

MAC.  
SKE in Practice.

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Lecture 5

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RECALL

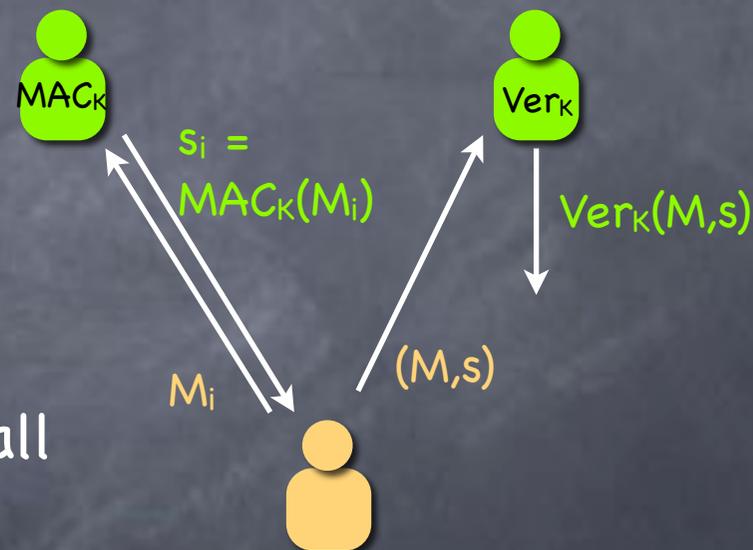
# Message Authentication Codes

- A single short key shared by Alice and Bob
  - Can sign any (polynomial) number of messages

- A triple (KeyGen, MAC, Verify)

- Correctness: For all  $K$  from KeyGen, and all messages  $M$ ,  $\text{Verify}_K(M, \text{MAC}_K(M))=1$

- Security: probability that an adversary can produce  $(M,s)$  s.t.  $\text{Verify}_K(M,s)=1$  is negligible unless Alice had computed and output  $s=\text{MAC}_K(M)$



$$\text{Advantage} = \Pr[ \text{Ver}_K(M,s)=1 \text{ and } (M,s) \notin \{(M_i,s_i)\} ]$$

