## CS 173, Fall 2015 Examlet 11, Part B

## NETID:

FIRST:
Discussion: $\begin{array}{llllllllllll} & \text { Thursday } & 2 & 3 & 4 & 5 & \text { Friday } & 9 & 10 & 11 & 12 & 1\end{array} 2$
(6 points) Your partner has implemented the function Merge(A,B), which merges two sorted linked lists of integers. Using Merge, fill in the missing parts of this implementation of Mergesort.
$\operatorname{Mergesort}\left(L=\left(a_{1}, a_{2}, \ldots, a_{n}\right)\right) \quad \backslash \backslash$ input is a linked list L containing n integers


$$
\mathrm{p}=\text { floor }(\mathrm{n} / 2)
$$


(9 points) Check the (single) box that best characterizes each item.

$$
T(1)=d
$$

$$
\Theta(n) \quad \square \quad \Theta(n \log n) \quad \Theta\left(n^{2}\right) \quad \square
$$

$T(n)=4 T(n / 2)+n$

$$
\Theta\left(n^{\log _{3} 2}\right) \quad \square \quad \Theta\left(n^{\log _{2} 3}\right) \quad \square \quad \Theta\left(2^{n}\right) \quad \square
$$

The Towers of Hanoi puzzle can be solved in polynomial time.
proven true $\square$ proven false $\quad \square$ not known $\square$

Merging two sorted lists

$$
\Theta(\log n) \quad \Theta(n) \quad \square
$$

$$
\Theta(n \log n) \quad \Theta\left(n^{2}\right) \quad \square
$$

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(15 points) Check the (single) box that best characterizes each item.
$T(1)=d$
$T(n)=2 T(n-1)+c$
$\Theta(n) \quad \Theta\left(n^{2}\right) \quad \square$
$\Theta(n \log n) \quad \Theta\left(2^{n}\right)$

Circuit satisfiability can be solved in polynomial time.
proven true $\quad \square$ proven false $\quad \square$ not known $\square$

The running time of the Towers of Hanoi solver $\Theta(\log n) \quad \square \Theta(n \log n) \quad \square \quad \Theta\left(n^{2}\right) \quad \square \Theta\left(2^{n}\right) \quad \square$
$T(1)=d$
$T(n)=T(n-1)+c$
$\Theta(n) \quad \Theta\left(n^{2}\right) \quad \square$
$\Theta(n \log n)$ $\square$ $\Theta\left(2^{n}\right)$ $\square$

The running time of Karatsuba's algorithm is recursively defined by $T(1)=d$ and $T(n)=$

$$
\begin{array}{llll}
2 T(n / 2)+c n & \square & 3 T(n / 2)+c n & \square \\
4 T(n / 2)+c n & \square & 4 T(n / 2)+c & \square
\end{array}
$$

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(15 points) Check the (single) box that best characterizes each item.

| $\Theta\left(n^{2}\right)$ | $\square$ | $\Theta\left(n^{3}\right)$ | $\square$ | $\Theta(n \log n)$ |
| :--- | :--- | :--- | :--- | :--- |
| $\Theta\left(n^{\log _{2} 3}\right)$ | $\square$ | $\Theta\left(n^{\log _{3} 2}\right)$ | $\square$ | $\Theta\left(2^{n}\right)$ |

The running time of binary search is recur-

| $T(n / 2)+c$ | $\square$ | $T(n / 2)+c n$ |
| ---: | ---: | ---: |
| $2 T(n / 2)+c$ | $\square$ |  |
| $2 T(n / 2)+c n$ | $\square$ |  |

If a yes/no problem is in NP, a "yes" answer always has a succinct justification.
true $\square$ false $\square$ not known $\square$

Algorithm A takes $n^{5}$ time. On one input, A takes x time. How long will it take if I double the input size?

Problems in class P (as in P vs. NP) require exponential time
never $\square \quad$ sometimes $\square$ always $\square$ not known $\square$

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(15 points) Check the (single) box that best characterizes each item.

The running time of the Towers of Hanoi solver is recursively defined by $T(1)=d$ and $T(n)=$

$$
\begin{array}{rlll}
2 T(n-1)+c & \square & 2 T(n-1)+c n & \square \\
2 T(n / 2)+c & \square & 2 T(n / 2)+c n & \square
\end{array}
$$

If a yes/no problem is in co-NP, a "no" answer always has a succinct justification. true
 not known $\square$

The running time of the Towers of Hanoi solver

$$
\begin{array}{lll}
\Theta(\log n) & \square & \Theta(n \log n) \\
& \\
\text { n one } \\
\text { g will } \\
\text { e? } & 2 x & \square
\end{array} 2^{x} \boxed{\square} \quad x^{2} \quad \square
$$ it take if I double the input size?

Finding the chromatic number of a graph with $n$ nodes requires $\Theta\left(2^{n}\right)$ time.


Algorithm A takes $2^{n}$ time. On one input, A takes x time. How long will

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(6 points) Fill in the missing bits of this recursive algorithm for returning the location of a number $k$ in a sorted list of numbers $a_{p}, a_{2}, \ldots, a_{q}$.

$$
\operatorname{search}(\mathrm{p}, \mathrm{q}, \mathrm{k}) \quad \backslash \backslash \quad \text { assume } p \leq q
$$

$m:=\lfloor(p+q) / 2\rfloor$
if $k=a_{m}$ then return m
else if $\left(k<a_{m}\right)$ and $p<m$ then
$\square$
else if $\left(k>a_{m}\right)$ and $q>m$ then
$\square$
else return-1 <br>i.e. error, not found
(9 points) Check the (single) box that best characterizes each item.

It takes exponential time to determine whether a propositional logic expression can be made true by picking the right true/false values for its propositional variables (e.g. p, q, r).


The running time of mergesort is $O\left(n^{3}\right)$.

$n^{\log _{2} 3}$ grows

$$
\text { faster than } n^{2} \quad \square
$$

$$
\text { slower than } n^{2}
$$

$\square$
$\square$

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(6 points) Fill in the missing bits of the recursive algorithm for solving the Towers of Hanoi puzzle.
hanoi $\left(A, B, C\right.$ : pegs, $d_{1}, d_{2} \ldots d_{n}$ : disks) $\backslash \backslash$ move n disks from peg A to peg B
if $(n=1)$ move $d_{1}$ from $A$ to $B$
else

move $d_{n}$ from $A$ to $B$
(9 points) Check the (single) box that best characterizes each item.

Determining whether a graph with $n$ edges is connected.
polynomial $\square$
exponential $\square$
in NP $\square$

The running time of mergesort is recursively defined by $T(1)=d$ and $T(n)=$

$$
\begin{array}{rrr}
2 T(n-1)+c & \square & 2 T(n-1)+c n \\
2 T(n / 2)+c & \square & 2 T(n / 2)+c n \\
\hline
\end{array}
$$

The running time of binary search

$$
\Theta(\log n) \quad \square
$$

$\Theta(n) \square$
$\Theta(n \log n) \quad \square$
$\Theta\left(n^{2}\right) \quad \square$

