Describe a DFA that accepts the following language over the alphabet $\Sigma = \{0, 1\}$.

- 1 All strings in which the number of 0s is even and the number of 1s is *not* divisible by 3.
- 2 All strings that are **both** the binary representation of an integer divisible by 3 **and** the ternary (base-3) representation of an integer divisible by 4.

For example, the string 1100 is an element of this language, because it represents $2^3 + 2^2 = 12$ in binary and $3^3 + 3^2 = 36$ in ternary.

Describe deterministic finite-state automata that accept each of the following languages over the alphabet $\Sigma = \{0, 1\}$. You may find it easier to describe these DFAs formally than to draw pictures.

3 All strings w such that $\binom{|w|}{2} \mod 6 = 4$. (**Hint:** Maintain both $\binom{|w|}{2} \mod 6$ and $|w| \mod 6$.)

Work on this later:

4 (Hard.) All strings w such that $F_{\#(10,w)} \mod 10 = 4$, where #(10,w) denotes the number of times 10 appears as a substring of w, and F_n is the nth Fibonacci number:

$$F_n = \begin{cases} 0 & \text{if } n = 0\\ 1 & \text{if } n = 1\\ F_{n-1} + F_{n-2} & \text{otherwise} \end{cases}$$