# One-time MAC



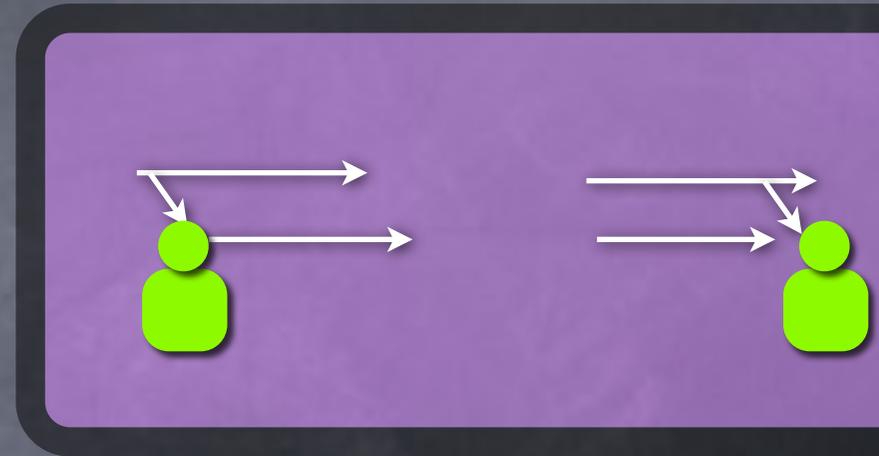
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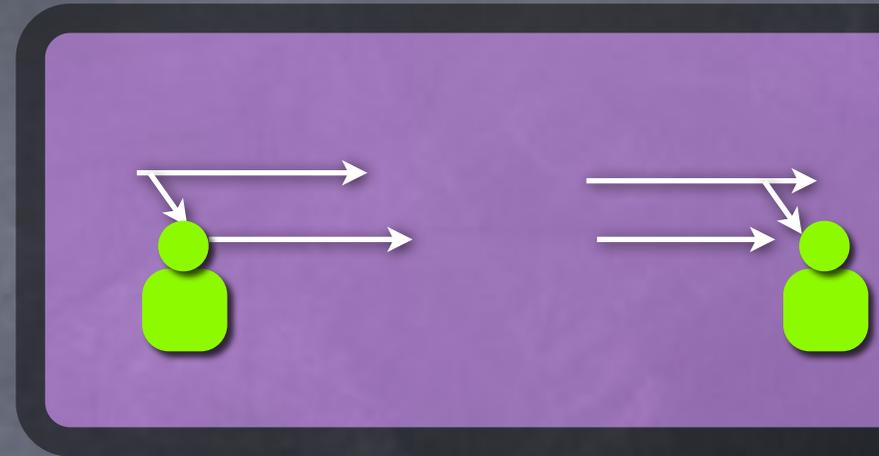
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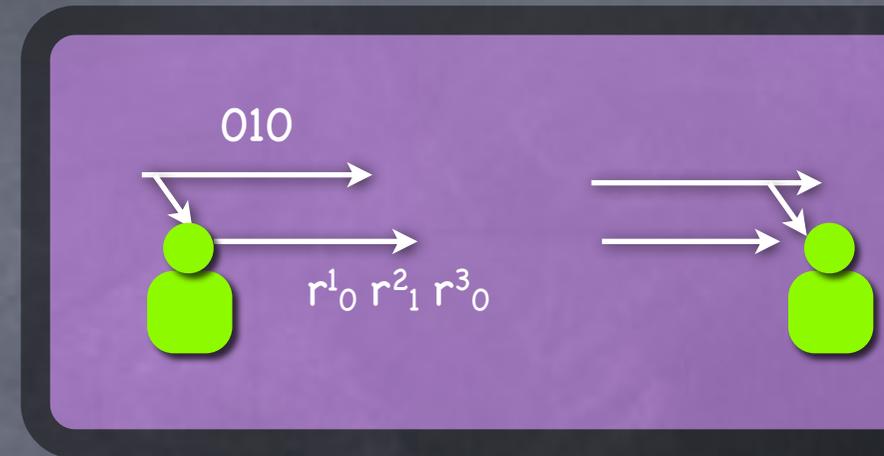
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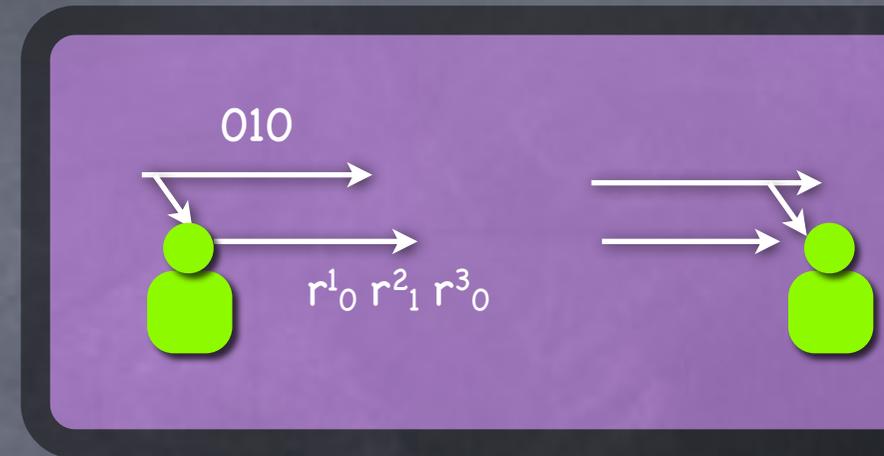
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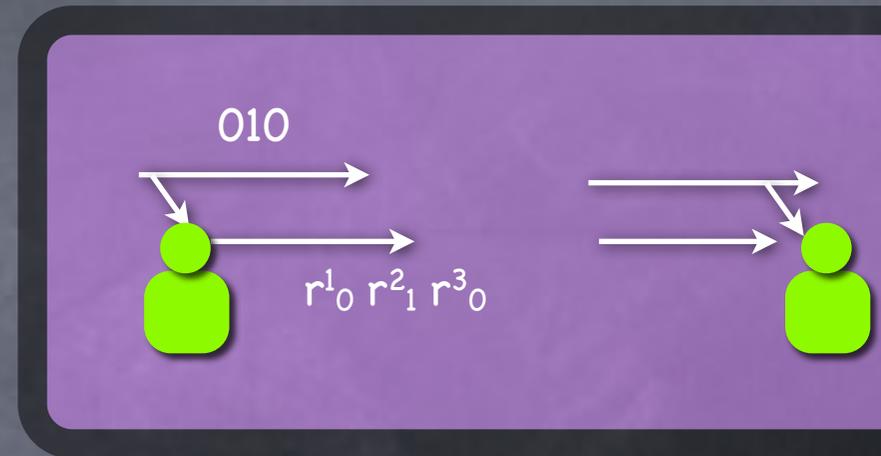
