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# Confidentiality Policies

CS461/ECE422 Computer Security I  
Fall 2010

# Reading

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- Chapter 5 in CS
- Bell-LaPadula and McLean papers linked on class web site if you are interested in the proofs

# Outline

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- Overview
  - Mandatory versus discretionary controls
  - What is a confidentiality model
- Bell-LaPadula Model
  - General idea
  - Description of rules
- Tranquility
- Controversy
  - †-property
  - System Z

# MAC vs DAC

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- Discretionary Access Control (DAC)
  - Normal users can change access control state directly assuming they have appropriate permissions
  - Access control implemented in standard OS's, e.g., Unix, Linux, Windows
  - Access control is at the discretion of the user
- Mandatory Access Control (MAC)
  - Access decisions cannot be changed by normal rules
  - Generally enforced by system wide set of rules
  - Normal user cannot change access control schema
- “Strong” system security requires MAC
  - Normal users cannot be trusted

# Confidentiality Policy

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- Goal: prevent the unauthorized disclosure of information
  - Deals with information flow
  - Integrity incidental
- Multi-level security models are best-known examples
  - Bell-LaPadula Model basis for many, or most, of these

# Bell-LaPadula Model, Step 1

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- Security levels arranged in linear ordering
  - Top Secret: highest
  - Secret
  - Confidential
  - Unclassified: lowest
- Levels consist of *security clearance*  $L(s)$ 
  - Objects have *security classification*  $L(o)$

# Example

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<i>security level</i>	<i>subject</i>	<i>object</i>
Top Secret	Tamara	Personnel Files
Secret	Samuel	E-Mail Files
Confidential	Claire	Activity Logs
Unclassified	Ulaley	Telephone Lists

- Tamara can read all files
- Claire cannot read Personnel or E-Mail Files
- Ulaley can only read Telephone Lists

# Reading Information

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- Information flows *up*, not *down*
  - “Reads up” disallowed, “reads down” allowed
- Simple Security Condition (Step 1)
  - Subject  $s$  can read object  $o$  iff,  $L(o) \leq L(s)$  and  $s$  has permission to read  $o$ 
    - Note: combines mandatory control (relationship of security levels) and discretionary control (the required permission)
  - Sometimes called “no reads up” rule



# Writing Information

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- Information flows up, not down
  - “Writes up” allowed, “writes down” disallowed
- \*-Property (Step 1)
  - Subject  $s$  can write object  $o$  iff  $L(s) \leq L(o)$  and  $s$  has permission to write  $o$ 
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  - Sometimes called “no writes down” rule

# Basic Security Theorem, Step 1

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- If a system is initially in a secure state, and every transition of the system satisfies the simple security condition (step 1), and the \*-property (step 1), then every state of the system is secure
  - Proof: induct on the number of transitions
- Meaning of “secure” in axiomatic

# Bell-LaPadula Model, Step 2

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- Expand notion of security level to include categories (also called compartments)
- Security level is (*clearance, category set*)
- Examples
  - ( Top Secret, { NUC, EUR, ASI } )
  - ( Confidential, { EUR, ASI } )
  - ( Secret, { NUC, ASI } )

