Final Examination
CS 125 Introduction to Computer Science
Fall 2009
3 Hours

PLEASE READ THE FOLLOWING CAREFULLY
• You may not leave with this exam script. You must hand it in and your scratch sheet before you leave.
• Please write your NetID in the top-right corner of each sheet.
• This is a closed book and closed notes exam.
• You are not allowed to use the break, continue, or switch statements on this exam.

Furthermore, you cannot use loops in any problem unless otherwise stated.
• Unless we say otherwise in the specific problem, you can assume all values entered by the user will be acceptable input for that program.
• When you write code, you may use a shorthand for System.out and TextIO input and output methods provided it is obvious to the graders which method you are using. For example it is acceptable to use Sprintln in place of System.out.println and to use Sprintln in place of System.out.print. Likewise, you can use T.rln(), in place of TextIO.readln().
• For full marks correct syntax is required: Ensure all statements include a semicolon and the correct use of upper/lower case, single quotes and double quotes.

<table>
<thead>
<tr>
<th>Problem</th>
<th>Points</th>
<th>Score</th>
<th>Grader</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
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<td>2</td>
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<td>8</td>
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<td>Bonus</td>
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<tr>
<td>Total</td>
<td>105</td>
<td></td>
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</tbody>
</table>
1. Concepts – 10 points (2 points each)

1. Carefully analyze the following mystery program. What is the last value to be printed?

```java
public class Mystery {
    public static void main(String[] arg) {
        mystery(1);
    }
    
    public static void mystery(int v)
        System.out.println(v);
        if(v == 4) return;
        if(v < 4) mystery(7-v);
        else mystery(9-v);
        System.out.println(-v);
    }
}
```

Your answer: _______

2. I measure the running time of particular sorting algorithm for different sizes of arrays of randomly ordered integers. I can approximate the running time with the following formula (N is the number of integers to sort).

\[
\text{time} \ (\text{milliseconds}) = 0.12 + 0.03 \ N + 0.24 \ N^2
\]

Suggest one sorting algorithm discussed in CS125 that is consistent with the above formula.

Your answer: _____________________

3. Which one of the following must be true if the statement "this.foo++; " is part of a valid Java program?

a) The above code must be inside a public (static) class method.
b) The above code must be inside a private (static) class method.
c) The class contains a public class method named "foo".
d) The above code must be inside an instance method.
e) The local variable named "foo" is immutable.

Your answer: _______

4. Which data structure was used to hold Robots of Challenge7-RecursiveKnight? Circle the correct answer.

- Red-black tree
- Skip-list
- Hash
- Linked-list
- Priority queue
- Map
- FIFO queue
- Tree

5. Circle the best response below to complete the following: When a software engineer has finished developing and testing the code on their local machine, they will __________ their work to the subversion server.

- regionate
debug
- checkout
- execute
- commit
- sandwich
2. Fast Flood Simulation – 14 points

You may not use loops in this question. Write a complete program to recursively simulate fast flooding of a large geographic area. The terrain is represented as an evenly-spaced square grid of \( N \) by \( N \) miles (\( N \) is odd), each grid square represents 1 square mile. 

Flooding starts at the center square and will recursively attempt to flood the four nearest neighbors (NSEW). Water will flow into a neighbor if it is lower and dry. Write a main method and a recursive method to determine which grid squares quickly become wet and print the result.

In a different class named Given, three public class methods are already implemented:

```java
public class Given {
    public static int getN() {...}
    public static double getHeight(int x, int y) {...}
    public static void display(boolean[][] wet, int xx) {...}
}
```

- `getN` returns an odd integer, the number of rows (and columns) of the grid.
- `getHeight` returns the elevation (always positive for valid square) for the requested \((x,y)\) square. Returns 0 if \((x,y)\) is out-of-bounds, \(x<0,y<0,x>=N\), or, \(y>=N\).
- `display` prints out the flood map (W's and _'s). If you choose row-first, `wet[x][y]`, use \(xx=0\); for column-first data, `wet[y][x]`, \(xx=1\).