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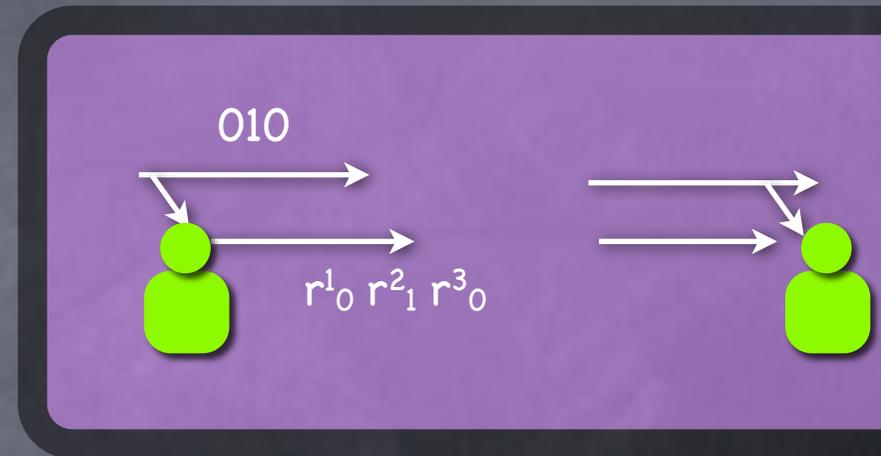
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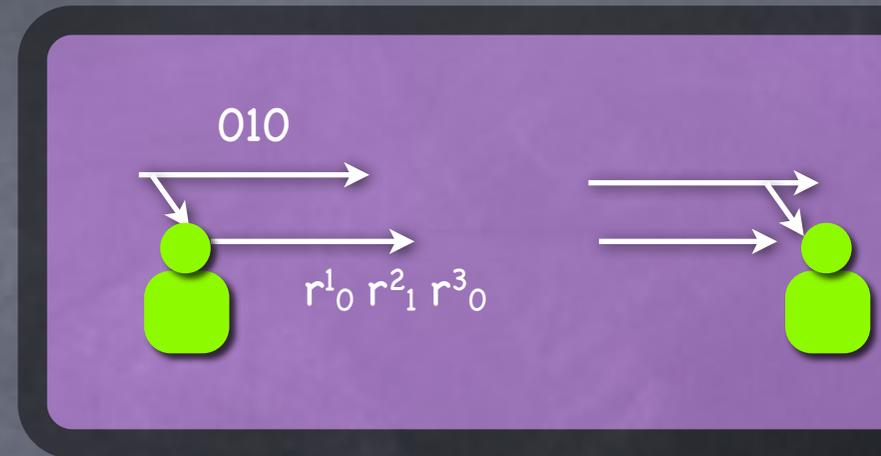
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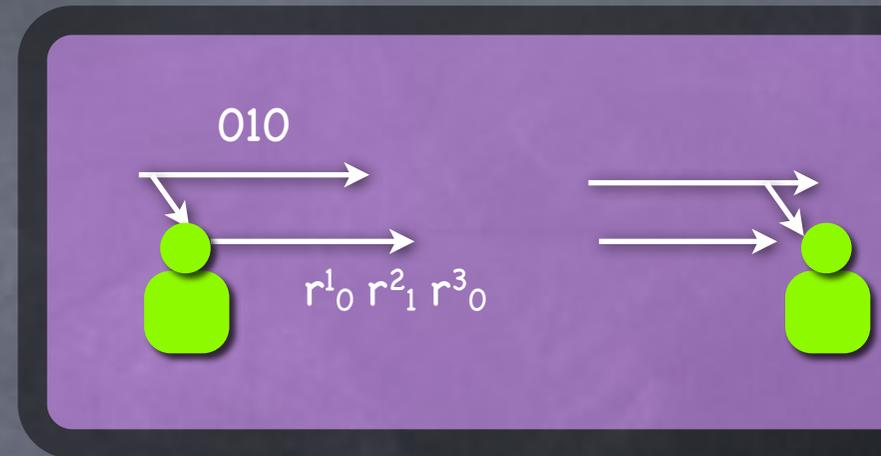
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  - No computational restriction on adversary