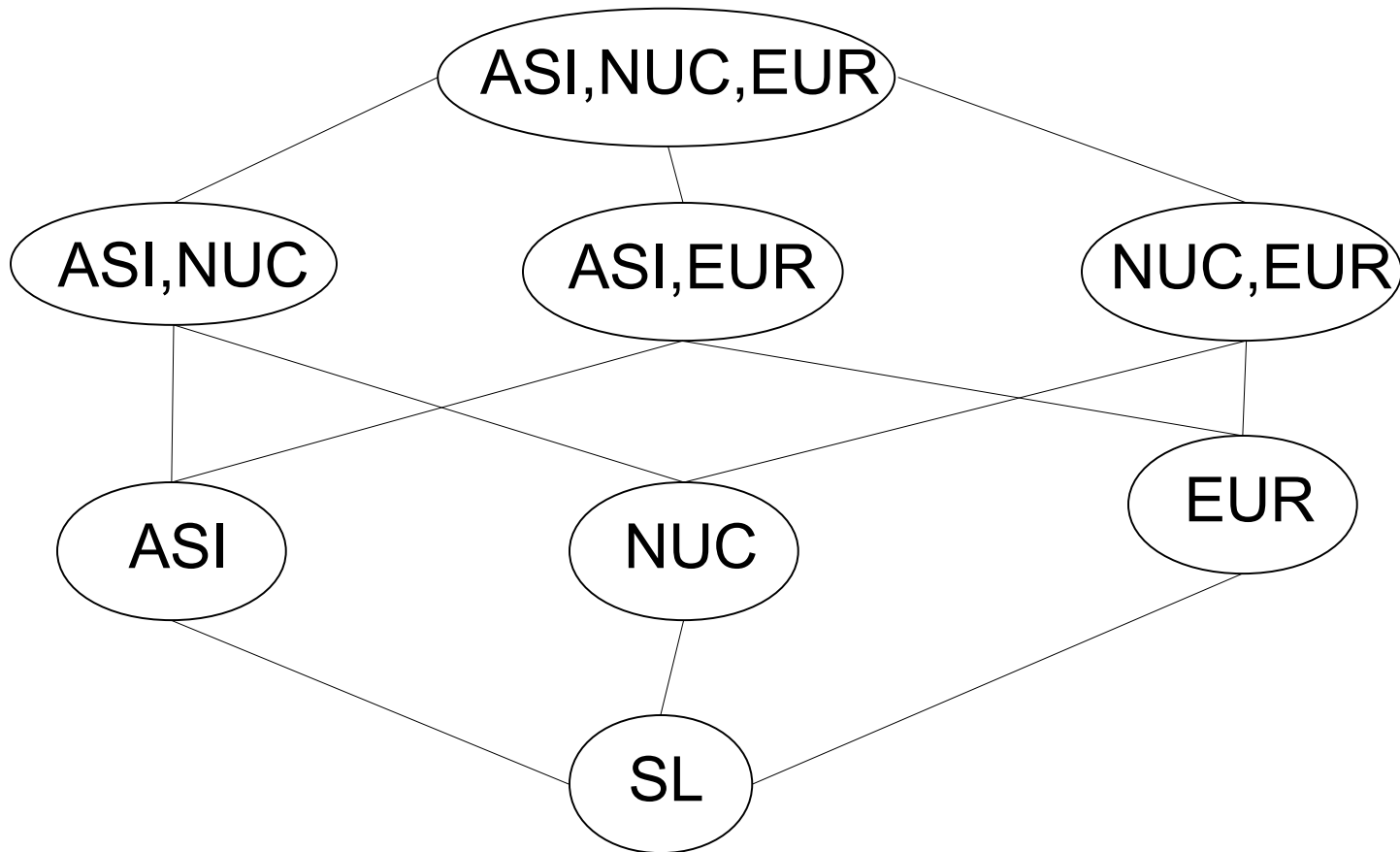
# Levels and Lattices

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- $(A, C) \text{ dom } (A', C')$  iff  $A' \leq A$  and  $C' \subseteq C$
- Examples
  - (Top Secret, {NUC, ASI})  $\text{dom}$  (Secret, {NUC})
  - (Secret, {NUC, EUR})  $\text{dom}$  (Confidential, {NUC, EUR})
  - (Top Secret, {NUC})  $\neg \text{dom}$  (Confidential, {EUR})
  - (Secret, {NUC})  $\neg \text{dom}$  (Confidential, {NUC, EUR})
- Let  $C$  be set of classifications,  $K$  set of categories. Set of security levels  $L = C \times K$ ,  $\text{dom}$  form lattice
  - *Partially ordered set*
  - *Any pair of elements*
    - *Has a greatest lower bound*
    - *Has a least upper bound*

