

# Data Structures

## Queues and Iterators (and Trees)

CS 225

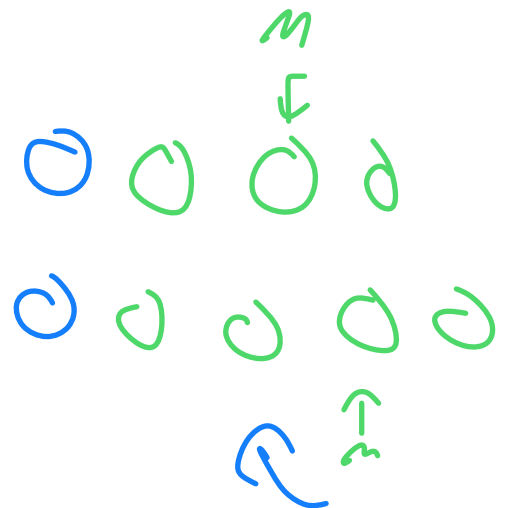
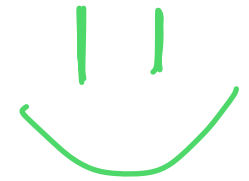
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**ILLINOIS**  
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# Announcements

**Honors Class 199-225:** First class today at CIF - 4039 @ 5 PM

**Exam 1** starts today!

**mp\_stickers** due date is Tuesday for everyone

No late day!

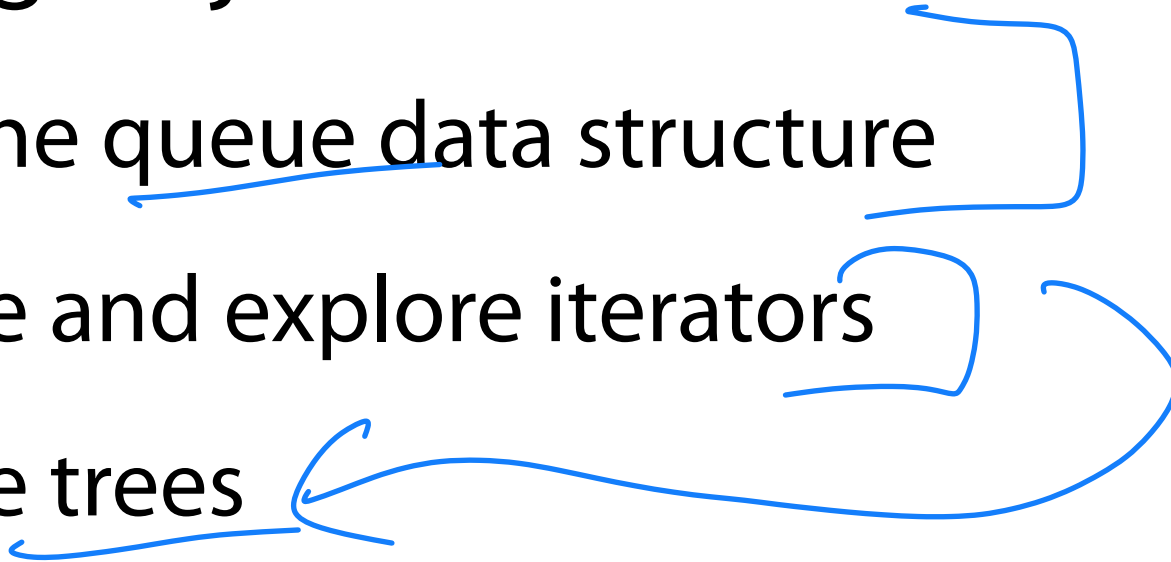
**mp\_lists** releases today (or tomorrow)

# Learning Objectives

Review the queue data structure

Introduce and explore iterators

Introduce trees



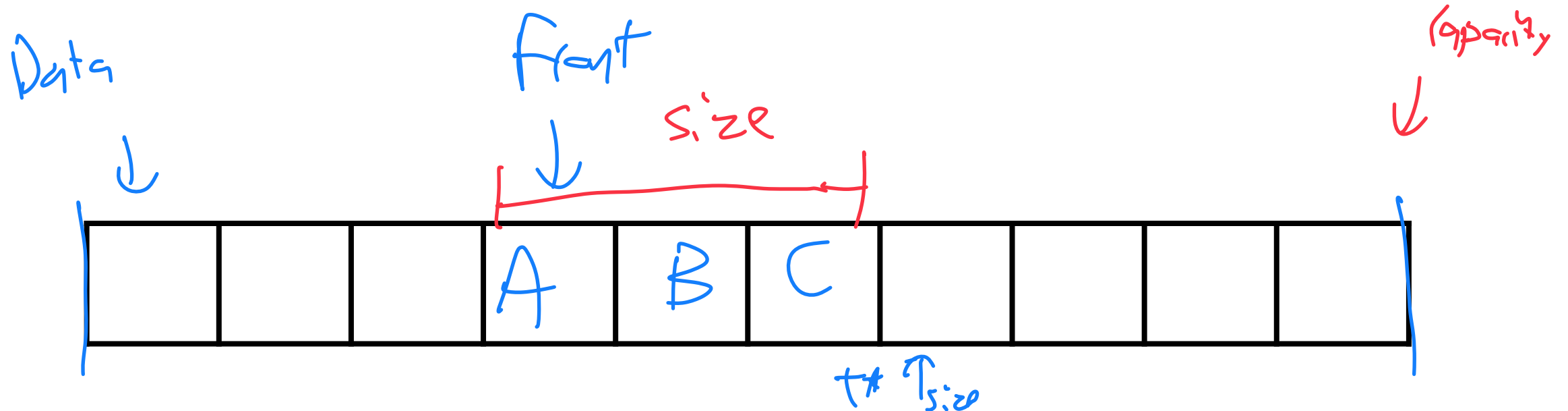
# Queue Data Structure

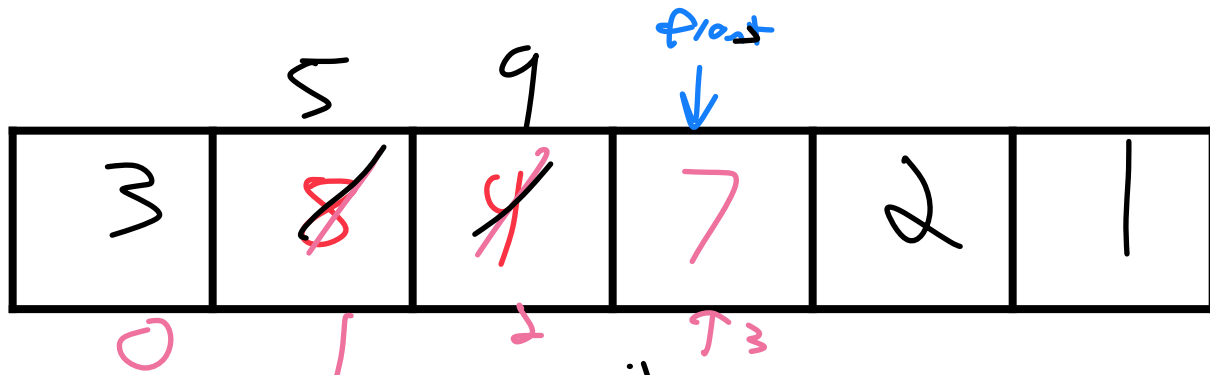
①  
↑  
head

②  
↑  
tail

What do we need to track to maintain a queue with an array list?

