## CS 173, Fall 2015 Examlet 6, Part B

NETID:

FIRST:

## LAST:

## Discussion: $\begin{array}{llllllllllll} & \text { Thursday } & 2 & 3 & 4 & 5 & \text { Friday } & 9 & 10 & 11 & 12 & 1 \\ 2\end{array}$

1. (9 points) How many paths are there from Q to B in the graph below? Explain or show work.


Solution: There are four cases: the path goes through P and then R , through R and then P , just through P, or just through R. In each case, we must then go to T or Y. And then there are two choices of how to finish. So there are a total of 8 paths.
2. (3 points) How many connected components does the above graph have?

Solution: One connected component.
3. (3 points) Does the above graph have a cut edge? Briefly explain why or why not.

Solution: No, it does not. There is no edge that will break the graph into two pieces if you remove it, because every edge belongs to a cycle.

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1. ( 9 points) How many cycle subgraphs (i.e. subgraphs isomorphic to $C_{n}$ for some $n$ ) does the graph below contain? Count two cycles as the same if they have the same set of nodes; don't worry about (for example) which node is the start/end node. Briefly justify and/or show work.


Solution: Six. One is BCFQED. A second is AHQK. Then there are four cycles that choose one of the upper paths from A to Q (AFDEQ or ABCFQ) followed by one of the lower paths from Q to A (QHA or QKA).
2. (3 points) What is the diameter of this graph?

Solution: 3. For exmaple, A and E are three edges apart.
3. (3 points) Is this graph bipartite? Briefly justify your answer.

Solution: Yes, it is bipartite. Put B, E, F, H, K, and A, C, D, Q into the other group. Then all the edges link nodes from different groups.

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1. (9 points) How many paths are there from A to Q in the graph below? Explain or show work.


Solution: There is one path along the lower route (via K ).
Along the upper route, there are two ways to get from A to B , then four ways to get from C to Q .
So there are eight options along the upper route.
So there are $8+1=9$ paths total.
2. (3 points) Does this graph contain a 6-node cycle? Briefly justify your answer

Solution: Yes, the cycle A, B, C, F, Q, K.
3. (3 points) Does the above graph have a cut edge? Briefly explain why or why not.

Solution: Yes. The edge QM is a cut edge.

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1. (9 points) How many paths are there from A to B in the graph below? Explain or show work.


Solution: There are 4 paths from A to R. Then there are 3 paths from R to T. And 5 paths from T to B. So there are $4 \cdot 3 \cdot 5=60$ paths total.
2. (3 points) How many connected components does the above graph have?

Solution: One connected component.
3. (3 points) Does this graph contain a 4-node cycle? Briefly justify your answer Solution: Yes, the cycle APRQ for example.

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1. (9 points) How many paths are there from $Q$ to $L$ in the graph below? Explain or show work.


Solution: There are three paths from Q to H. Then four paths from H to L. So 12 paths total.
2. (3 points) How many connected components does the above graph have?

Solution: This graph has two connected components
3. (3 points) Is this graph bipartite? Briefly justify your answer.

Solution: No. It contains triangles such as B, C, D.

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1. (9 points) How many paths are there from a to h in the graph below? Explain or show work.


Solution: There are five paths from a to e: ae, abe, ade, adbe, abde. We must then to go k . Then we have the choice of goign through c or not. So $5 \cdot 2=10$ paths total.
2. (3 points) Does this graph have an Euler circuit? Briefly explain why or why not.

Solution: No. Some of the nodes have odd degree.
3. (3 points) Does the above graph have a cut edge? Briefly explain why or why not.

Solution: Yes. ek is a cut edge (also other edges like fk).

