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OSAI SHOWCASE

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MARCH 2, WEDNESDAY 5 PM TO 6 PM
ROOM 1302 - SIEBEL CS

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BST Rotation Summary

- Four kinds of rotations (L, R, LR, RL)
- All rotations are local (subtrees are not impacted)
- All rotations are constant time: $O(1)$
- BST property maintained

**GOAL:**

We call these trees:
AVL Trees

Three issues for consideration:
- Rotations
- Maintaining Height
- Detecting Imbalance
AVL Tree Rotations

Four templates for rotations:
Theorem:
If an insertion occurred in subtrees $t_3$ or $t_4$ and a subtree was detected at $t$, then a __________ rotation about $t$ restores the balance of the tree.

We gauge this by noting the balance factor of $t$->right is ______.
Finding the Rotation on Insert

**Theorem:**
If an insertion occurred in subtrees $t_2$ or $t_3$ and a subtree was detected at $t$, then a __________ rotation about $t$ restores the balance of the tree.

We gauge this by noting the balance factor of $t$->right is _______.

Insertion into an AVL Tree

```
struct TreeNode {
    T key;
    unsigned height;
    TreeNode *left;
    TreeNode *right;
};
```
Insertion into an AVL Tree

Insert (pseudo code):
1: Insert at proper place
2: Check for imbalance
3: Rotate, if necessary
4: Update height

```c
struct TreeNode {
    T key;
    unsigned height;
    TreeNode *left;
    TreeNode *right;
};
```
template <typename K, typename V>
void AVL<K, D>::_insert(const K & key, const V & data, TreeNode * & cur) {
    if (cur == NULL) { cur = new TreeNode(key, data); }
    else if (key < cur->key) {_insert(key, data, cur->left); }
    else if (key > cur->key) {_insert(key, data, cur->right);}
    _ensureBalance(cur);
}
template <typename K, typename V>
void AVL<K, D>::_ensureBalance(TreeNode *& cur) {
    // Calculate the balance factor:
    int balance = height(cur->right) - height(cur->left);

    // Check if the node is currently not in balance:
    if ( balance == -2 ) {
        int l_balance =
            height(cur->left->right) - height(cur->left->left);
        if ( l_balance == -1 ) { ____________________________; }
        else                   { ____________________________; }
    }

    if ( balance == 2 ) {
        int r_balance =
            height(cur->right->right) - height(cur->right->left);
        if ( r_balance == 1 ) { ____________________________; }
        else                 { ____________________________; }
    }

    _updateHeight(cur);
};
Height-Balanced Tree

Height balance:  \( b = \text{height}(T_R) - \text{height}(T_L) \)
AVL Tree Analysis

We know: insert, remove and find runs in: ____________.

We will argue that: h = ____________.
AVL Tree Analysis

Definition of big-O:

...or, with pictures: