

# Structural Recursion

- Functions on recursive datatypes (eg lists) tend to be recursive
- Recursion over recursive datatypes generally by structural recursion
  - Recursive calls made to components of structure of the same recursive type
  - Base cases of recursive types stop the recursion of the function

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# Structural Recursion : List Example

# let rec length list = match list with [] -> 0 (\* Nil case \*) | x :: xs -> 1 + length xs;; (\* Cons case \*) val length : 'a list -> int = <fun> # length [5; 4; 3; 2];; - : int = 4 • Nil case [] is base case • Cons case recurses on component list xs

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### Terms

- A function is in Direct Style when it returns its result back to the caller.
- A Tail Call occurs when a function returns the result of another function call without any more computations (eg tail recursion)
- A function is in Continuation Passing Style when it passes its result to another function.
- Instead of returning the result to the caller, we pass it forward to another function.

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Example
Simple reporting continuation:
# let report x = (print\_int x; print\_newline());; val report : int -> unit = <fun>
Simple function using a continuation:
# let plusk a b k = k (a + b) val plusk : int -> int -> (int -> 'a) -> 'a = <fun>
# plusk 20 22 report;; 42
- : unit = ()

# Simple Functions Taking Continuations Given a primitive operation, can convert it to pass its result forward to a continuation Examples: # let subk x y k = k(x + y);; val subk : int -> int -> (int -> 'a) -> 'a = <fun> # let eqk x y k = k(x = y);; val eqk : 'a -> 'a -> (bool -> 'b) -> 'b = <fun> # let timesk x y k = k(x \* y);; val timesk : int -> int -> (int -> 'a) -> 'a = <fun>

## Nesting Continuations

# let add\_three x y z = x + y + z;; val add\_three : int -> int -> int -> int = <fun> # let add\_three x y z= let p = x + y in p + z;; val add\_three : int -> int -> int -> int = <fun> # let add\_three\_k x y z k = addk x y (fun p -> addk p zk);; val add\_three\_k : int -> int -> int -> (int -> 'a) -> 'a = <fun>