$T^*$  → unsigned integers  
↳ front =  
↳ size =





→ If size < capacity  
 Enqueue(D): insert at  $(front + size) \% capacity$   
 ↳ size ++ % capacity

If size == 0 (return null)  
 Dequeue(D): remove at **front**  
 ↳ front ++ % capacity  
 ↳ size --;

Be aware of edge case 5

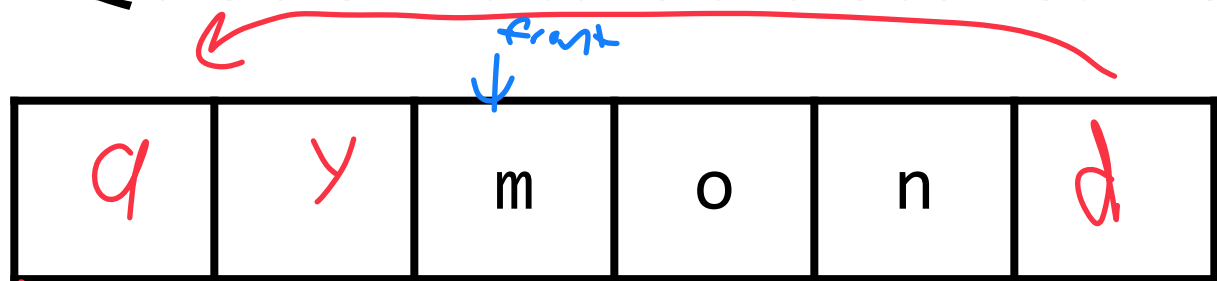
```
Queue<int> q;
q.enqueue(3);
q.enqueue(8);
q.enqueue(4);
q.dequeue();
q.enqueue(7);
q.dequeue();
q.dequeue();
q.enqueue(2);
q.enqueue(1);
q.enqueue(3);
q.enqueue(5);
q.dequeue();
q.enqueue(9);
```

Size: ~~0~~ ~~1~~ ~~2~~ ~~3~~ 4

Front: ~~0~~ ~~1~~ 2

Capacity: 6

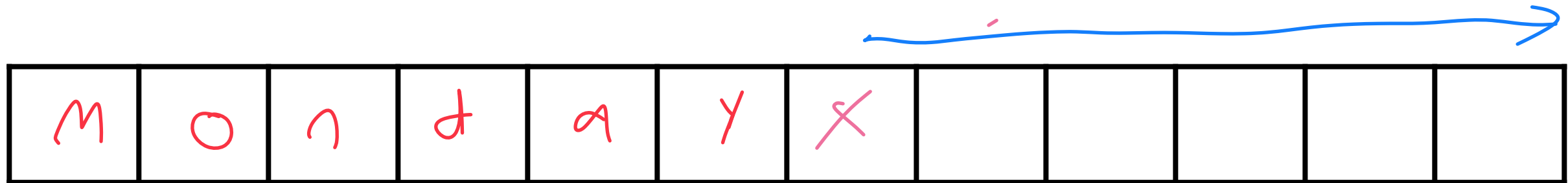
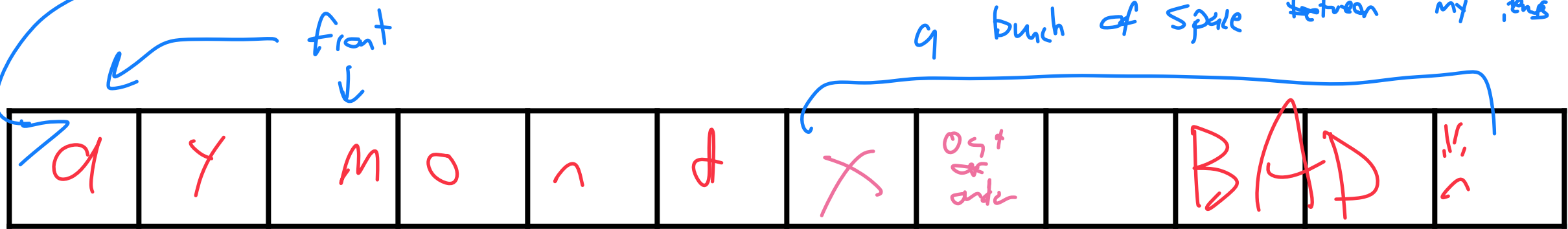
# Queue Data Structure: Resizing



1) Copy from front to end of queue  
 2) set front = 0

```
Queue<char> q;
...
q.enqueue(d);
q.enqueue(a);
q.enqueue(y);
q.enqueue(i);
q.enqueue(s);
```

1) Double size (like normal array)  
 2) When do we copy?





