Final Examination
CS 125 Introduction to Computer Science
Spring 2008
3 Hours

Name: ____________________________
Last, First

NetID: _ _ _ _ _ _ _ @ uiuc.edu

PLEASE READ THE FOLLOWING CAREFULLY
• This is a closed book and closed notes exam.
• You are not allowed to use the break, continue, or switch statements on this exam. Furthermore, you cannot use loops in any problem unless we specifically say that you can.
• Unless we say otherwise in the specific problem, you can assume all values entered by the user will be acceptable input for that program.
• When you write code, you may use a shorthand for System.out and TextIO input and output methods provided it is obvious to the graders which method you are using. For example it is acceptable to use Sopln in place of System.out.println and to use Sopt in place of System.out.print Likewise, you can use T.rln(), T.rlnC(), and T.rlnD() in place of TextIO.readlnInt(), TextIO.readlnChar(), and TextIO.readlnDouble().
• For full marks correct syntax is required: Ensure all statements include a semicolon and the correct use of upper/lower case, single quotes and double quotes.

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<tr>
<th>Problem</th>
<th>Points</th>
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1. Guess my number – 6 points.

HAL and Arthur are playing a simple 'guess my number' game:

HAL: "I'm thinking of a integer between 1 and 1000 inclusive"
Arthur: "Is it 500?"
HAL: "No, go lower"
Arthur "Is it 250?"
HAL: "No, go higher"
Arthur "Is it 375?"
HAL: "Yes"

For the following questions:
- The problem size, 'N' is the number of integers that HAL claims must be considered at the start of the game (i.e. N=1000 in the dialog above).
- Use Big-O notation for your answer e.g. O(n²). You only need to write the order of growth; you do NOT need to explain how you got your answer.

Q. #1 HAL chooses an unknown integer apparently at random so Arthur uses an intelligent divide and conquer strategy to minimize the number of guesses required. Determine the order of growth for the worst case: How does the time required to discover HAL's answer increase as the initial number of possible answers increases?

Q. #2. What is the best case order of growth running time for the same scenario described in Q1? Use big-O notation.

Q. #3 Later HAL changes the rules and responds with just "No, that's not my number" or "Yes". Arthur modifies his algorithm to run optimally given HAL's uncooperative responses. Determine the worst case running time of Arthur's algorithm.
2. Recursive Thesaurus – 14 points (8+6).

a) You want to recursively search an array of words. The words are randomly ordered. Write a recursive class method named 'find' that has three parameters: an array of strings 'arr', the search string 's' and an integer starting array index 'lo'. The method returns the integer array index of 's' or -1 if the search word is not found. You may not use loops. Assume that all object references are valid i.e. there no null references.

b) Complete the order-of-growth for the worst case running time for each algorithm.

```java
public static boolean isUniqueA(int[] arr) { // N = arr.length
    for(int i = 0; i < arr.length - 1; i++)
        for(int j = i + 1; j < arr.length; j++)
            if (arr[i] == arr[j])
                return false;
    return true;
}

public static boolean isUniqueB(int[] arr) { // N = arr.length
    for(int i = 0; i < arr.length - 1; i++)
        if (arr[i] == arr[i + 1])
            return false;
    return true;
}
```

If there no duplicate values then `isUniqueA & isUniqueB` must return true i.e. the array values are all unique. However these algorithms make different assumptions about the ordering of the data. If you know that your integer array is already sorted in descending order, which one of the following accurately describes a Computer Scientist's choice of algorithm to check for duplicate values?

A. Use `isUniqueA` because `isUniqueB` will be slower.
B. Use `isUniqueA` because `isUniqueB` may not find duplicates.
C. Use `isUniqueB` because `isUniqueA` will be slower.
D. Use `isUniqueB` because `isUniqueA` may not find duplicates.
E. Neither algorithm will function correctly.

Your Answer: ______________
3. Recursive lip reading – 14 points (6+6+2).

To lip-read, HAL encodes mouth, tongue and lip movements of human speech using decimal digits. Write a recursive class method 'digits' that takes a single positive integer parameter and returns the sum of digits that are less than 4 (other digits contribute zero) of the parameter. Your method may not use any loops. Examples: digits(2340) returns 5; digits(9876543211) returns 7 (1+1+2+3). Hint: % operator and integer division may be useful.

To look for the pauses in speech, HAL checks for two neighboring digits that are both equal to nine. Write the recursive class method gap that takes an int parameter and returns a boolean. Return true if and only if the parameter includes two consecutive nine digits. For example, gap(99) and gap(399391) return true, but gap(949), gap(0), gap(9) return false.

Determine the worst case running time for the gap method as a function of the number of digits to be analyzed. Give your answer in big-O notation. You only need to write the order of growth; you do NOT need to explain how you got your answer.

Your Answer: ______________
4. [Algorithm Analysis – 15 points (3 points each)].

For each method below determine the order of growth of the worst case running time. Write your answer to the right of the method using big-O notation. You only need to write the order of growth; you do NOT need to explain how you got your answer.

