

#31: Bloom Filters

A bloom filter consists of:

1.

2.

Bloom Filter: Insertion

Example: $S = \{ 16, 8, 4, 13, 29, 11, 22 \}, |S| = n$ h(k) = k % 7, |Array| = N

[0]	
[1]	
[2]	
[3]	
[4]	
[5]	
[6]	

Bloom Filter: Deletion

Bloom filters do not support the deletion operation because:

Bloom Filter: Search

With h(k) = k % 7, find(16), find(20), find(3)

[0]	0
[1]	1
[2]	1
[3]	0
[4]	1
[5]	0
[6]	1

Probabilistic Accuracy

What are the four possible outcomes for a probabilistic function?

1.

2.

3.

4.

Which outcome can a bloom filter NOT have?

Bloom Filter: Repeated Trial Insertion

Example: $S = \{ 16, 8, 4, 13, 29, 11, 22 \}$ $h_1(x) = x \% 10, h_2(x) = 2x \% 10, h_3(x) = (5+3x) \% 10$

Given k hashes and a bit vector of length m, what is the run time for insert and find:

False Positive Rate

What is the expected false positive rate in terms of k (hashes), m (bit vector length), and n (number of inserted items)?

Optimal Bloom Filters

What equation describes the relationship between m bits, n items, and k hashes for an optimal bloom filter?

Combining bloom filters

Given the following bloom filters, write a bloom filter which 'contains' all the items present in both filters.

[0]	0	[0]	0	[0]	
[1]	1	[1]	1	[1]	
[2]	1	[2]	O	[2]	
[3]	0	[3]	0	[3]	
[4]	1	[4]	1	[4]	
[5]	0	[5]	1	[5]	
[6]	O	[6]	O	[6]	

Given the same bit vectors, write a filter which 'contains' only items that are present in both filters.