CS 173 Discussion 12: Counting

Date: November 13/14, 2019.

Problem 1. How many positive integers between 100 and 999 inclusive

- 1. are multiples of 7?
- $2. \ {\rm are \ odd}?$
- 3. have the same three decimal digits?
- 4. are not divisible by 4?
- 5. are divisible by 3 and 4?

Problem 2. A circular *r*-permutation of *n* people is a seating of *r* of these *n* people around a circular table, where seatings are considered to be the same if they can be obtained from each other by rotating the table. How many circular *r*-permutation of *n* people are there?

Problem 3. Call a positive integer *monotonous* if it is a one-digit number or its digits, when read from left to right, for either a strictly increasing or a strictly decreasing sequence. For example 3, 23578, and 987620 are monotonous, but 88, 7434, 7345, and 23557 are not. How many monotonous positive integers are there?