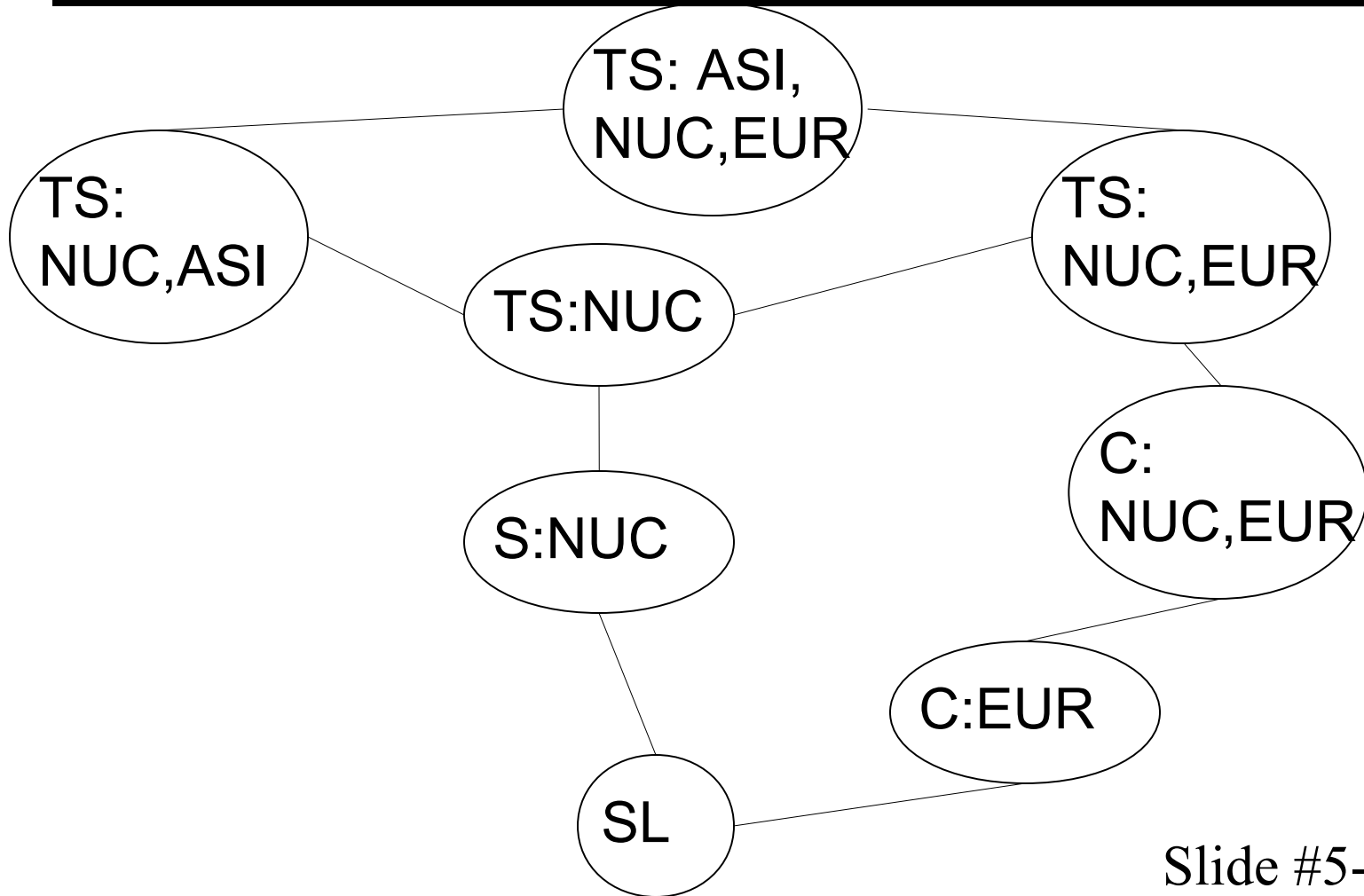
# Example Lattice

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# Subset Lattice

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# Levels and Ordering

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- Security levels partially ordered
  - Any pair of security levels may (or may not) be related by *dom*
- “dominates” serves the role of “greater than” in step 1
  - “greater than” is a total ordering, though

# Reading Information

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    - Note: combines mandatory control (relationship of security levels) and discretionary control (the required permission)
  - Sometimes called “no writes down” rule

# Basic Security Theorem, Step 2

---

- If a system is initially in a secure state, and every transition of the system satisfies the simple security condition (step 2), and the \*-property (step 2), then every state of the system is secure
  - Proof: induct on the number of transitions
  - In actual Basic Security Theorem, discretionary access control treated as third property, and simple security property and \*-property phrased to eliminate discretionary part of the definitions — but simpler to express the way done here.

# Problem

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- Colonel has (Secret, {NUC, EUR}) clearance
- Major has (Secret, {EUR}) clearance
- Can Major write data that Colonel can read?
- Can Major read data that Colonel wrote?

# Solution

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- Define maximum, current levels for subjects
  - $maxlevel(s) \text{ dom } curlevel(s)$
- Example
  - Treat Major as an object (Colonel is writing to him/her)
  - Colonel has  $maxlevel$  (Secret, { NUC, EUR })
  - Colonel sets  $curlevel$  to (Secret, { EUR })
  - Now  $L(\text{Major}) \text{ dom } curlevel(\text{Colonel})$ 
    - Colonel can write to Major without violating “no writes down”
  - Does  $L(s)$  mean  $curlevel(s)$  or  $maxlevel(s)$ ?
    - Formally, we need a more precise notation

# Adjustments to “write up”

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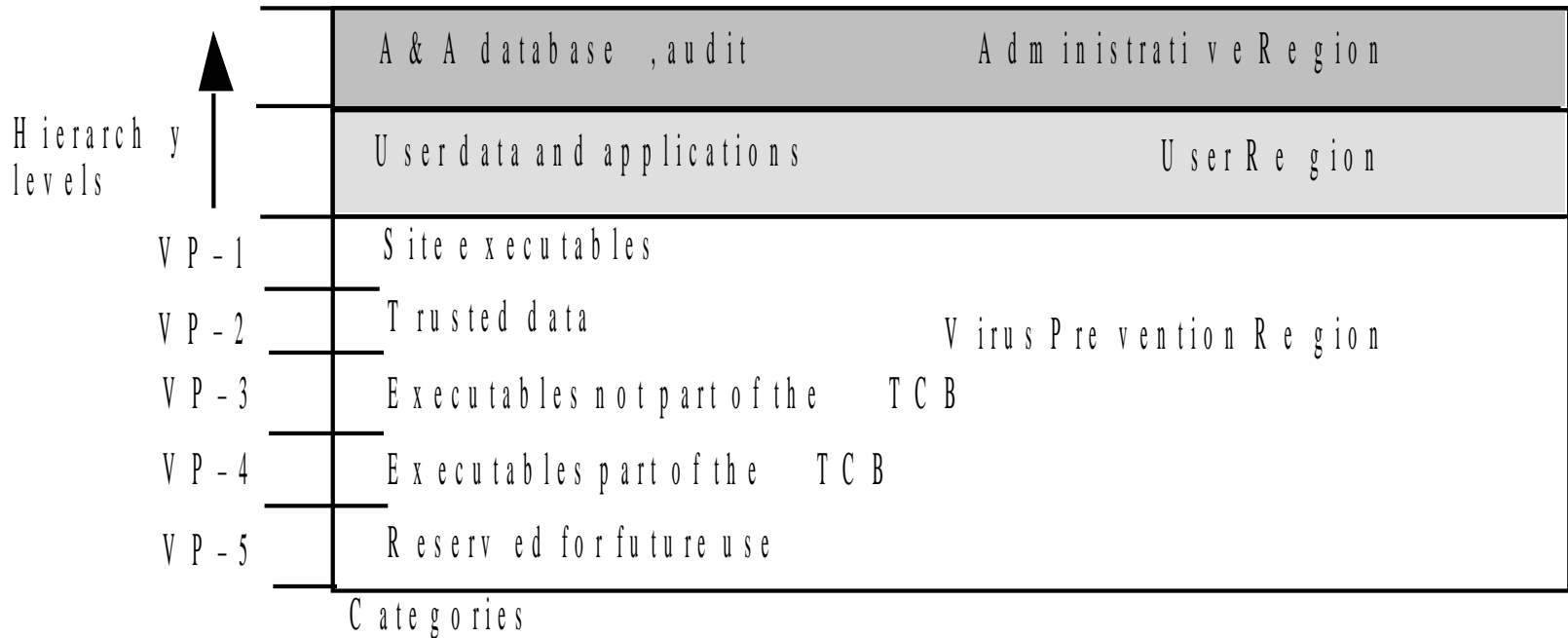
- General write permission is both read and write
  - So both simple security condition and \*-property apply
  - $S \text{ dom } O$  and  $O \text{ dom } S$  means  $S=O$
- BLP discuss **append** as a “pure” write so writeup still applies

