

**From Friday:**

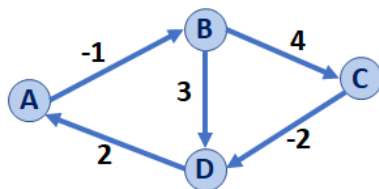
- Graphs with a negative-weight **cycle** have no finite shortest path. (*We can always take the cycle one more time to get an even shorter path!*)
- Graphs with a negative-weight **edge without a negative-weight cycle** DO have a finite shortest path!

**Floyd-Warshall Algorithm**

Floyd-Warshall's Algorithm is an alternative to Dijkstra in the presence of negative-weight edges (but not negative weight cycles).

**Algorithm Design:**

- **Goal:** Find the shortest path from vertex **u** to **v**.
- **Setup:** Create an  $n \times n$  matrix that maintains the best known path between every pair of vertices:
  - Initialize  $(u, u)$  to 0.
  - Initialize all edges present on the graph to their edge weight.
  - Initialize all other edges to +infinity.



	A	B	C	D
A				
B				
C				
D				

- For every vertex **k**, consider which of the following are shorter:
  - $path(u, v)$  - or -
  - $path(u, k) + path(k, v)$

**Big Idea:** \_\_\_\_\_

- Store intermediate results to improve build towards an optimal solution.
- Example application of memorization and **dynamic programming (DP)** – more in CS 374!

**Running Time:**

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Pseudocode for Floyd-Warshall's Algorithm
1 FloydWarshall(G):
2   Input: G, Graph;
3   Output: d, an adjacency matrix of distances between
4           All vertex pairs
5
6   Let d be an adj. matrix (2d array) initialized to +inf
7   foreach (Vertex v : G):
8     d[v][v] = 0
9   foreach (Edge (u, v) : G):
10    d[u][v] = cost(u, v)
11
12  foreach (Vertex k : G):
13    foreach (Vertex u : G):
14      foreach (Vertex v : G):
15        if d[u, v] > d[u, k] + d[k, v]:
16          d[u, v] = d[u, k] + d[k, v]
17
18  return d
    
```

CS 225 – Things To Be Doing:
<ol style="list-style-type: none"> <li>1. lab_hash due Sunday</li> <li>2. last mp released next week</li> <li>3. potds ongoing</li> </ol>