# Queue ADT

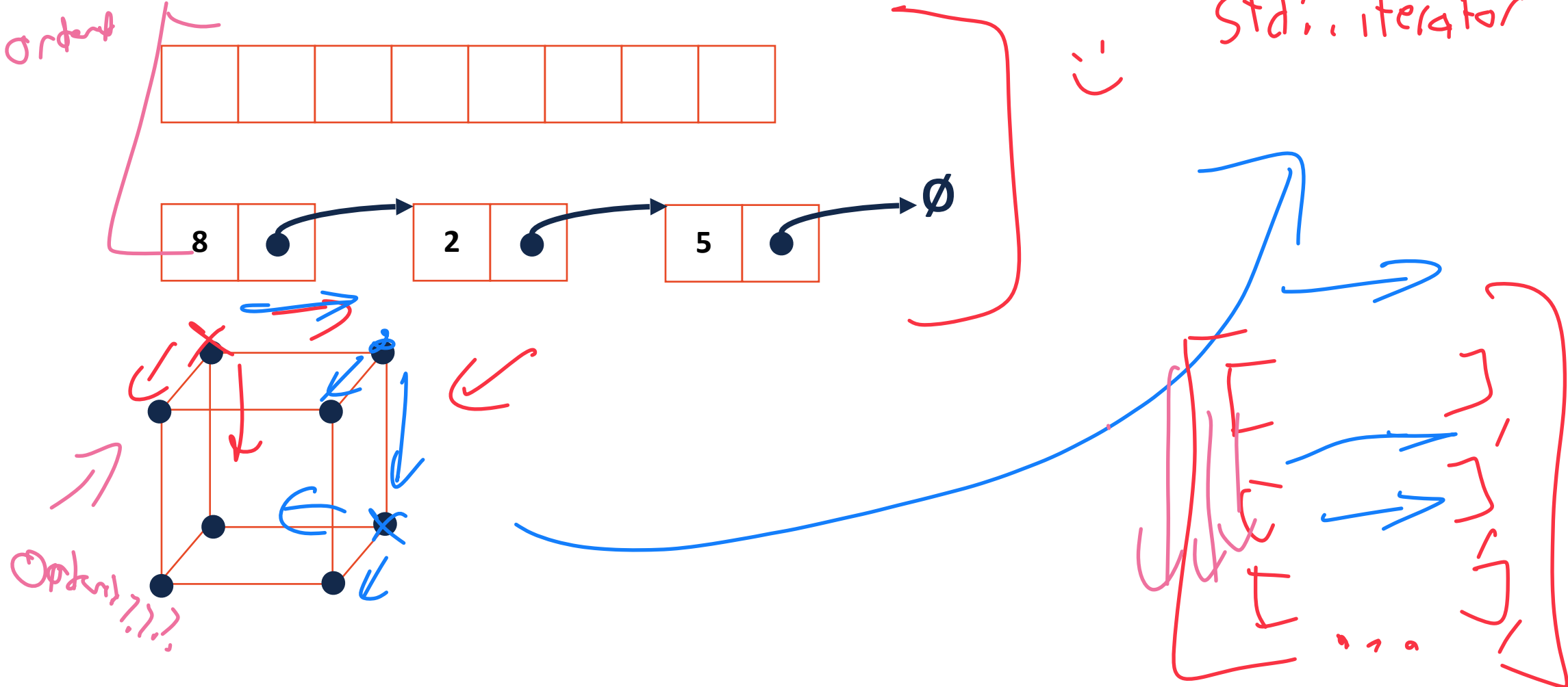
• [Order]: First in first out FIFO

• [Implementation]: LL w/ head and tail  
Circular array list\*  
↳ worst case for array is  $O(n)$

• [Runtime]: Enqueue  
Dequeue  
 $O(1)$ \*  
b/c resize

# Iterators

We want to be able to loop through all elements for any underlying implementation in a systematic way



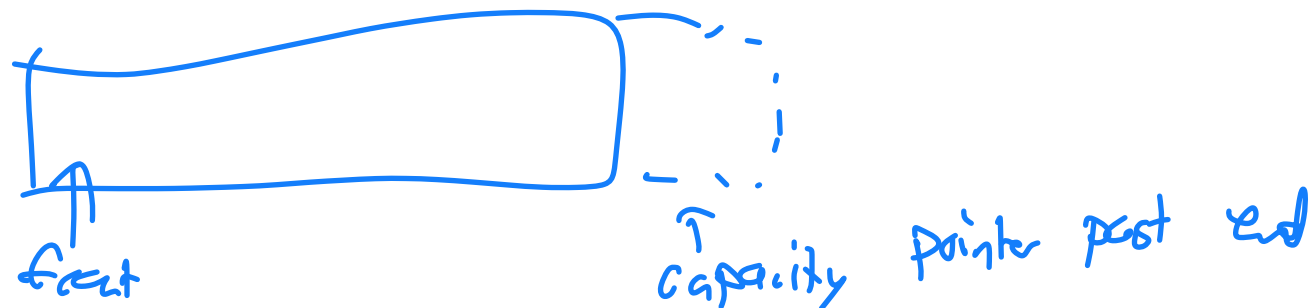


# Iterators <sup>list</sup>

For a class to implement an iterator, it needs two functions:

Iterator **begin()** - iterator points at start (my first element)

**end()** - returns  $\uparrow$  past the end of my data structure



# Iterators

class List  
private  
linked list

The actual iterator is defined as a class **inside** the outer class:

1. It must be of base class **std::iterator** (std::vector)

2. It must implement at least the following operations:

Iterator& operator ++() - pre-increment (point to next object)

const T & operator \*() - de-reference

bool operator !=(const Iterator &) - check if two iterators - pointers are same



# Iterators

This is truncated code *iter, ++*

Future assignments will have you write custom iterators:

```

1 template <class T>
2 class List {
3
4     class ListIterator : public
5     std::iterator<std::bidirectional_iterator_tag, T> {
6     public:
7
8         ListIterator& operator++();
9         ListIterator& operator--();
10
11         bool operator!=(const ListIterator& rhs);
12
13         const T& operator*();
14     };
15
16     ListIterator begin() const;
17
18     ListIterator end() const;
19 };

```

*built-in overloads  
ops in inner class*

*Array[+4 i]  
↑  
increments before*

*getters in main class  
array[i++]  
↑  
look up i, get the increment*

```
1 #include <list>
2 #include <string>
3 #include <iostream>
4
5 struct Animal {
6     std::string name, food;
7     bool big;
8     Animal(std::string name = "blob", std::string food = "you", bool big = true) :
9         name(name), food(food), big(big) { /* nothing */ }
10 };
11
12 int main() {
13     Animal g("giraffe", "leaves", true), p("penguin", "fish", false), b("bear");
14     std::vector<Animal> zoo;
15
16     zoo.push_back(g);
17     zoo.push_back(p); // std::vector's insertAtEnd
18     zoo.push_back(b);
19
20     for ( std::vector<Animal>::iterator it = zoo.begin(); it != zoo.end(); ++it ) {
21         std::cout << (*it).name << " " << (*it).food << std::endl;
22     }
23
24     return 0;
25 }
```

*Handwritten notes:*

- A blue bracket on the right side of the code, spanning from line 5 to line 10, indicates the scope of the `Animal` struct definition.
- A blue underline under `std::vector<Animal> zoo;` on line 14.
- A blue bracket under `std::vector<Animal>::iterator` on line 20.
- A red arrow points from the handwritten note `List<T>::ListIterator` to the `it` variable on line 20.
- A red arrow points from the handwritten note `it` to the `it` variable on line 20.
- A blue bracket on the right side of the code, spanning from line 20 to line 22, indicates the scope of the `for` loop.



```
1
2 std::vector<Animal> zoo;
3
4
5 /* Full text snippet */
6
7 for ( std::vector<Animal>::iterator it = zoo.begin(); it != zoo.end(); ++it ) {
8     std::cout << (*it).name << " " << (*it).food << std::endl;
9 }
10
11
12 /* Auto Snippet */
13
14 for ( auto it = zoo.begin(); it != zoo.end(); ++it ) {
15     std::cout << animal.name << " " << animal.food << std::endl;
16 }
17
18 /* For Each Snippet */
19
20 for ( const Animal & animal : zoo ) {
21     std::cout << animal.name << " " << animal.food << std::endl;
22 }
23
24
25
```