(a) public static void threeRows(int[][] arr) {
    int n = arr.length; // N for this problem
    for(int i = 0; i < n; i++)
        for(int j=0; j < 3; j++)
            System.out.println("arr["+i+"]["+j+"]=" + arr[i][j]);
}

(b) public static int quickCount(int[] arr, int start) {
    int n = start; // N for this problem
    int count = 0;
    while(n>0) {
        count += arr[n];
        n = n / 2;
        if(count > 1000) return count;
    }
    return count;
}

(c) public static void crisscross(int size) {
    int n = size; // N for this problem
    for(int i = 0; i < size; i++) {
        for(int j = 0; j<size; j++)
            System.out.print( (i+j)%2 == 0 ? "X" : "O");
        System.out.println();
    }
}

(d) // N = initial value of hi-lo+1
public int foo(int[] arr, int key, int lo, int hi) {
    if(lo > hi) return -1;
    if(arr[hi] == key)
        return hi;
    return foo(arr,key,lo , hi-1);
}

(e) // N = array.length
public void bar(int[] array) {
    for (int i = 0; i < array.length - 1; i++)
        for (int j = i; 0 <= j; j--) {
            if (array[j] > array[j + 1]) swap(array,j,j+1);
            else j= 0;
        }
    // assume swap(array, x,y) swaps x\text{th} y\text{th} array elements i.e. a constant time operation.
5. Sorting Algorithms – 12 points (6+5+1).

(a) Complete the 6 missing entries in the following table to indicate the order of growth in running time of each sorting algorithm studied in CS125. Use Big-O notation:

<table>
<thead>
<tr>
<th>Name of Sorting Algorithm</th>
<th>Best case</th>
<th>Worst case</th>
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<tbody>
<tr>
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<td>O( N^2 )</td>
<td>?</td>
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<td>?</td>
<td>O( N log N )</td>
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<tr>
<td>Quicksort</td>
<td>?</td>
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(b) Complete the following method to implement a recursive selection sort. Assume findMin and swap are already defined: findMin(a,x,y) returns the index of the minimum value of array elements \{a[x],a[x+1]...,a[y]\}; swap(array,x,y) exchanges the values of the x^{th} and y^{th} array elements.

```java
public static void mysort(int[] arr, __________________________

    if( __________________________
        return;

    int i = findMin( arr, __________________________

    swap( arr, __________________________

    mysort( arr, __________________________
}
```


```java
public static int f2 (int[] A, int lo, int hi, int p){
    if (hi == lo) Answer:________________________
        if (A[lo] < p) return lo; else return lo-1;
    else if (A[lo] <= p)
        return f2 (A, lo+1, hi, p);
    else{
        swap(A, lo, hi);
        return f2 (A, lo, hi-1, p);
    }
}
```
6. Festive Tree – 15 points.

Complete the three class methods (Utility.prcc, Festive.main, Festive.tree) below to print an ASCII pine tree. You are not permitted to use loops in the prcc or tree methods. The recursive method tree must use Utility class prcc method for any text output. Your program will print trees of different heights, inverted or normal depending on the user's responses. Note the height of the tree does not include the row with the star.

<table>
<thead>
<tr>
<th>height=1, inverted=false</th>
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```java
public class Utility {
    /** Prints the character 'c' 'count' times then followed by a newline if 'newline' is true. */
    public static void prcc(char c, int count, boolean newline) {
        public class Festive {
            public static void main(String[] args) {
                System.out.println(prcc('c', 5, false));
            }
        }
    }
}
```
public class Festive {

    // Add height input logic, then call your recursive tree method
    // If the user enters a negative height, redisplay the height question - "height?"
    // and obtain a new response from the user.
    // Once the user has entered a zero or positive height integer value, print the tree and exit.

    public static void main(String[] arg) {
        System.out.println("Upside down tree? Y/N");
        boolean inverted = TextIO.getlnBoolean();
    }

    // write your tree() method here:

} // end of main

// write your tree() method here:
7. Sorting – 12 points (4+4+4).

(a) HAL unwinds after a long day by sorting the world’s greatest chess masters by their age. The unsorted data is shown in the array below, indexed from 0 to 11

| 95 | 23 | 60 | 48 | 89 | 16 | 45 | 19 | 82 | 44 | 61 | 31 |

If HAL passes this array into selectionSort, as well as passing 0 and 11 as the initial values of lo and hi, what are the contents of the array just as the 6th recursive call is starting? Count the initial call, when passed 0 and 11 as arguments, as the start of the first call.

(b) If HAL passes the original array (95,23...) into Mergesort, as well as passing 0 and 11 as the initial values of lo and hi, what are the array contents just before the last merge (i.e. the final Merge call in the MergeSort call)?

(c) HAL completes a recursive Quicksort partition on the array below: Assume the pivot is 48 and is stored somewhere else. Show the array after every time an element has been placed into one of the partitions. Indicate the current bounds of each partition with [ ] brackets. If a section of array does not change from one row to the next, to save time you may circle that part of the array instead of copying the values. Finally, indicate where the pivot value would be swapped in. You may not need all of the rows.

| [ 22 | 52 | 84 | 89 | 41 | 50 | 38 | 60 | 83 ] |
8. Don’t quote me– 12 points (5 + 7)

a) Add a public copy constructor to the following Quotes class. The copy constructor will perform a deep copy of the String array: However, to reduce memory requirements do not create additional String objects. You may use a loop in the constructor code.

```java
public class Quotes {
    private String[] quotes;
    public int count() { return quotes.length; }
    public String get(int i) { return quotes[i]; }
    public Quotes(String[] arr) { this.quotes = arr; }
    public Quotes(Quotes q) {
        // Write your code here
    }
}
```

b) Create a class 'ActorQuotes' that extends Quotes.
   - Add a private data member 'name' of type String and public method getName.
   - Provide a constructor which initializes the Quotes superclass to an empty String array and the private member to the constructor's parameter.
   - Provide a copy constructor which performs a copy of the source object using the super classes' copy constructor and copies the reference to the name field.