# DG/UX System

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- Provides mandatory access controls
  - MAC label identifies security level
  - Default labels, but can define others
- Initially
  - Subjects assigned MAC label of parent
    - Initial label assigned to user, kept in Authorization and Authentication database
  - Object assigned label at creation
    - Explicit labels stored as part of attributes
    - Implicit labels determined from parent directory

# MAC Regions



IMPL\_HI is “maximum” (least upper bound) of all levels

IMPL\_LO is “minimum” (greatest lower bound) of all levels

# Directory Problem

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- Process  $p$  at MAC\_A tries to create file  $/tmp/x$
- $/tmp/x$  exists but has MAC label MAC\_B
  - Assume  $MAC\_B \not\sqsubseteq dom\ MAC\_A$
- Create fails
  - Now  $p$  knows a file named  $x$  with a higher label exists
- Fix: only programs with same MAC label as directory can create files in the directory
  - Now compilation won't work, mail can't be delivered



# Multilevel Directory

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- Directory with a set of subdirectories, one per label
  - Not normally visible to user
  - $p$  creating  $/tmp/x$  actually creates  $/tmp/d/x$  where  $d$  is directory corresponding to  $MAC\_A$
  - All  $p$ 's references to  $/tmp$  go to  $/tmp/d$
- $p$   $cd$ 's to  $/tmp/a$ , then to  $..$ 
  - System call  $stat(“.”, \&buf)$  returns inode number of real directory
  - System call  $dg\_stat(“.”, \&buf)$  returns inode of  $/tmp$

# Object Labels

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- Requirement: every file system object must have MAC label
  1. Roots of file systems have explicit MAC labels
    - If mounted file system has no label, it gets label of mount point
  1. Object with implicit MAC label inherits label of parent

# Object Labels

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- Problem: object has two names
  - */x/y/z*, */a/b/c* refer to same object
  - *y* has explicit label IMPL\_HI
  - *b* has explicit label IMPL\_B
- Case 1: hard link created while file system on DG/UX system, so ...
  1. Creating hard link requires explicit label
    - If implicit, label made explicit
    - Moving a file makes label explicit

# Object Labels

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- Case 2: hard link exists when file system mounted
  - No objects on paths have explicit labels: paths have same *implicit* labels
  - An object on path acquires an explicit label: implicit label of child must be preserved

so ...

- Change to directory label makes child labels explicit *before* the change

# Object Labels

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- Symbolic links are files, and treated as such, so ...
1. When resolving symbolic link, label of object is label of target of the link
    - System needs access to the symbolic link itself

# Using MAC Labels

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- Simple security condition implemented
- \*-property not fully implemented
  - Process MAC must equal object MAC
  - Writing allowed only at same security level
- Overly restrictive in practice

# MAC Tuples

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- Up to 3 MAC ranges (one per region)
- MAC range is a set of labels with upper, lower bound
  - Upper bound must dominate lower bound of range
- Examples
  1. [(Secret, {NUC}), (Top Secret, {NUC})]
    - [(Secret,  $\emptyset$ ), (Top Secret, {NUC, EUR, ASI})]
  1. [(Confidential, {ASI}), (Secret, {NUC, ASI})]

# MAC Ranges

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1. [(Secret, {NUC}), (Top Secret, {NUC})]
- [(Secret,  $\emptyset$ ), (Top Secret, {NUC, EUR, ASI})]
1. [(Confidential, {ASI}), (Secret, {NUC, ASI})]
- (Top Secret, {NUC}) in ranges 1, 2
- (Secret, {NUC, ASI}) in ranges 2, 3
- [(Secret, {ASI}), (Top Secret, {EUR})] not valid range
  - as (Top Secret, {EUR})  $\neg dom$  (Secret, {ASI})



# Objects and Tuples

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- Objects must have MAC labels
  - May also have MAC label
  - If both, tuple overrides label
- Example
  - Paper has MAC range:  
[(Secret, {EUR}), (Top Secret, {NUC, EUR})]