An example for \(N=5\) is below. Flooding starts at the center square * and wets 13 squares.

<table>
<thead>
<tr>
<th>x</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3</td>
<td>2</td>
<td>1</td>
<td>4</td>
<td>3</td>
</tr>
<tr>
<td>2</td>
<td>4</td>
<td>6</td>
<td>8</td>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td>3</td>
<td>5</td>
<td>6</td>
<td>8</td>
<td>4</td>
<td>5</td>
</tr>
<tr>
<td>4</td>
<td>2</td>
<td>4</td>
<td>2</td>
<td>1</td>
<td>2</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>2D Wetted Array</th>
<th>Program output</th>
</tr>
</thead>
<tbody>
<tr>
<td>T T T F F</td>
<td>Wetted=13</td>
</tr>
<tr>
<td>T F F F F</td>
<td>W w w _ _</td>
</tr>
<tr>
<td>T T T F F</td>
<td>w _ _ _ _</td>
</tr>
<tr>
<td>T T F F F</td>
<td>w w w _ _</td>
</tr>
<tr>
<td>T T T T F</td>
<td>w w _ _ _</td>
</tr>
</tbody>
</table>

Write a complete Java class "FloodSim" with two methods: A main method and a recursive method. Your main method will create a two dimensional array of booleans to represent which squares become wet (for each square, true=wet, false=dry) so that the flood map can be calculated by the recursive method. After using your recursive method print out `Wetted=` followed by the total number of squares wetted and finally call the given `display` method to print out the map.

Your recursive method "flood" will modify the 2D array and return an integer – the total number of squares wetted. Consider base cases to handle out-of-bounds \((x,y)\) coordinates, already wet squares and squares that are same height or higher than the calling square.

All grid squares are initially dry. Water only flows downhill: A wet square will recursively cause a neighboring cell also to be wetted if the neighbor cell has a lower elevation than its wet neighbor. For this simple simulation recursively visit the four immediate neighbors \((x+1,y) (x-1,y) (x,y+1)\) and \((x, y-1)\), and the water's height remains the land elevation of the square. Cells that are already wet are not re-wetted and are not doubly-counted.

Hint: Do you need to change the wet array before or after the recursive call?
2. Fast Flood Simulation Continued
Write your program here
3. Recursion on Linked Lists – 14 points (3+3+4+4)

Complete the `Link` class by writing the methods described below. **Do not use loops, or create any more methods (other than those specified), class or instance variables.**

```java
public class Link {
    private Link next; // null if this is the last link
    private int value;

    public Link(Link n, int v) {next = n; value = v;}
}
```

1. Write a recursive instance method `count` that takes no parameters and returns an `int`. Return the number of links that hold the value zero, with the exception that the last link in the list is not included in the count. For example, for the linked list, `{(first) 5→0→3→1→0→0 (last)}` it would return the value 2.

2. Write a recursive instance method `square` that takes no parameters and returns a boolean. The effect of calling this method is to square the value of each link. Return true if the last link's new value is greater than 99. Otherwise return `false`. For example, the linked list, `{5→0→11}` would become `{25→0→121}` and return the value `true`. 
3. Recursion on Linked Lists Continued

**Do not use loops, or create any more methods (other than those specified), class or instance variables.**

3. Write a recursive instance method named `findBad` that takes no parameters and returns a reference to a Link. The result of calling `findBad` is a reference to the first link that has a value greater than the next link's value. If no such link exists return null. For example, for `{5 → 6 → 7 → 3 → 2}` it would return a reference to the third link ("7").