*for each animal in zoo*  
*cast Animal*

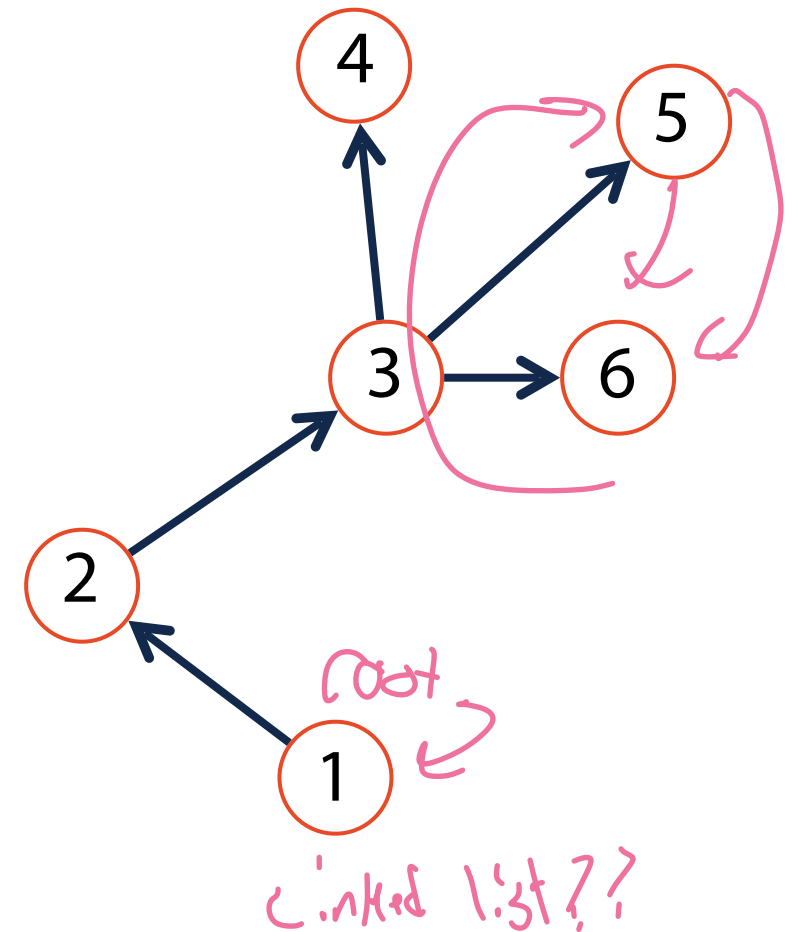
# Trees

A non-linear data structure defined recursively as a collection of nodes where each node contains a value and zero or more connected nodes.

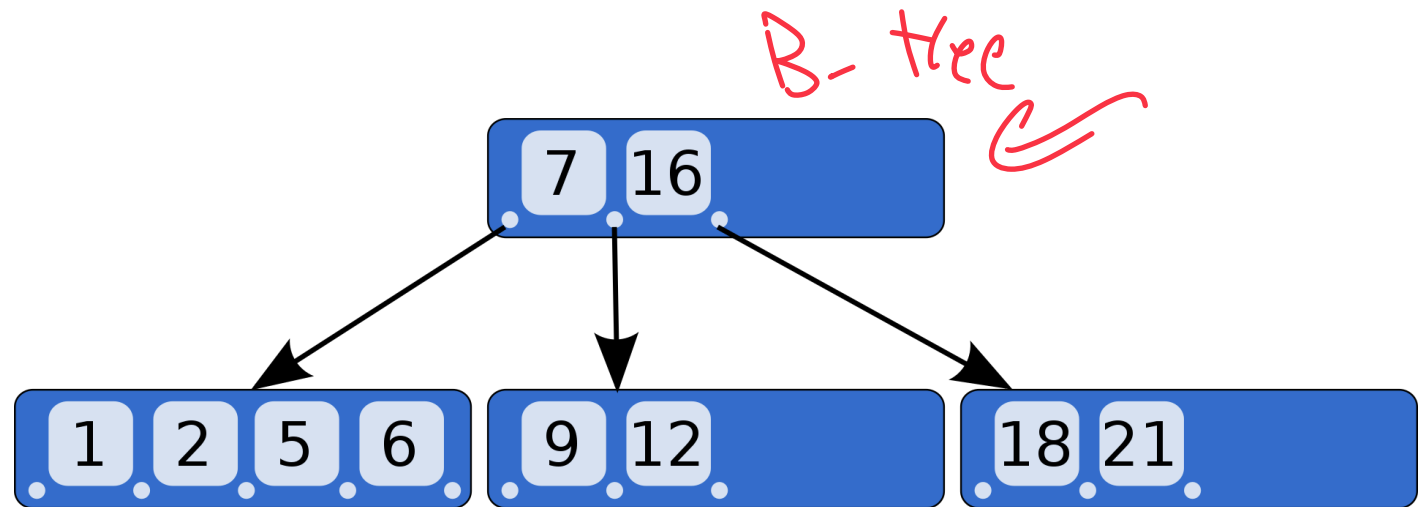
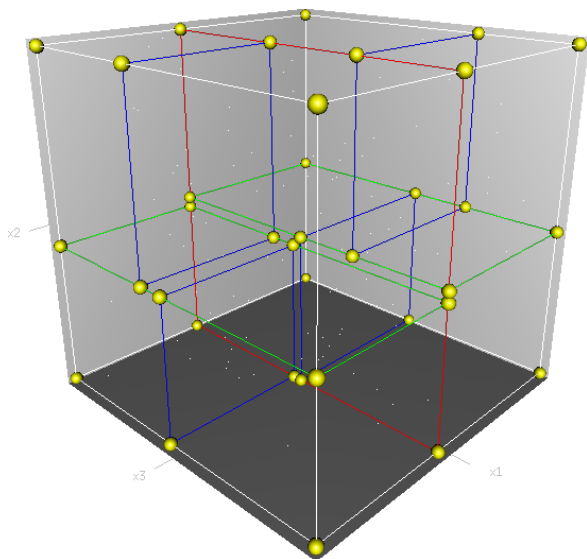
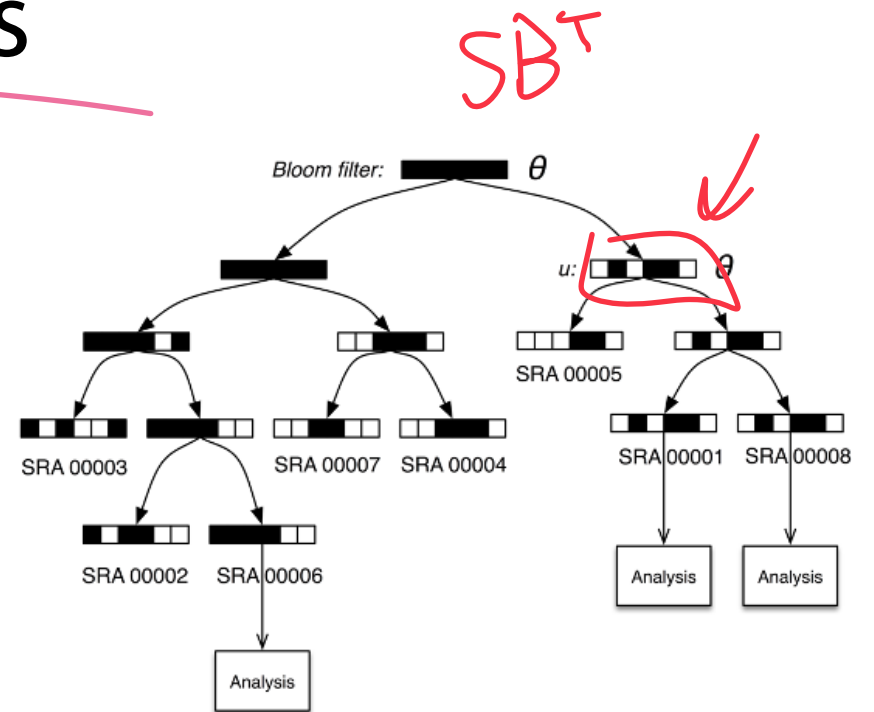
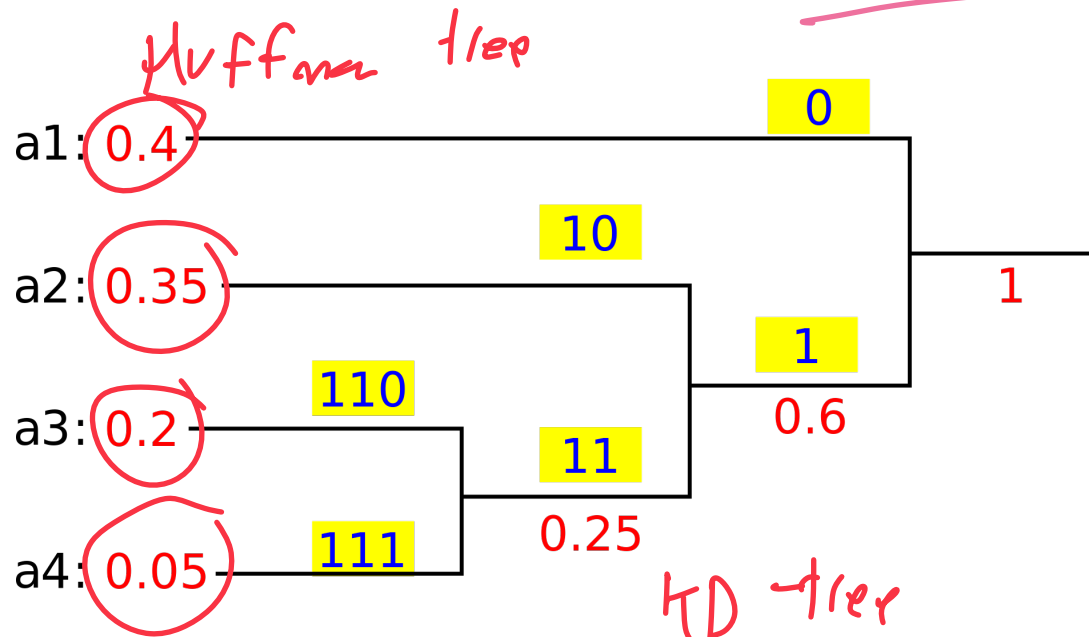
↳ Key, value