# MAC Tuples

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- Process can read object when:
  - Object MAC range  $(lr, hr)$ ; process MAC label  $pl$
  - $pl \text{ dom } hr$ 
    - Process MAC label grants read access to upper bound of range
- Example
  - Peter, with label  $(\text{Secret}, \{\text{EUR}\})$ , cannot read paper
    - $(\text{Secret}, \{\text{EUR}\}) \not\text{ dom } (\text{Top Secret}, \{\text{NUC}, \text{EUR}\})$
  - Paul, with label  $(\text{Top Secret}, \{\text{NUC}, \text{EUR}, \text{ASI}\})$  can read paper
    - $(\text{Top Secret}, \{\text{NUC}, \text{EUR}, \text{ASI}\}) \text{ dom } (\text{Top Secret}, \{\text{NUC}, \text{EUR}\})$

# MAC Tuples

---

- Process can write object when:
  - Object MAC range  $(lr, hr)$ ; process MAC label  $pl$
  - $pl \in (lr, hr)$ 
    - Process MAC label grants write access to any label in range
- Example
  - Peter, with label  $(\text{Secret}, \{\text{EUR}\})$ , can write paper
    - $(\text{Top Secret}, \{\text{NUC}, \text{EUR}\}) \text{ dom } (\text{Secret}, \{\text{EUR}\})$  and  $(\text{Secret}, \{\text{EUR}\}) \text{ dom } (\text{Secret}, \{\text{EUR}\})$
  - Paul, with label  $(\text{Top Secret}, \{\text{NUC}, \text{EUR}, \text{ASI}\})$ , cannot read paper
    - $(\text{Top Secret}, \{\text{NUC}, \text{EUR}\}) \not\text{ dom } (\text{Top Secret}, \{\text{NUC}, \text{EUR}, \text{ASI}\})$

# Formal Model

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- $S$  subjects,  $O$  objects,  $P$  rights
  - Defined rights:  $\underline{r}$  read,  $\underline{a}$  write,  $\underline{w}$  read/write,  $\underline{e}$  empty
- $M$  set of possible access control matrices
  - That is,  $m \in M$  iff  $m \subseteq S \times O \times P$
- Let  $C$  be a set of clearances, and  $K$  a set of categories
  - $L = C \times K$  set of security levels

# Security Level Assignments

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- $F = \{ (f_s, f_o, f_c) \}$
- $f_s : S \rightarrow L$ 
  - $f_s(s)$  *maximum* security level of subject  $s$
- $f_o : S \rightarrow L$ 
  - $f_o(o)$  security level of object  $o$
- $f_c : S \rightarrow L$ 
  - $f_c(s)$  *current* security level of subject  $s$

# More Definitions

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- Hierarchy functions  $h: O \rightarrow P(O)$
- Requirements
  - $o_i \neq o_j \Rightarrow h(o_i) \cap h(o_j) = \emptyset$
  - There is no set  $\{ o_1, \dots, o_{k+1} \} \subseteq O$  such that, for  $i = 1, \dots, k$ ,  $o_{i+1} \in h(o_i)$  and  $o_{k+1} = o_1$ .
- Defines a tree
  - Tree hierarchy; take  $h(o)$  to be the set of children of  $o$
  - No two objects have any common children (#1)
  - There are no loops (#2)

# States and Requests

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- $V$  set of states
  - $v = (b, m, f, h) \in M \times M \times F \times (O \rightarrow P(O))$ 
    - $b$  mandatory rights
    - $m$  discretionary rights
    - $b$  is like  $m$ , but excludes rights not allowed by  $f$
- $R$  set of requests for access
- $D$  set of outcomes
  - y allowed, n not allowed, i illegal, o error

# Actions

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- $W$  set of actions of the system
  - $W \subseteq R \times D \times V \times V$
  - $(r, v)$  transitions to  $(d, v')$

$$v \xrightarrow[r \text{ yields } d]{(r, d, v, v') \in W} v'$$



# History

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- $X =$  set of sequences  $(r_1, r_2, \dots, r_t)$  of requests,  $t \in \mathbb{N}$  and  $t > 1$
- $Y =$  set of sequences  $(d_1, d_2, \dots, d_t)$  of decisions,  $t \in \mathbb{N}$  and  $t > 1$
- $Z =$  set of sequences  $(v_0, v_1, \dots, v_t)$  of states,  $t \in \mathbb{N}$
- Interpretation
  - At time  $t \in \mathbb{N}$ , system is in state  $z_{t-1} \in V$ ; request  $x_t \in R$  causes system to make decision  $y_t \in D$ , transitioning the system into a (possibly new) state  $z_t \in V$

# History Continued

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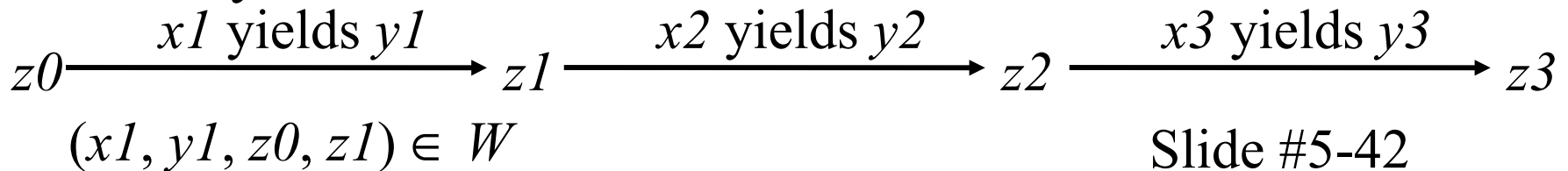
- System representation

$$\Sigma(R, D, W, z_0) \in X \times Y \times Z$$

–  $(x, y, z) \in \Sigma(R, D, W, z_0)$  iff  $(x_t, y_t, z_t, z_{t-1}) \in W$   
for all  $t$