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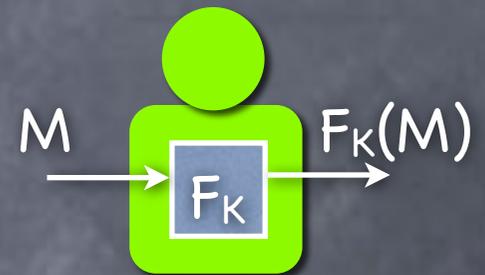
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  - Note: if random function  $R$ , probability of forgery,  $\epsilon_{MAC}^* = 2^{-m(k)}$



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- Inefficient! Tag length increases with message length

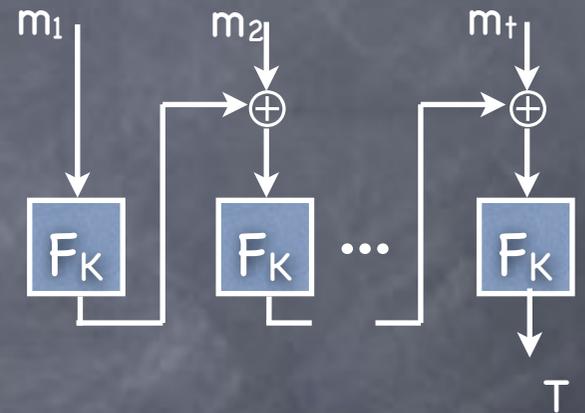
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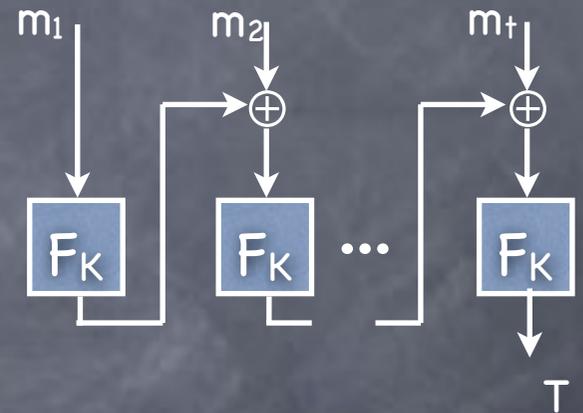
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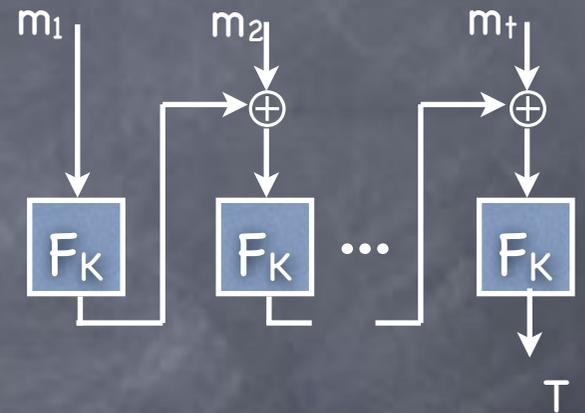
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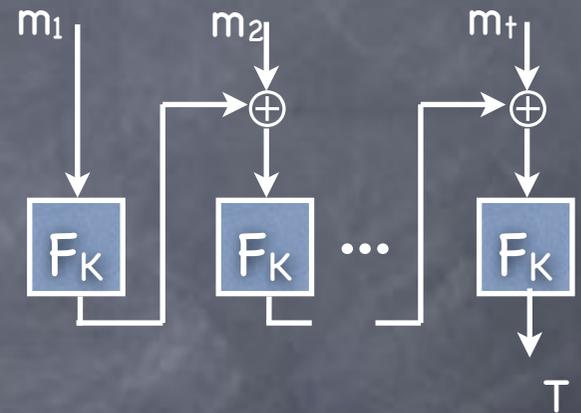
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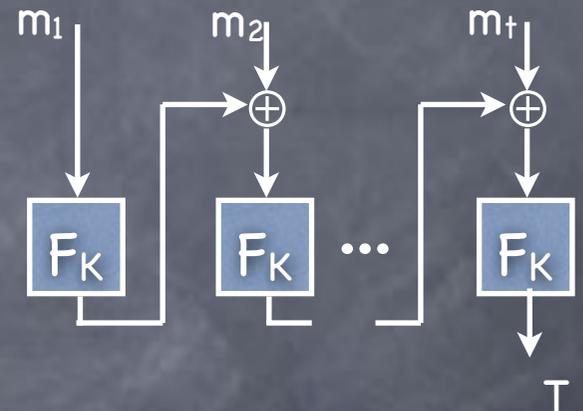
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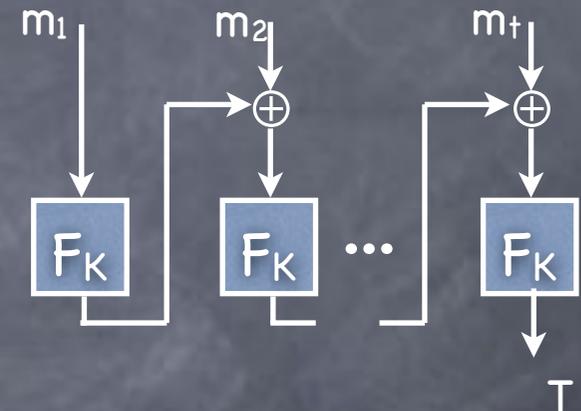
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  - Else attacks possible (by extending a previously signed message)



