b) = \{b\}$$
$$\text{FIRST}(b) = \{b\}$$

Rules for $\langle A \rangle$ not pairwise disjoint



Eliminating Left Recursion

- Rewrite grammar to shift left recursion to right recursion
 - Changes associativity

- Given

$\langle \text{expr} \rangle ::= \langle \text{expr} \rangle + \langle \text{term} \rangle$ and

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle$

- Add new non-terminal $\langle e \rangle$ and replace above rules with

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle \langle e \rangle$

$\langle e \rangle ::= + \langle \text{term} \rangle \langle e \rangle \mid \varepsilon$



Factoring Grammar

- Test too strong: Can't handle

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle [(+ \mid -) \langle \text{expr} \rangle]$

- Answer: Add new non-terminal and replace above rules by

$\langle \text{expr} \rangle ::= \langle \text{term} \rangle \langle e \rangle$

$\langle e \rangle ::= + \langle \text{term} \rangle \langle e \rangle$

$\langle e \rangle ::= - \langle \text{term} \rangle \langle e \rangle$

$\langle e \rangle ::= \varepsilon$

- You are delaying the decision point



Example

Both $\langle A \rangle$ and $\langle B \rangle$
have problems:

Transform grammar
to:

$\langle S \rangle ::= \langle A \rangle a \langle B \rangle b$

$\langle A \rangle ::= \langle A \rangle b \mid b$

$\langle B \rangle ::= a \langle B \rangle \mid a$

$\langle S \rangle ::= \langle A \rangle a \langle B \rangle b$

$\langle A \rangle ::= b \langle A1 \rangle$

$\langle A1 \rangle ::= b \langle A1 \rangle \mid \varepsilon$

$\langle B \rangle ::= a \langle B1 \rangle$

$\langle B1 \rangle ::= a \langle B1 \rangle \mid \varepsilon$



Semantics

- Expresses the meaning of syntax
- Static semantics
 - Meaning based only on the form of the expression without executing it
 - Usually restricted to type checking / type inference



Dynamic semantics

- Method of describing meaning of executing a program
- Several different types:
 - Operational Semantics
 - Axiomatic Semantics
 - Denotational Semantics



Dynamic Semantics

- Different languages better suited to different types of semantics
- Different types of semantics serve different purposes



Operational Semantics

- Start with a simple notion of machine
- Describe how to execute (implement) programs of language on virtual machine, by describing how to execute each program statement (ie, following the *structure* of the program)
- Meaning of program is how its execution changes the state of the machine
- Useful as basis for implementations



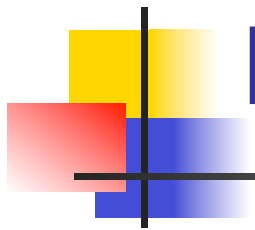
Axiomatic Semantics

- Also called Floyd-Hoare Logic
- Based on formal logic (first order predicate calculus)
- Axiomatic Semantics is a logical system built from *axioms* and *inference rules*
- Mainly suited to simple imperative programming languages



Axiomatic Semantics

- Used to formally prove a property (*post-condition*) of the *state* (the values of the program variables) after the execution of program, assuming another property (*pre-condition*) of the state before execution
- Written :
 {Precondition} Program {Postcondition}
- Source of idea of *loop invariant*



Denotational Semantics

- Construct a function \mathcal{M} assigning a mathematical meaning to each program construct
- Lambda calculus often used as the range of the meaning function
- Meaning function is compositional: meaning of construct built from meaning of parts
- Useful for proving properties of programs



Natural Semantics

- Aka Structural Operational Semantics, aka “Big Step Semantics”
- Provide value for a program by rules and derivations, similar to type derivations
- Rule conclusions look like

$$(C, m) \Downarrow m'$$

or

$$(E, m) \Downarrow v$$