–  $(x, y, z)$  called an *appearance* of  $\Sigma(R, D, W, z_0)$

– Each  $z_t$  in an appearance  $(x, y, z)$  is a *state* of the  
system



# Rules

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- A function  $\rho : R \times V \rightarrow D \times V$  together with a start state determines a system

$$z_0 \xrightarrow{x_1 \text{ yields } \rho(x_1, z_0)} z_1 \xrightarrow{x_2 \text{ yields } \rho(x_2, z_1)} z_2 \xrightarrow{x_3 \text{ yields } \rho(x_3, z_2)} z_3$$

# Example

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- $S = \{ s \}, O = \{ o \}, P = \{ \underline{r}, \underline{w} \}$
- $C = \{ \text{High}, \text{Low} \}, K = \{ \text{All} \}$
- For every  $f \in F$ , either  $f_c(s) = ( \text{High}, \{ \text{All} \} )$  or  $f_c(s) = ( \text{Low}, \{ \text{All} \} )$
- Initial State:
  - $b_1 = \{ (s, o, \underline{r}) \}, m_1 \in M$  gives  $s$  read access over  $o$ , and for  $f_1 \in F, f_{c,1}(s) = ( \text{High}, \{ \text{All} \} ), f_{o,1}(o) = ( \text{Low}, \{ \text{All} \} )$
  - Call this state  $v_0 = (b_1, m_1, f_1, h_1) \in V$ .

# First Transition

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- Now suppose in state  $v_0$ :  $S = \{s, s'\}$
- Suppose  $f_{c,1}(s \uparrow) = (\text{Low}, \{\text{All}\})$
- $m_1 \in M$  gives  $s$  and  $s'$  read access over  $o$
- As  $s'$  not written to  $o$ ,  $b_1 = \{ (s, o, \underline{r}) \}$
- $z_0 = v_0$ ; if  $s'$  requests  $r_1$  to write to  $o$ :
  - System decides  $d_1 = \underline{y}$
  - New state  $v_1 = (b_2, m_1, f_1, h_1) \in V$
  - $b_2 = \{ (s, o, \underline{r}), (s', o, \underline{w}) \}$
  - Here,  $x = (r_1)$ ,  $y = (\underline{y})$ ,  $z = (v_0, v_1)$

# Second Transition

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- Current state  $v_1 = (b_2, m_1, f_1, h_1) \in V$ 
  - $b_2 = \{ (s, o, \underline{r}), (s', o, \underline{w}) \}$
  - $f_{c,1}(s) = (\text{High}, \{ \text{All} \}), f_{o,1}(o) = (\text{Low}, \{ \text{All} \})$
- $s'$  requests  $r_2$  to write to  $o$ :
  - System decides  $d_2 = \underline{n}$  (as  $f_{c,1}(s) \text{ dom } f_{o,1}(o)$ )
  - New state  $v_2 = (b_2, m_1, f_1, h_1) \in V$
  - $b_2 = \{ (s, o, \underline{r}), (s', o, \underline{w}) \}$
  - So,  $x = (r_1, r_2), y = (\underline{y}, \underline{n}), z = (v_0, v_1, v_2)$ , where  $v_2 = v_1$

# Basic Security Theorem

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- Define action, secure formally
  - Using a bit of foreshadowing for “secure”
- Restate properties formally
  - Simple security condition
  - \*-property
  - Discretionary security property
- State conditions for properties to hold
- State Basic Security Theorem

# Action

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- A request and decision that causes the system to move from one state to another
  - Final state may be the same as initial state
- $(r, d, v, v') \in R \times D \times V \times V$  is an *action* of  $\Sigma(R, D, W, z_0)$  iff there is an  $(x, y, z) \in \Sigma(R, D, W, z_0)$  and a  $t \in N$  such that  $(r, d, v, v') = (x_t, y_t, z_{t-1}, z_t)$ 
  - Request  $r$  made when system in state  $v$ ; decision  $d$  moves system into (possibly the same) state  $v'$
  - Correspondence with  $(x_t, y_t, z_{t-1}, z_t)$  makes states, requests, part of a sequence



e empty  
a write  
r read  
w read/write

# Simple Security Condition

- $(s, o, p) \in S \times O \times P$  satisfies the *simple security condition relative to  $f$*  (written *ssc rel  $f$* ) iff one of the following holds:
  - $p = \underline{e}$  or  $p = \underline{a}$
  - $p = \underline{r}$  or  $p = \underline{w}$  and  $f_s(s) \text{ dom } f_o(o)$
- Holds vacuously if rights do not involve reading
- If all elements of  $b$  satisfy *ssc rel  $f$* , then state satisfies simple security condition
- If all states satisfy simple security condition, system satisfies simple security condition

# Necessary and Sufficient

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- $\forall \Sigma(R, D, W, z_0)$  satisfies the simple security condition for a secure state  $z_0$  iff every action  $(r, d, (b, m, f, h), (b', m', f', h'))$  satisfies
- Every  $(s, o, p) \in b - b'$  satisfies *ssc rel f*
  - Every  $(s, o, p) \in b'$  that does not satisfy *ssc rel f* is not in  $b$
- Note: “secure” means  $z_0$  satisfies *ssc rel f*
  - First says every  $(s, o, p)$  added satisfies *ssc rel f*; second says any  $(s, o, p)$  in  $b'$  that does not satisfy *ssc rel f* is deleted