[In CS 225] a tree is also:

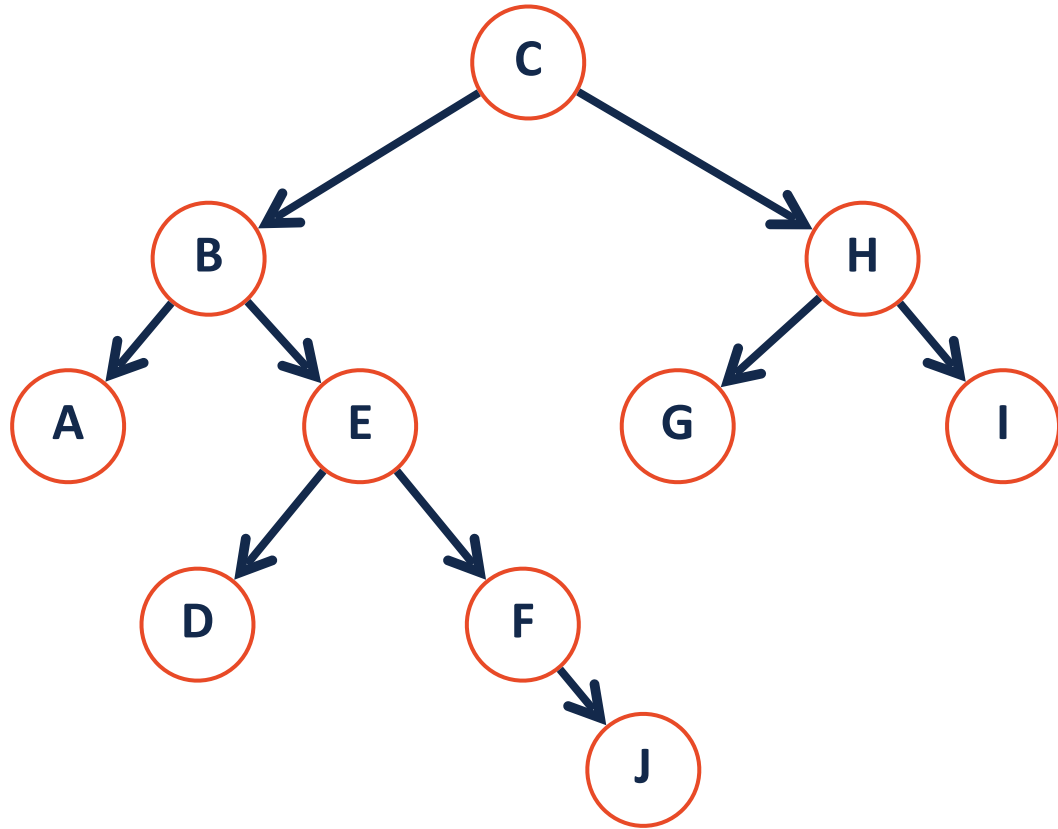
- 1) acyclic - has no cycles  
has no path from node to itself
- 2) rooted - has a root  
↳ Define some node to be root



