

CS 173, Fall 2015
Examlet 3, Part A

NETID:

FIRST:

LAST:

Discussion: Thursday 2 3 4 5 Friday 9 10 11 12 1 2

$$A = \{(p, q) \in \mathbb{Z}^2 \mid 3pq + 15p - 5q - 25 \geq 0\}$$

$$B = \{(s, t) \in \mathbb{Z}^2 \mid t \geq 0\}$$

$$C = \{(x, y) \in \mathbb{Z}^2 \mid x \geq 0\}$$

Prove that $(A \cap B) \subseteq C$.

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$$A = \{\lambda(0, 3) + (1 - \lambda)(2, 4) \mid \lambda \in [0, 1]\}$$

$$B = \{(x, y) \in \mathbb{R}^2 \mid x \leq y\}$$

Prove that $A \subseteq B$.

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$$A = \{(x, y) \in \mathbb{R}^2 \mid y = x^2 - 3x + 2\}$$

$$B = \{(p, q) \in \mathbb{R}^2 \mid p \geq 0\}$$

$$C = \{(m, n) \in \mathbb{R}^2 \mid n \geq 1\}$$

Prove that $A \subseteq B \cup C$.

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$$A = \{(x, y) \in \mathbb{R}^2 \mid x = \lfloor 3y + 5 \rfloor\}$$

$$B = \{(p, q) \in \mathbb{Z}^2 \mid 2p + q \equiv 3 \pmod{7}\}$$

Prove that $A \cap \mathbb{Z}^2 \subseteq B$.

Use the following definition of congruence mod k : if s, t, k are integers, k positive, then $s \equiv t \pmod{k}$ if and only if $s = t + nk$ for some integer n .

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$$A = \{(p, q) \in \mathbb{R} \mid p = 0\}$$

$$B = \{(x, y) \in \mathbb{R} \mid (x - 1)^2 + y^2 = 4\}$$

$$C = \{(s, t) \in \mathbb{R} \mid (s + 1)^2 + t^2 = 4\}$$

Prove that $B \cap C \subseteq A$.

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$$A = \{\lambda(3, 2) + (1 - \lambda)(5, 0) \mid \lambda \in [0, 1]\}$$

$$B = \{(x, y) \in \mathbb{R}^2 \mid x \geq y\}$$

Prove that $A \subseteq B$.