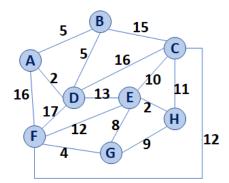


| *38: MSTs: Kruskai + Priii s Aigurum | November 30, 2018 · Wade Fagen-Ulmschneider

Kruskal's Algorithm



(A, D)
(E, H)
(F, G)
(A, B)
(B, D)
(G, E)
(G, H)
(E, C)
(C, H)
(E, F)
(F, C)
(D, E)
(B, C)
(C, D)
(A, F)
(D, F)

```
Pseudocode for Kruskal's MST Algorithm
   KruskalMST(G):
2
     DisjointSets forest
      foreach (Vertex v : G):
        forest.makeSet(v)
5
     PriorityQueue Q
                         // min edge weight
      foreach (Edge e : G):
8
        Q.insert(e)
9
10
     Graph T = (V, \{\})
11
12
     while |T.edges()| < n-1:
13
       Vertex (u, v) = Q.removeMin()
14
        if forest.find(u) == forest.find(v):
15
           T.addEdge(u, v)
16
           forest.union( forest.find(u),
17
                         forest.find(v) )
18
19
      return T
```

Kruskal's Running Time Analysis

We have multiple choices on which underlying data structure to use to build the Priority Queue used in Kruskal's Algorithm:

Priority Queue Implementations:	Неар	Sorted Array
Building : 6-8		
Each removeMin :13		

Based on our algorithm choice:

Priority Queue	m · lp · m
Implementation:	Total Running Time
Неар	
Sorted Array	

Reflections

Why would we prefer a Heap?

Why would be prefer a Sorted Array?

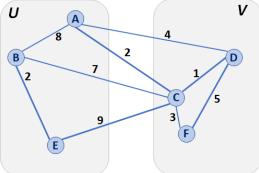
Partition Property

Consider an arbitrary partition of the vertices on G into two subsets U and **V**.

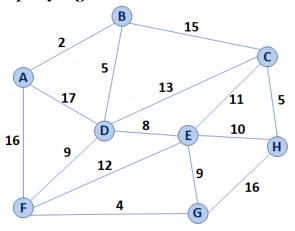
Let **e** be an edge of minimum weight across the partition.

Then **e** is part of some minimum spanning tree.

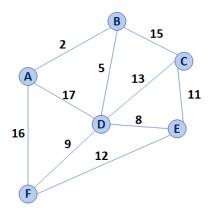
Proof in CS 374!



Partition Property Algorithm



Prim's Minimum Spanning Tree Algorithm



	Adj. Matrix	Adj. List
Неар		
Unsorted Array		

```
Pseudocode for Prim's MST Algorithm
    PrimMST(G, s):
 2
      Input: G, Graph;
 3
             s, vertex in G, starting vertex of algorithm
      Output: T, a minimum spanning tree (MST) of G
 5
 6
      foreach (Vertex v : G):
        d[v] = +inf
        p[v] = NULL
 9
      d[s] = 0
10
11
      PriorityQueue Q // min distance, defined by d[v]
      Q.buildHeap(G.vertices())
12
13
      Graph T
                        // "labeled set"
14
      repeat n times:
15
16
        Vertex m = Q.removeMin()
17
        T.add(m)
18
        foreach (Vertex v : neighbors of m not in T):
19
          if cost(v, m) < d[v]:
20
            d[v] = cost(v, m)
21
            p[v] = m
22
23
      return T
```

Running Time of MST Algorithms

Kruskal's Algorithm:

Prim's Algorithm:

Q: What must be true about the connectivity of a graph when running an MST algorithm?

...what does this imply about the relationship between \mathbf{n} and \mathbf{m} ?

CS 225 - Things To Be Doing:

- 1. Programming Exam C is different than usual schedule: Exam: Sunday, Dec 2 – Tuesday, Dec 4
- 2. MP7 Released Slightly different structure: Hard Deadline on Monday, Dec. 3 for Part 1
- 3. lab_ml in lab this week!
- 4. Daily POTDs are ongoing for +1 point /problem