4. Write a recursive method `modify` to replace each link's value with the next link's original value. The last link's value should be set to zero. For example if the linked list is `{(first)4 → 3 → 2(last)}`. The final values will be `{3 → 2 → 0}`. You are free to choose the parameters and return value required (if any) to implement your recursive function.
4. Algorithm Analysis – 15 points (3 points each)

For each method determine the order of growth of the *worst case* running time as N increases. Write your answer to the right of the method using big O notation. You only need to write the order of growth; you do NOT need to explain how you got your answer.

```java
public static double f1(double[][] array) {
    int N = array[0].length;
    double b = Math.random();
    for(int i = 0; i < 3; i++)
        for(int j = N - 1; j > 0; j--)
            b *= N * N * array[i][j];
    return b;
}
```

```java
public static int f2(int[] arr) {
    int count = arr.length - 1;
    while(count > 0) {
        if(arr[count] < 0)
            count -= 7;
        count = count - arr.length / 50;
    }
    return count;
}
```

```java
public static boolean f3(double[][] array) {
    for(int i=0;i<array.length;i++)
        for(int j=0;j<i;j++)
            if(array[i][j] == 0) return true;
    return false;
}
```

```java
public boolean f4(int[] arr, int lo, int hi) {
    if(lo == hi) return false;
    if(arr[hi] * arr[lo]>10)
        return true;
    return f4(arr,lo+1 , hi);
}
```

```java
public int f5(int[] array, int x) {
    int m = array.length-1;
    while(array[m] > x && m>0)
        m=m/2;
    return m;
}
```
5. Complexity Analysis of Mergesort – 14 points

Use Big O notation to complete the following Order of Growth table for sorting N items using the simple Mergesort studied in CS125. (Pseudo-code is shown to the right).

<table>
<thead>
<tr>
<th>For N items</th>
<th>Best Case</th>
<th>Worst Case</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Running Time</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2. Space requirements</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

3. Why does Mergesort need more memory than Quicksort?

The following questions refer to the above pseudo-code for the Mergesort algorithm.

4. For the following array what are the array values just after executing the very first call to the `merge` function?

<table>
<thead>
<tr>
<th>Initial values</th>
<th>13</th>
<th>8</th>
<th>26</th>
<th>53</th>
<th>14</th>
<th>9</th>
<th>2</th>
<th>38</th>
</tr>
</thead>
<tbody>
<tr>
<td>After first <code>merge</code> call</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

5. How many times will `merge` (not `mergesort`; see code above) be executed (activated) to completely sort 8 items? Hint: Sketching an activation diagram may be useful.

```
# Activations of merge(arr,lo,mid,mid+1,hi): ______
```

6. For the following array what are the array values just before executing the very last call to `merge`?

<table>
<thead>
<tr>
<th>Initial values</th>
<th>13</th>
<th>8</th>
<th>26</th>
<th>53</th>
<th>14</th>
<th>9</th>
<th>2</th>
<th>38</th>
</tr>
</thead>
<tbody>
<tr>
<td>Before final <code>merge</code> call</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

7. It takes 100 milliseconds for Mergesort to process an array of 10,000 integers that are initially in random order. If the array was in almost sorted order, how many integers could now be sorted by Mergesort in approximately 100 milliseconds?

   a) 100 or fewer
   b) 1,000
   c) 10,000
   d) 100,000
   e) 1,000,000 or greater

   Your choice: ______
6. Quicksort – 12 points

1. "For quicksort, the median value would be an excellent pivot value but it is impractical to find." Briefly explain the two facts (good pivot but impractical) in the above statement.

2. Circle the one best answer: The last value of the subarray to be partitioned is a reasonable pivot value to choose when the array contents are initially______.
   
   randomly ordered,  pre-sorted,  sorted in reverse

3. An adversary wishes to disable your surgical robot. They know your application uses a particular Quicksort and are able to send it a large amount of carefully ordered data to be sorted. What is the worst case running time of Quicksort in this case? Use Big O notation.

