

**CS 173, Fall 2015**  
**Examlet 4, Part B**

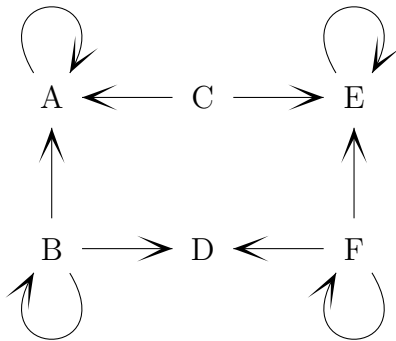
NETID:

FIRST:

LAST:

Discussion:    Thursday    2    3    4    5    Friday    9    10    11    12    1    2

1. (5 points) Check all boxes that correctly characterize this relation on the set  $\{A, B, C, D, E, F\}$ .



Reflexive:     Irreflexive:

Symmetric:     Antisymmetric:

Transitive:

2. (5 points) Suppose that  $R$  is a partial order on a set  $A$ . What additional property is required for  $R$  to be a linear order (aka total order)? Give specific details of the property, not just its name.

3. (5 points) Recall that  $\mathbb{N}^2$  is the set of all pairs of natural numbers. Let's define the equivalence relation  $\sim$  on  $\mathbb{N}^2$  as follows:  $(x, y) \sim (p, q)$  if and only if  $|x - y| = |p - q|$ . List three members of  $[(2, 3)]$ .

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A

C

E

Reflexive:

Irreflexive:

(that is, 6 nodes  
and no arrows  
at all)

Symmetric:

Antisymmetric:

B

D

F

Transitive:

2. (5 points) Suppose that  $R$  is a relation on a set  $A$ . Using precise mathematical words and notation, define what it means for  $R$  to be transitive.

3. (5 points) Let  $T$  be the relation defined on set of pairs  $(x, y) \in \mathbb{R}^2$  such that  $(x, y)T(p, q)$  if and only if  $x \leq p$  or  $y \leq q$ . Is  $T$  transitive? Informally explain why it is, or give a concrete counter-example showing that it is not.

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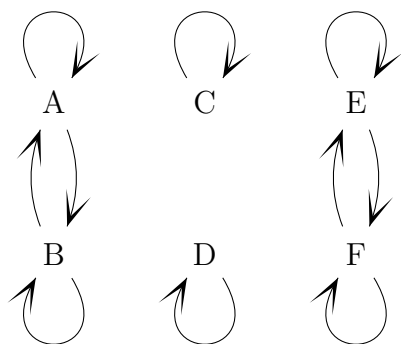
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1. (5 points) Check all boxes that correctly characterize this relation on the set  $\{A, B, C, D, E, F\}$ .



Reflexive:     Irreflexive:

Symmetric:     Antisymmetric:

Transitive:

2. (5 points) A relation is an equivalence relation if it has which three properties? (Naming the properties is sufficient. You don't have to define them.)

3. (5 points) Let  $T$  be the relation defined on set of pairs  $(x, y) \in \mathbb{R}^2$  such that  $(x, y)T(p, q)$  if and only if  $xp + yq = 0$ . Is  $T$  irreflexive? Informally explain why it is, or give a concrete counter-example showing that it is not.

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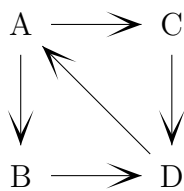
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1. (5 points) Check all boxes that correctly characterize this relation on the set  $\{A, B, C, D, E, F\}$ .



E

Reflexive:

Irreflexive:

Symmetric:

Antisymmetric:

F

Transitive:

2. (5 points) A relation is a strict partial order if it has which three properties? (Naming the properties is sufficient. You don't have to define them.)

3. (5 points) Let  $T$  be the relation defined on set of pairs  $(x, y) \in \mathbb{R}^2$  such that  $(x, y)T(p, q)$  if and only if  $x - p \leq y - q$ . Is  $T$  transitive? Informally explain why it is, or give a concrete counter-example showing that it is not.

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1. (5 points) Check all boxes that correctly characterize this relation on the set  $\{A, B, C, D, E, F\}$ .



Reflexive:     Irreflexive:

Symmetric:     Antisymmetric:

Transitive:

2. (5 points) Suppose that  $R$  is an equivalence relation on a set  $A$ . Using precise set notation, define  $[x]_R$ , i.e. the equivalence class of  $x$  under the relation  $R$ .

3. (5 points) Suppose that  $T$  is the relation on the set of integers such that  $aTb$  if and only if  $\gcd(a, b) = 3$ . Is  $T$  transitive? Informally explain why it is, or give a concrete counter-example showing that it is not.

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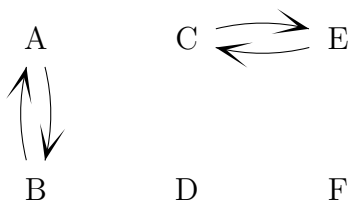
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1. (5 points) Check all boxes that correctly characterize this relation on the set  $\{A, B, C, D, E, F\}$ .



Reflexive:     Irreflexive:   
 Symmetric:     Antisymmetric:   
 Transitive:

2. (5 points) Can a relation be irreflexive, symmetric, and also transitive? Either give such a relation or briefly explain why it's not possible to construct one.
3. (5 points) Let  $\sim$  be the relation defined on set of pairs  $(x, y) \in \mathbb{R}^2$  such that  $(x, y) \sim (p, q)$  if and only if  $x^2 + y^2 = p^2 + q^2$ . Find three elements in the equivalence class  $[(0, 1)]$