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- Later: Hash-based HMAC used in TLS and IPSec IETF Standard. 1997

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- NIST Standard: Use a block-cipher in CTR mode

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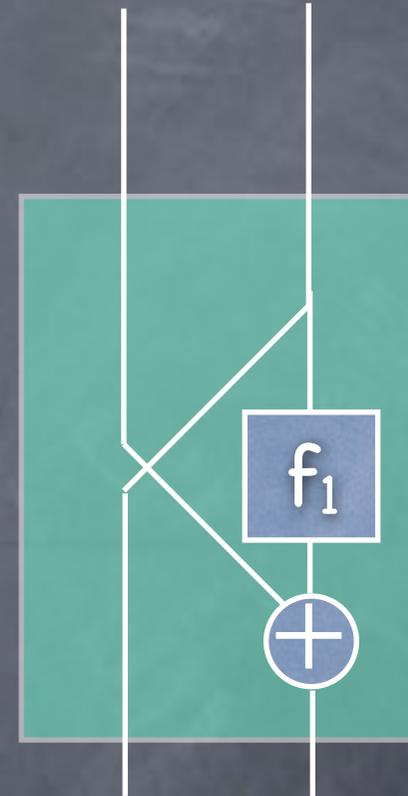
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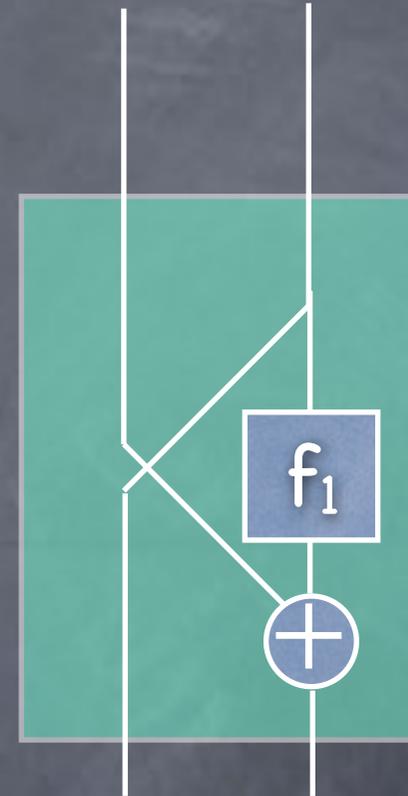
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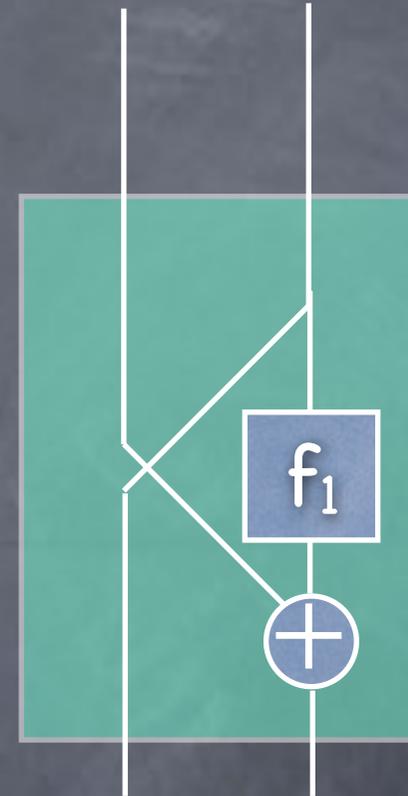
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# Feistel Network