# There are many *types* of trees



# Tree Terminology



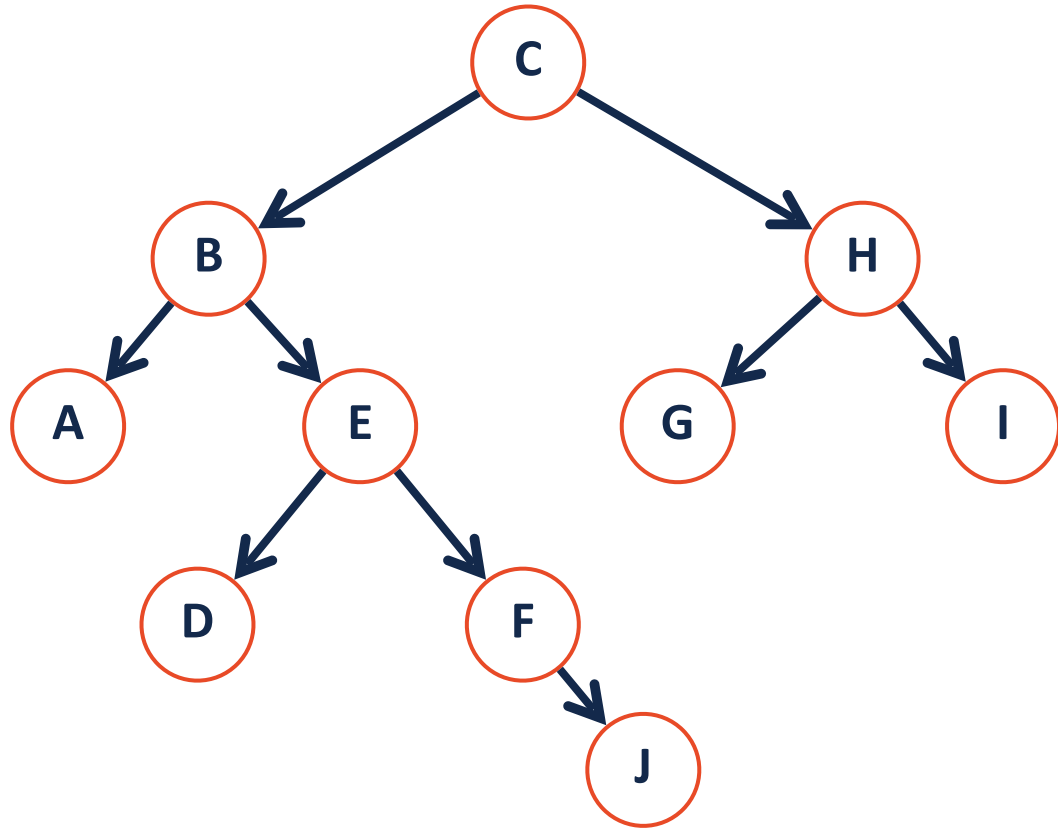
**Node:** The vertex of a tree

**Edge:** The connecting path between nodes

**Path:** A list of the edges (or nodes) traversed to go from node *start* to node *end*



# Tree Terminology



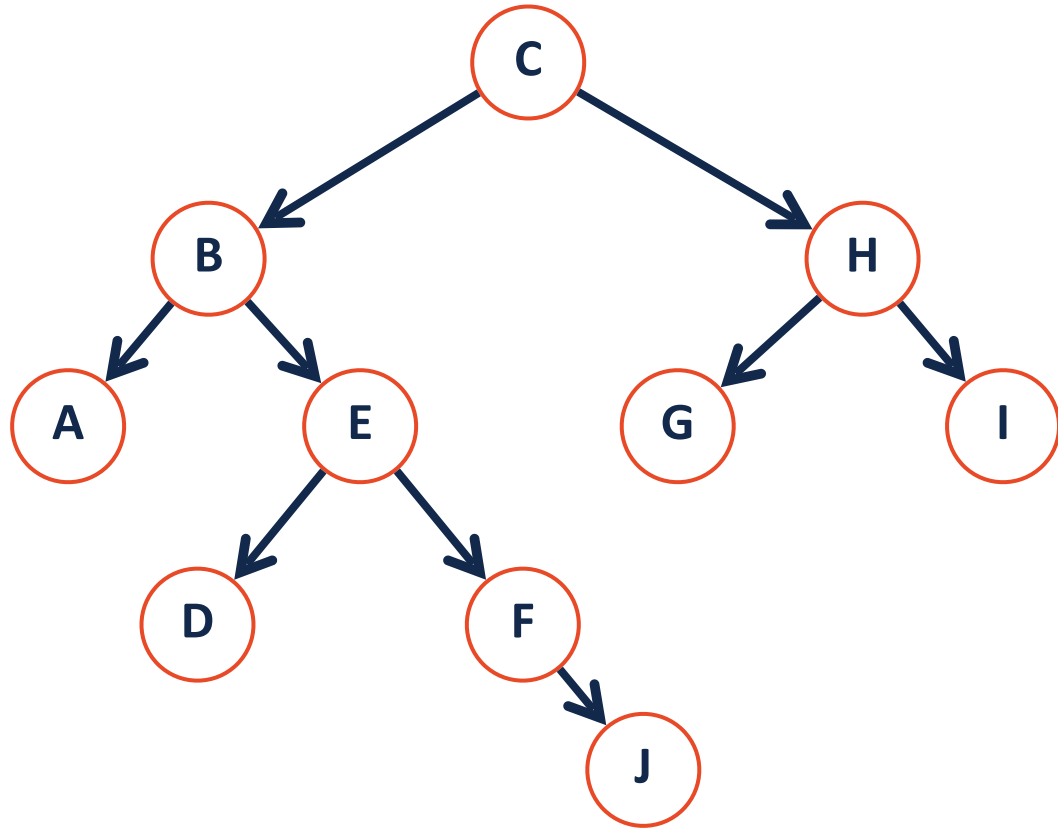
**Parent:** The precursor node to the current node is the 'parent'

**Child:** The nodes linked by the current node are its 'children'

**Neighbor:** Parent or child

**Degree:** The number of children for a given node

# Tree Terminology



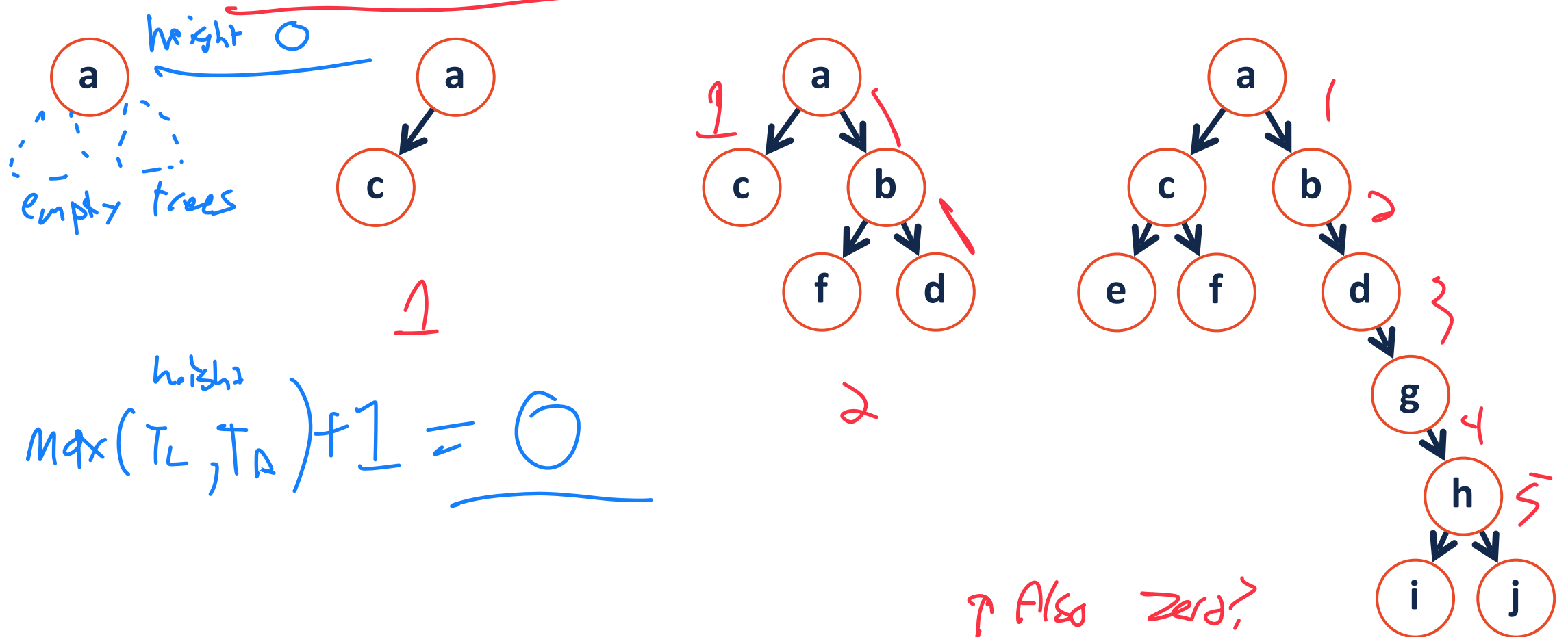
**Root:** The start of a tree (the only node with no parent).

