

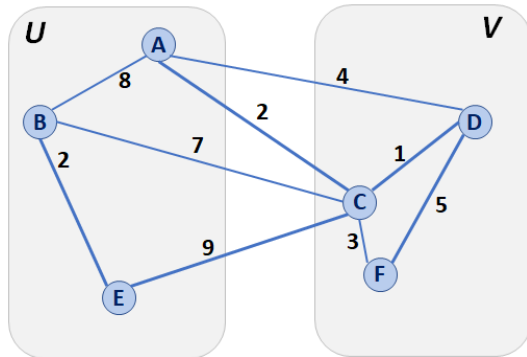
Partition Property

Consider an arbitrary partition of the vertices on **G** into two subsets **U** and **V**.

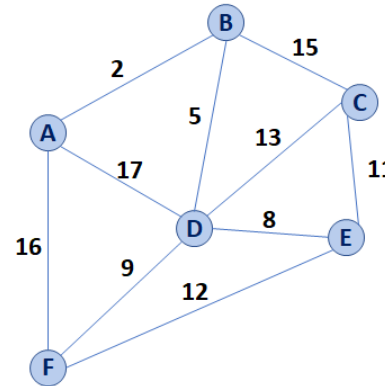
Let **e** be an edge of minimum weight across the partition.

Then **e** is part of some minimum spanning tree.

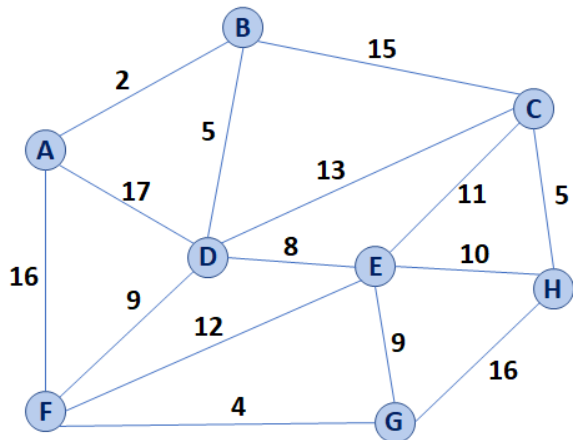
Proof in CS 374!



Prim's Minimum Spanning Tree Algorithm



Partition Property Algorithm



Pseudocode for Prim's MST Algorithm	
1	PrimMST(G, s):
2	Input: G, Graph;
3	s, vertex in G, starting vertex of algorithm
4	Output: T, a minimum spanning tree (MST) of G
5	
6	foreach (Vertex v : G):
7	d[v] = +inf
8	p[v] = NULL
9	d[s] = 0
10	
11	PriorityQueue Q // min distance, defined by d[v]
12	Q.buildHeap(G.vertices())
13	Graph T // "labeled set"
14	
15	repeat n times:
16	Vertex m = Q.removeMin()
17	T.add(m)
18	foreach (Vertex v : neighbors of m not in T):
19	if cost(v, m) < d[v]:
20	d[v] = cost(v, m)
21	p[v] = m
22	
23	return T

	Adj. Matrix	Adj. List
Heap		
Unsorted Array		

Running Time of MST Algorithms

Kruskal's Algorithm:

Prim's Algorithm:

Q: What must be true about the connectivity of a graph when running an MST algorithm?

...what does this imply about the relationship between n and m ?

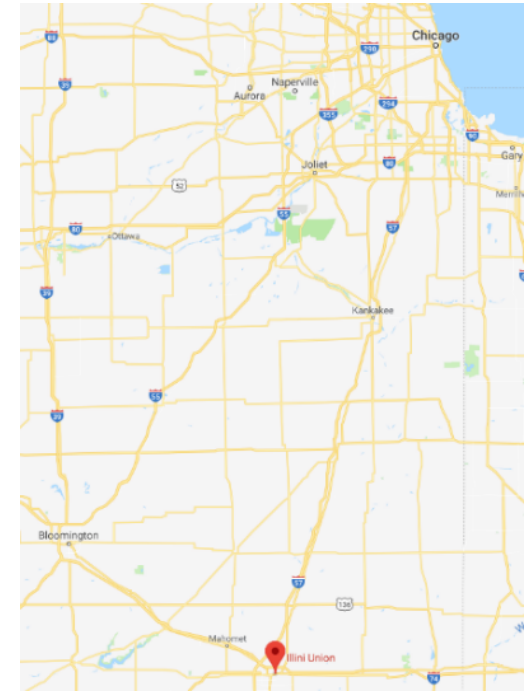
Kruskal's MST	Prim's MST

Q: Suppose we built a new heap that optimized the decrease-key operation, where decreasing the value of a key in a heap updates the heap in amortized constant time, or $O(1)^*$. How does that change Prim's Algorithm runtime?

Final big-O Running Times of classical MST algorithms:

Kruskal's MST	Prim's MST

Shortest Path Home:



CS 225 – Things To Be Doing:

1. Get your projects approved and start work on them.
2. mp_mazes due today.
3. No new mp this week.
4. Daily POTDs are ongoing.