

- Suppose you are given an array of numbers, some of which are marked as *icky*, and you want to compute the length of the longest increasing subsequence of A that includes at most k icky numbers. Your input consists of the integer k , the number array $A[1..n]$, and another boolean array $Icky[1..n]$.

For example, suppose your input consists of the integer $k = 2$ and the following array (with icky numbers are indicated by stars):

3*	1*	4	1*	5*	9	2*	6	5	3*	5	9	7	9*	3	2	3	8*	4	6*	2	6*
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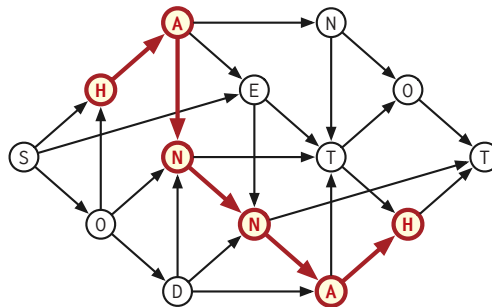
Then your algorithm should return the integer 5, which is the length of the increasing subsequence 4, 5*, 6, 7, 9*.

- Describe an algorithm for this problem using dynamic programming.
- Describe an algorithm for this problem by reducing it to a standard graph problem.

Harder problem to think about later:

- Let G be a directed acyclic graph whose vertices have labels from some fixed alphabet. Any directed path in G has a label, which is a string obtained by concatenating the labels of its vertices. Recall that a *palindrome* is a string that is equal to its reversal.

Describe and analyze an algorithm to find the length of the longest palindrome that is the label of a path in G . For example, given the dag below, your algorithm should return the integer 6, which is the length of the palindrome **HANNAH**.



- Describe an algorithm for this problem using dynamic programming.
- Describe an algorithm for this problem by reducing it to a standard graph problem.