**Leaf:** The terminating nodes of a tree (have no children)

**Internal:** A node with at least one child

# Tree Terminology

**Height:** the length of the longest path from the root to a leaf



$$\max(T_L, T_R) + 1 = 0$$

Also zero?

What is the height of a tree with **zero** nodes?

# Tree Height

**height(T) =**

**Base Case:**

$$\text{height}(\text{empty}) = -1$$

**Recursive Step:**

get height( $T_L$ ) & height( $T_R$ )

**Combining:**

$$\max[\text{height}(T_L), \text{height}(T_R)] + 1$$



height = 0



Binary Tree

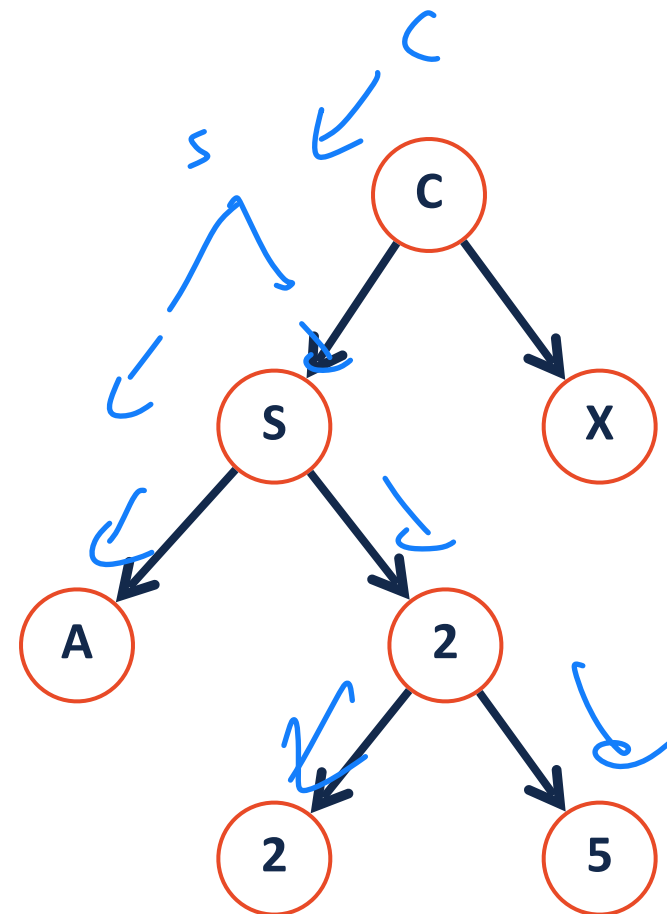
↳ root = null

# Binary Tree

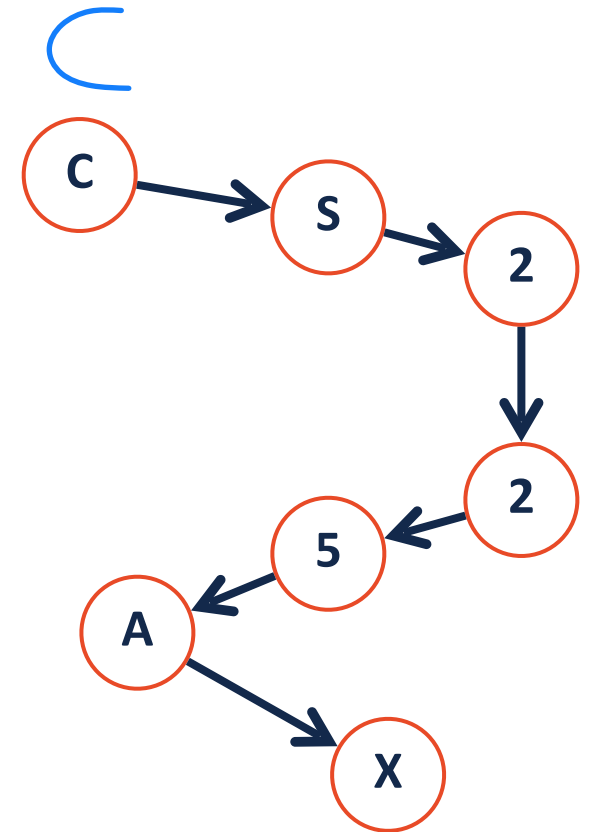
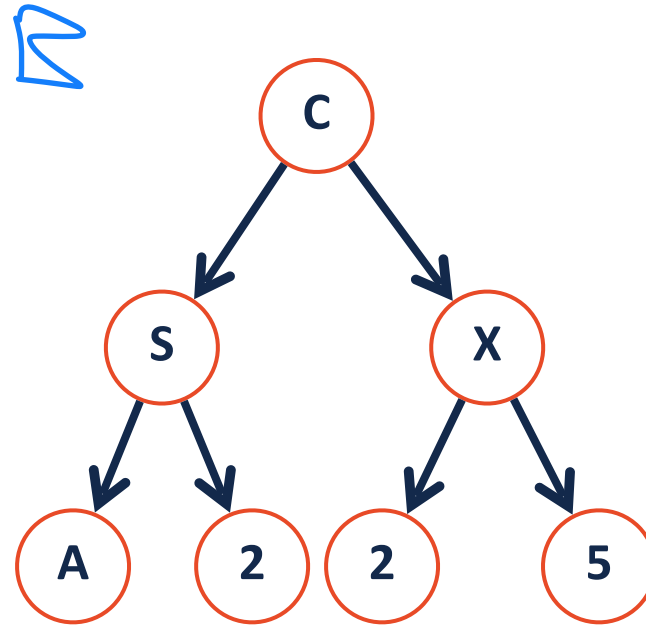
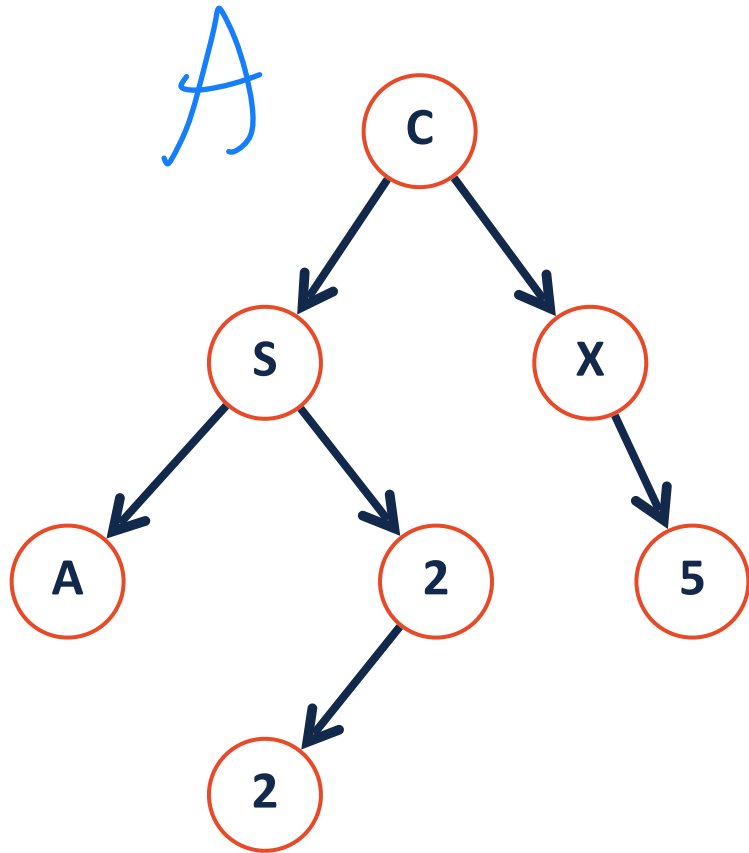
A **binary tree** is a tree  $T$  such that:

1.  $T = \text{null } (\emptyset)$

2.  $T = (\text{data}, T_L, T_R)$



# Which of the following are binary trees?



# Binary Tree

*E added here*

Lets define additional terminology for different **types** of binary trees!