# \*-Property

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- $b(s: p_1, \dots, p_n)$  set of all objects that  $s$  has  $p_1, \dots, p_n$  access to
- State  $(b, m, f, h)$  satisfies the *\*-property* iff for each  $s \in S$  the following hold:
  - $b(s: \underline{a}) \neq \emptyset \Rightarrow [\forall o \in b(s: \underline{a}) [f_o(o) \text{ dom } f_c(s) ] ]$
  - $b(s: \underline{w}) \neq \emptyset \Rightarrow [\forall o \in b(s: \underline{w}) [f_o(o) = f_c(s) ] ]$
  - $b(s: \underline{r}) \neq \emptyset \Rightarrow [\forall o \in b(s: \underline{r}) [f_c(s) \text{ dom } f_o(o) ] ]$
- Idea: for writing, object dominates subject; for reading, subject dominates object

# \*-Property

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- If all states satisfy simple security condition, system satisfies simple security condition
- If a subset  $S'$  of subjects satisfy \*-property, then \*-property satisfied relative to  $S' \subseteq S$

# Necessary and Sufficient

---

- $\forall \Sigma(R, D, W, z_0)$  satisfies the \*-property relative to  $S' \subseteq S$  for any secure state  $z_0$  iff every action  $(r, d, (b, m, f, h), (b', m', f', h'))$  satisfies the following for every  $s \in S'$
- Every  $(s, o, p) \in b - b'$  satisfies the \*-property relative to  $S'$
  - Every  $(s, o, p) \in b'$  that does not satisfy the \*-property relative to  $S'$  is not in  $b$
- Note: “secure” means  $z_0$  satisfies \*-property relative to  $S'$
  - First says every  $(s, o, p)$  added satisfies the \*-property relative to  $S'$ ; second says any  $(s, o, p)$  in  $b'$  that does not satisfy the \*-property relative to  $S'$  is deleted

# Discretionary Security Property

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- State  $(b, m, f, h)$  satisfies the *discretionary security property* iff, for each  $(s, o, p) \in b$ , then  $p \in m[s, o]$
- Idea: if  $s$  can read  $o$ , then it must have rights to do so in the access control matrix  $m$
- This is the discretionary access control part of the model
  - The other two properties are the mandatory access control parts of the model

# Necessary and Sufficient

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$\forall \Sigma(R, D, W, z_0)$  satisfies the ds-property for any secure state  $z_0$  iff every action  $(r, d, (b, m, f, h), (b', m', f', h'))$  satisfies:

- Every  $(s, o, p) \in b - b'$  satisfies the ds-property
- Every  $(s, o, p) \in b'$  that does not satisfy the ds-property is not in  $b$

- Note: “secure” means  $z_0$  satisfies ds-property
- First says every  $(s, o, p)$  added satisfies the ds-property; second says any  $(s, o, p)$  in  $b'$  that does not satisfy the \*-property is deleted

# Secure

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- A system is *secure* iff it satisfies:
  - Simple security condition
  - \*-property
  - Discretionary security property
- A state meeting these three properties is also said to be secure



# Basic Security Theorem

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$\forall \Sigma(R, D, W, z_0)$  is a secure system if  $z_0$  is a secure state and  $W$  satisfies the conditions for the preceding three theorems

- The theorems are on the slides titled “Necessary and Sufficient”

# Example Instantiation: Multics

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- 11 rules affect rights:
  - set to request, release access
  - set to give, remove access to different subject
  - set to create, reclassify objects
  - set to remove objects
  - set to change subject security level
- Set of “trusted” subjects  $S_T \subseteq S$ 
  - \*-property not enforced; subjects trusted not to violate
- $\forall \Delta(\rho)$  domain of a rule  $\rho$ 
  - determines if components of request are valid

# *get-read* Rule

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- Request  $r = (get, s, o, \underline{r})$ 
  - $s$  gets (requests) the right to read  $o$
- Rule is  $\rho_1(r, v)$ :
  - if**  $(r \neq \Delta(\rho_1))$  **then**  $\rho_1(r, v) = (\underline{i}, v)$ ;
  - else if**  $(f_s(s) \text{ dom } f_o(o) \text{ and } [s \in S_T \text{ or } f_c(s) \text{ dom } f_o(o)])$ 
    - and**  $r \in m[s, o]$
    - then**  $\rho_1(r, v) = (\underline{y}, (b \cup \{ (s, o, \underline{r}) \}, m, f, h))$ ;
  - else**  $\rho_1(r, v) = (\underline{n}, v)$ ;

# Security of Rule

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- The get-read rule preserves the simple security condition, the \*-property relative to  $S - S_T$ , and the ds-property
  - Proof
    - Let  $v$  satisfy all conditions. Let  $\rho_1(r, v) = (d, v')$ . If  $v' = v$ , result is trivial. Suppose  $v' = (b' \cup \{ (s_2, o, \underline{r}) \}, m, f, h)$  where  $b' = b \cup \{ (s_2, o, \underline{r}) \}$ .