   Write your answer here: ______

Consider the following algorithm (swap swaps the values at the left and right indices).

   int mystery(int[] data, int t) {
     int left = 0, right = data.length-1
     while (left < right) {
       if (data[left] >= t) {
         swap(data, left, right);
         right --;
       }
     else left ++;
   }
   return left;

4. Show the contents of the following array after mystery(data, 19) completes.

<table>
<thead>
<tr>
<th>Initial data</th>
<th>13</th>
<th>8</th>
<th>14</th>
<th>18</th>
<th>1</th>
<th>20</th>
<th>2</th>
<th>38</th>
</tr>
</thead>
<tbody>
<tr>
<td>After mystery returns</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

5. Circle the one best description of the above mystery function.

   quicksort, find-minimum, binary-search, merge-sort, selection-sort, partition
7. Arthur Dent (Objects and Conditionals) – 12 Points

You are writing a Java program to help Arthur Dent choose how to respond to a question. Arthur has 3 options: Agree, Disagree, or Shrug. Use the following rules to decide which option Arthur will use:

1. Arthur will shrug if the audience is larger than one person or the question text is empty.
2. If rule 1 does not apply, Arthur will agree if the question is a joke and is 140 characters or less.
3. If neither rule 1 nor rule 2 applies, Arthur will disagree.

Complete the following Arthur class by writing the following:

• A public constructor that takes a string, int and boolean and sets all instance variables defined below with parameter values of the same types as the instance variables. However, if the question's parameter value is null set the question variable to an empty string.

• A public instance method, "choose" with no parameters that returns one of 3 Strings, "Agree", "Disagree", or "Shrug", based on the above rules. Your code must have exactly 3 return statements, one for each condition.

public class Arthur {

    private String question; // the question text
    private int audience; // size of audience
    private boolean joke; // true if the question is a joke

    // constructor

    public Arthur(String question, int audience, boolean joke) {
        this.question = question != null ? question : "";
        this.audience = audience;
        this.joke = joke;
    }

    // choose method

    public String choose() {
        if (question.isEmpty() || audience <= 1) {
            return "Shrug";
        } else if (question.length() <= 140 && joke) {
            return "Agree";
        } else {
            return "Disagree";
        }
    }

}
8. Santa's Elves Todo List – 9 Points

Read the given code. Complete the class "Presents" started below, according to the following specification. You may use loops in this question.

- A public constructor that takes an integer parameter – the maximum capacity of the list and will also initialize data to a new String array. This is the only time you will create a new array.

- A public instance method `add` that takes a String – the name of the present to add – and returns a boolean. Assume the name is non-null. If there is space left in the array, store if after the last present previously added, increment size and return true, otherwise ignore the present and return false. **Do not create a new array.**

- A public instance method `equals` that takes a reference to a Java object and returns a boolean. Return `true` if and only if the other object is also a Presents object and contains an identical list of presents in the same order: You are required to use `instanceof` to verify object type and `String.equals` to compare present names.

```java
public class Presents {
    private String[] data; // valid strings stored in 0... size-1
    private int size; // initially =0, =data.length once array is full
    public int getSize() { return size; }
    public String get(int i) { return data[i]; }
}
```
9. Social Network Bonus Challenge – 5 points

You may use loops in this question. See the Movie and Actor class below. Each actor object represents a famous actor and the movies that they appeared in. Each movie object represents a movie - specifically its title and the listed actors. The boolean flag, 'printed' is initially false for all actors. The same actor may appear in many movies i.e. the same actor object may be referenced in several actors arrays of different movies. You can assume a constructor and instance variables have already been written. Write the following recursive instance method 'visit' in the Actor class. Do not create any other instance or class variables or any other methods.

The visit method takes no parameters and returns an integer. The effect of calling this recursive method is such that all actors' names in this network are printed once (one name per line) and their printed flag is set to true. Return the total number of unique actors visited. Assume all references in the arrays are valid and non-null.

```java
public class Movie {
    public String title;
    public Actor[] actors;
}

public class Actor {
    private String name;
    private Movie[] movies;
    private boolean printed;
    // constructor not shown.
}
```

END OF THE EXAM
Scratch paper. You may tear this off but need to turn it in with your exam.