- Building a permutation from a (block) function
  - Let  $f: \{0,1\}^m \rightarrow \{0,1\}^m$  be an arbitrary function
  - $F_f: \{0,1\}^{2m} \rightarrow \{0,1\}^{2m}$  defined as  $F_f(x,y) = (y, x \oplus f(y))$ 
    - $F_f$  is a permutation (Why?)
      - Can invert (How?)
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- Fewer layers do not suffice! [Exercise]



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- Triple DES: 3 successive applications of DES (or DES<sup>-1</sup>) with 3 keys

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  - No “simple” hardness assumption known to imply any sort of security for AES



General Math

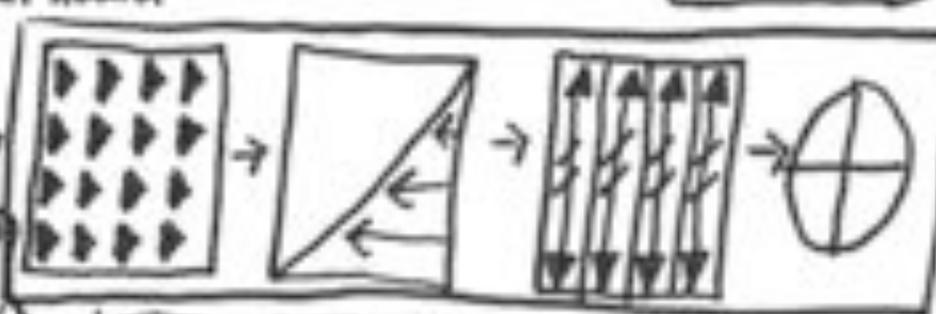
11B = AES Polynomial =  $x^8 + x^4 + x^3 + x + 1$

Fast Multiply

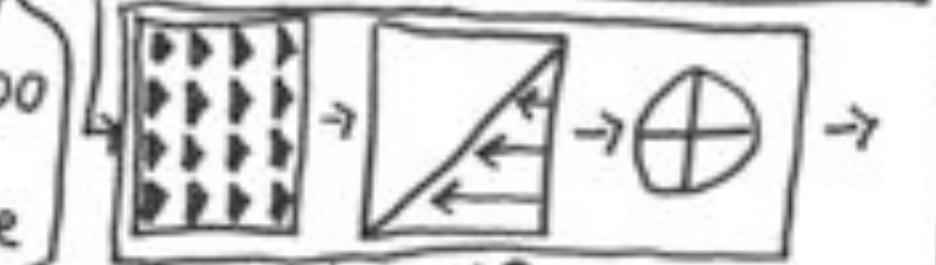
$x \cdot a(x) = (a \ll 1) \oplus (a_7 = 1) ? 1B : 00$

$\log(x \cdot y) = \log(x) + \log(y)$

Use  $(x+1) = 03$  for log base



Intermediate Rounds #	Key
9	128
11	192
13	256



?	?	?	?
?	?	?	?
?	?	?	?
?	?	?	?