# Proof

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- Consider the simple security condition.
  - From the choice of  $v'$ , either  $b' - b = \emptyset$  or  $\{ (s_2, o, \underline{r}) \}$
  - If  $b' - b = \emptyset$ , then  $\{ (s_2, o, \underline{r}) \} \in b$ , so  $v = v'$ , proving that  $v'$  satisfies the simple security condition.
  - If  $b' - b = \{ (s_2, o, \underline{r}) \}$ , because the *get-read* rule requires that  $f_c(s) \text{ dom } f_o(o)$ , an earlier result says that  $v'$  satisfies the simple security condition.

# Proof

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- Consider the \*-property relative to  $S - S_T$ .
  - Either  $s_2 \in S_T$  or  $f_c(s) \text{ dom } f_o(o)$  from the definition of *get-read*
  - If  $s_2 \in S_T$ , then there is nothing to prove.
  - If  $f_c(s) \text{ dom } f_o(o)$ , then condition 3 of the \*-property is trivially satisfied.

# Proof

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- Consider the discretionary security property.
  - Conditions in the *get-read* rule require  $\underline{r} \in m[s, o]$  and either  $b' - b = \emptyset$  or  $\{ (s_2, o, \underline{r}) \}$
  - If  $b' - b = \emptyset$ , then  $\{ (s_2, o, \underline{r}) \} \in b$ , so  $v = v'$ , proving that  $v'$  satisfies the simple security condition.
  - If  $b' - b = \{ (s_2, o, \underline{r}) \}$ , then  $(s_2, o, \underline{r})$  is in  $m$  because that is a condition in the definition of  $\rho_1$ .

# Principle of Tranquility

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- Raising object's security level
  - Information once available to some subjects is no longer available
  - Usually assume information has already been accessed, so this does nothing
- Lowering object's security level
  - The *declassification problem*
  - Essentially, a “write down” violating \*-property
  - Solution: define set of trusted subjects that *sanitize* or remove sensitive information before security level lowered



# Types of Tranquility

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- Strong Tranquility
  - The clearances of subjects, and the classifications of objects, do not change during the lifetime of the system
- Weak Tranquility
  - The clearances of subjects, and the classifications of objects change in accordance with a specified policy.

# Example

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- DG/UX System
  - Only a trusted user (security administrator) can lower object's security level
  - In general, process MAC labels cannot change
    - If a user wants a new MAC label, needs to initiate new process
    - Cumbersome, so user can be designated as able to change process MAC label within a specified range
- Other systems allow multiple labeled windows to address users operating a multiple levels

# Controversy

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- McLean:
  - “value of the BST is much overrated since there is a great deal more to security than it captures. Further, what is captured by the BST is so trivial that it is hard to imagine a realistic security model for which it does not hold.”
  - Basis: given assumptions known to be non-secure, BST can prove a non-secure system to be secure

# †-Property

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- State  $(b, m, f, h)$  satisfies the †-property iff for each  $s \in S$  the following hold:
  - $b(s: \underline{a}) \neq \emptyset \Rightarrow [\forall o \in b(s: \underline{a}) [f_c(s) \text{ dom } f_o(o) ] ]$
  - $b(s: \underline{w}) \neq \emptyset \Rightarrow [\forall o \in b(s: \underline{w}) [f_o(o) = f_c(s) ] ]$
  - $b(s: \underline{r}) \neq \emptyset \Rightarrow [\forall o \in b(s: \underline{r}) [f_c(s) \text{ dom } f_o(o) ] ]$
- Idea: for writing, subject dominates object; for reading, subject also dominates object
- Differs from \*-property in that the mandatory condition for writing is reversed
  - For \*-property, it's object dominates subject

# Analogue

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The following two theorems can be proved

- $\forall \Sigma(R, D, W, z_0)$  satisfies the  $\dagger$ -property relative to  $S' \subseteq S$  for any secure state  $z_0$  iff for every action  $(r, d, (b, m, f, h), (b', m', f', h'))$ ,  $W$  satisfies the following for every  $s \in S'$
- Every  $(s, o, p) \in b - b'$  satisfies the  $\dagger$ -property relative to  $S'$
  - Every  $(s, o, p) \in b'$  that does not satisfy the  $\dagger$ -property relative to  $S'$  is not in  $b$
- $\forall \Sigma(R, D, W, z_0)$  is a secure system if  $z_0$  is a secure state and  $W$  satisfies the conditions for the simple security condition, the  $\dagger$ -property, and the ds-property.

# Problem

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- This system is *clearly* non-secure!
  - Information flows from higher to lower because of the  $\dagger$ -property

# System Z

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- Only one transition rule
  - Get-read(s,o), if s dom o allow read and set all objects to system low
- This system meets BLP requirements for security given weak tranquility
  - Given secure initial state, each subsequent state is secure
- Points out the need to evaluate the transition rules

# Discussion

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- Role of Basic Security Theorem is to demonstrate that rules preserve security
- Key question: what is security?
  - Bell-LaPadula defines it in terms of 3 properties (simple security condition, \*-property, discretionary security property)
  - Theorems are assertions about these properties
  - Rules describe changes to a *particular* system instantiating the model
  - Showing system is secure requires proving rules preserve these 3 properties



# Key Points

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- Confidentiality models restrict flow of information
- Bell-LaPadula models multilevel security
  - Cornerstone of much work in computer security
- Controversy over meaning of security
  - Different definitions produce different results