1.

2.

3.

# Binary Tree: full

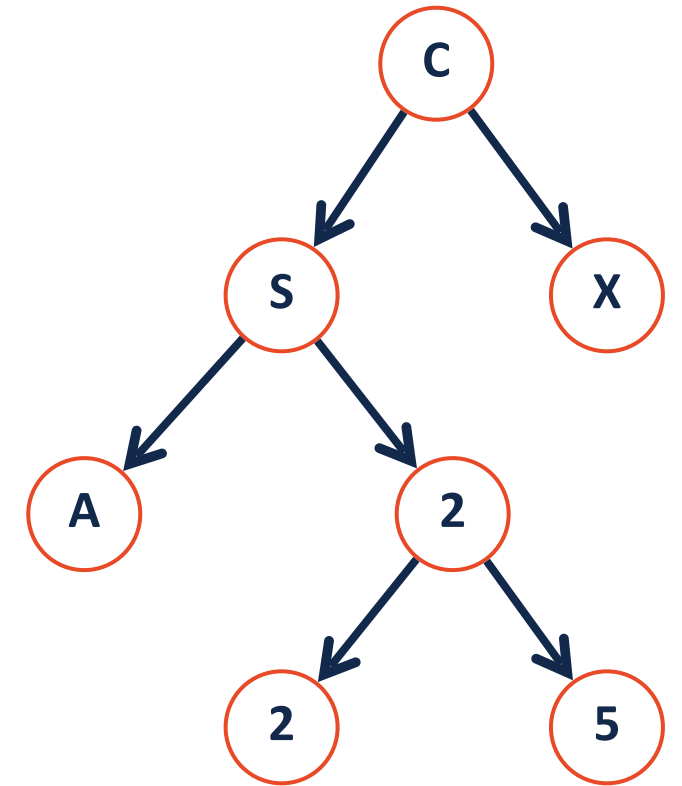
A **full tree** is a binary tree where every node has either 0 or 2 children

A tree **F** is **full** if and only if:

1.

2.

3.





# Binary Tree: perfect

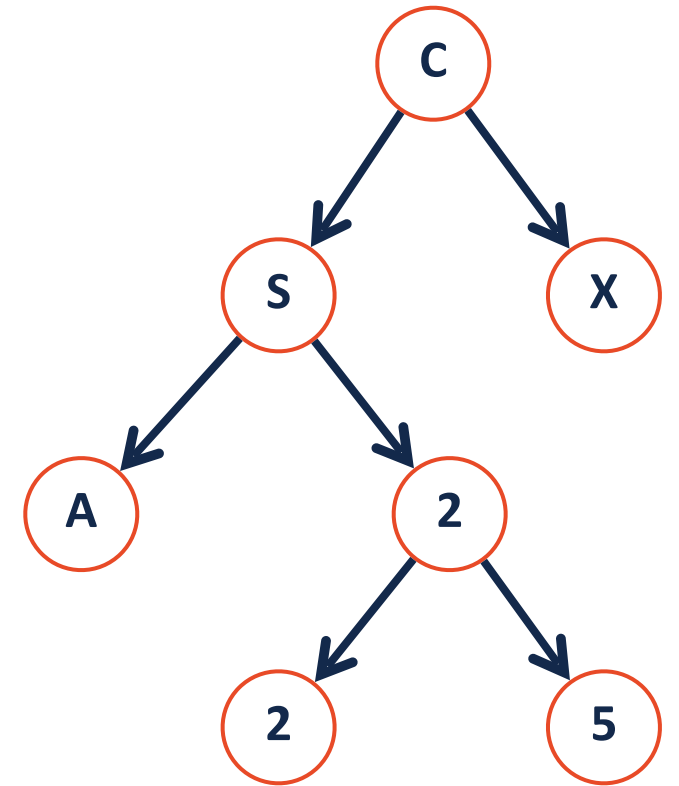
A **perfect tree** is a binary tree where...

Every internal node has 2 children and all leaves are at the same level.

A tree **P** is **perfect** if and only if:

1.

2.



# Binary Tree: complete

A **complete tree** is a B.T. where...

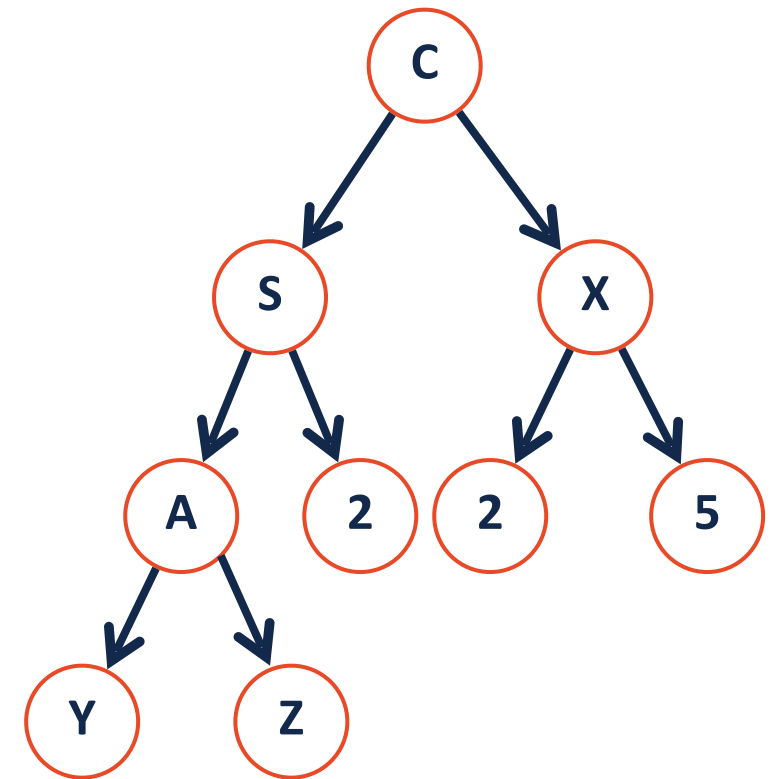
All levels are completely filled except the last (which is pushed to left)

A tree **C** is **complete** if and only if:

1.

2.

3.



# Binary Tree



Why do we care?

1. Terminology instantly defines a particular tree structure
2. Understanding how to think 'recursively' is very important.

# Binary Tree: Thinking with Types

Is every **full** tree **complete**?

Is every **complete** tree **full**?



For next time: Tree ADT and BinaryTree implementation