Ciphertext

S-Box (SRD)

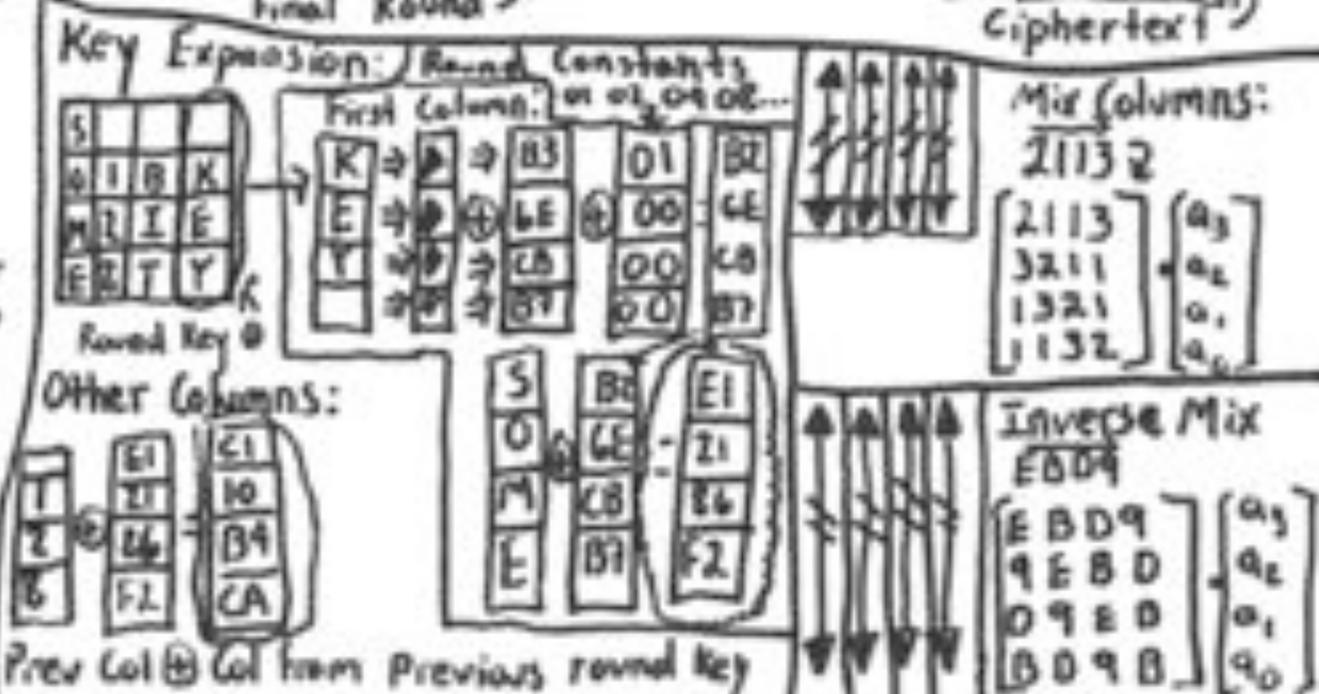
$SRD[a] = f(g(a))$

$g(a) = a^{-1} \text{ mod } m(x)$

Sea Think  $5^3 \oplus 6^3$

5 is and 3 0's  $[0110\ 0011]^T$

11111000	$a_6$	⊕	00000001
01111100	$a_5$		
00111110	$a_4$		
00011111	$a_3$		
10001111	$a_2$		
11000111	$a_1$		
11100011	$a_0$		
11110001	$a_0$		



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  - Meet-in-the-middle, linear cryptanalysis, differential cryptanalysis, impossible differential cryptanalysis, boomerang attack, integral cryptanalysis, cube attack, ...

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    - e.g. RC4 in BitTorrent, Skype, PDF

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  - AE with Associated Data: Allows unencrypted (but authenticated) parts of the plaintext, for headers etc.