## CS 361 Sample Midterm 1

## NAME:

## NETID:

## CIRCLE YOUR DISCUSSION:

## Thu 2-3 Thu 4-5 Fri 10-11 Fri 11-12

- Be sure that your exam booklet has 6 pages including this cover page
- Make sure to write your name exactly as it appears on your i-card
- Write your netid and circle your discussion section on this page
- Show your work
- This is a closed book exam
- You are allowed one handwritten $8.5 \times 11$-inch sheet of notes (both sides)
- You may not use a calculator or any other electronic device
- Turn off your phone and store it in your backpack
- Store away any other electronic devices including earphones and smartwatches
- Absolutely no interaction between students is allowed
- Use backs of pages for scratch work if needed
- Show your i-card when handing in your exam

| Problem | 1 | 2 | 3 | 4 | 5 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Possible | 30 | 30 | 30 | 30 | 30 | 150 |
| Score |  |  |  |  |  |  |

## Problem 1 ( 30 pts)

1. (10 points) Say you score 40 points out of 50 on Homework 1. Then you score 50 out of 50 on each of the remaining 9 homework assignments. Are your homework scores symmetric, left-skewed or right-skewed? Justify your answer with calculation.

Circle one answer: SYMMETRIC LEFT-SKEWED RIGHT-SKEWED
2. (20 points) Let $\{x\}$ be a dataset consisting of $N$ real numbers, $x_{1}, \ldots, x_{N}$. Show that the function $f(\mu)=\sum_{i}\left(x_{i}-\mu\right)^{2}$ is minimized when $\mu=\operatorname{mean}(\{x\})$.

Problem 2 ( 30 pts) Suppose a teacher gives a multiple choice test of 10 questions to $N$ students. Let $x_{i}$ and $y_{i}$ be the number of questions that the $i$ th student gets right and wrong, respectively.

1. (10 points) Write a formula for mean $(\{y\})$ in terms of mean $(\{x\})$. Draw a box around your answer.
2. (10 points) Write a formula for $\operatorname{std}(\{y\})$ in terms of $\operatorname{std}(\{x\})$. Draw a box around your answer.
3. (10 points) Show that $\operatorname{corr}(\{(x, y)\})=-1$

## Problem 3 (30 pts)

1. (15 points) You draw a card uniformly at random from a standard deck. Let $R$ be the event that the card is red and let $B$ be the event the card is black. Are $R$ and $B$ independent? Draw a box around your answer. Justify your answer with calculation.
2. (15 points) A student takes a multiple choice test. Each question has 4 answer choices. If the student knows the answer to a question, the student gives the right answer. Otherwise, the student guesses uniformly at random from among the answer choices. The student knows the answer to $60 \%$ of the questions. Let $K$ be the event that student knows the answer to a question and let $C$ be the event that the students answers that question correctly. Calculate $P(K \mid C)$. Draw a box around your answer.

## Problem 4 (30 pts)

1. (15 points) Suppose you make a bet on the roll of a fair six-sided die. If the die comes up 6 , you win $\$ 60$. Otherwise, you lose $\$ 30$. Let random variable $W$ be your net winnings. Calculate $E[W]$. Draw a box around your answer.
2. (15 points) Suppose you make the same bet as above three times in a row. Let random variable $T$ be your total net winnings after these three bets. Calculate $P(T \geq 0)$. You do not need to simplify your answer. Draw a box around your answer.

## Problem 5 ( 30 pts )

1. ( 15 points) If I attempt 20 free throws, what is the probability that I score more than 10 points? Assume that each free throw attempt is independent. Also assume that on each free throw attempt, I earn 1 point with probability $p$ and 0 points with probability $1-p$. You may use choose and summation notation in your answer. Draw a box around your answer.
2. (15 points) Suppose the daily number of car accidents per mile of road is a Poisson random variable with intensity $\lambda=0.001$. What is the probability that there are 10 accidents on 1000 miles of road in a week? You do not need to simplify your answer. Draw a box around your answer.
